

# Cathy Fosnot Math Strings

RIGHT HERE, WE HAVE COUNTLESS EBOOK **CATHY FOSNOT MATH STRINGS** AND COLLECTIONS TO CHECK OUT. WE ADDITIONALLY PRESENT VARIANT TYPES AND WITH TYPE OF THE BOOKS TO BROWSE. THE SUITABLE BOOK, FICTION, HISTORY, NOVEL, SCIENTIFIC RESEARCH, AS WELL AS VARIOUS SUPPLEMENTARY SORTS OF BOOKS ARE READILY GENIAL HERE.

AS THIS CATHY FOSNOT MATH STRINGS, IT ENDS IN THE WORKS MONSTER ONE OF THE FAVORED BOOK CATHY FOSNOT MATH STRINGS COLLECTIONS THAT WE HAVE. THIS IS WHY YOU REMAIN IN THE BEST WEBSITE TO SEE THE UNBELIEVABLE BOOK TO HAVE.

**TEACHING NUMBER IN THE CLASSROOM WITH 4-8 YEAR OLDS** ROBERT J WRIGHT 2014-10-17 BRING THE PRINCIPLES AND PRACTICE OF THE ACCLAIMED MATHEMATICS RECOVERY PROGRAMME TO WHOLE-CLASS TEACHING! WHY INVEST IN THE NEW EDITION? IN FULL-COLOUR WITH A REVISED LAYOUT FOR CLEARER NAVIGATION MORE UP-TO-DATE TASKS, ACTIVITIES AND REAL CLASSROOM EXAMPLES LEARNING TRAJECTORIES FOR GUIDING INSTRUCTION AND TRACKING PROGRESS ON KEY TOPICS EXTRA RESOURCES ONLINE ON THE COMPANION WEBSITE PART OF THE BEST-SELLING MATHS RECOVERY SERIES, THIS PRACTICAL, STEP-BY-STEP GUIDE TO CLASSROOM INSTRUCTION TAKES AN INQUIRY-BASED APPROACH TO ASSESS CHILDREN'S KNOWLEDGE AND BUILD ON THIS TO DEVELOP A FIRM FOUNDATION OF UNDERSTANDING AND CONFIDENCE IN MATHEMATICS. TOPICS COVERED RANGE FROM BEGINNING NUMBER AND EARLY COUNTING STRATEGIES TO MULTI-DIGIT ADDITION AND SUBTRACTION RIGHT THROUGH TO MULTIPLICATION AND DIVISION. AN INVALUABLE RESOURCE FOR USE ON PRE-SERVICE TEACHER TRAINING COURSES AND FOR ALL PRIMARY CLASSROOM TEACHERS AND ASSISTANTS, INCLUDING EXPERIENCED MATHEMATICS RECOVERY INSTRUCTORS, AS WELL AS LEARNING SUPPORT PERSONNEL, PRIMARY MATHEMATICS ADVISORS, NUMERACY CONSULTANTS AND EDUCATIONAL PSYCHOLOGISTS. WHAT EXTRAS ARE ON THE COMPANION WEBSITE? DOWNLOADABLE EXTRA CHAPTER RESOURCES LIKE PRINT-OUT GRIDS, WORKSHEETS, CARDS AND MUCH MORE A FACILITATOR'S GUIDE THAT CAN BE USED EITHER INDIVIDUALLY OR IN GROUP STUDY TO HELP YOU GET THE MOST OUT OF THE MATERIAL IN-CLASS VIDEO DEMONSTRATIONS TO CLEARLY SHOW HOW THE INSTRUCTIONAL ACTIVITIES IN THE BOOK ARE USED IN THE CLASSROOM WEBINAR DISCUSSING THE KEY POINTS IN THE BOOK AND HOW IT SUPPORTS YOUR TEACHING VISIT THE COMPANION WEBSITE AT [HTTPS://STUDY.SAGEPUB.COM/WRIGHTTNC](https://study.sagepub.com/wrighttnc) "RESEARCH INFORMS PRACTICE IN THIS EASY TO ACCESS RESOURCE. EACH CHAPTER GIVES EDUCATORS PRACTICAL, BITE-SIZED ASSESSMENTS, LINKED TO A HOST OF ACTIVITIES THAT HELPS THEM TARGET TEACHING AND DEVELOP THE FIRM FOUNDATIONS WHICH ARE SO VITAL FOR CONFIDENT AND COMPETENT MATHEMATICIANS." - JILL PIOTROWSKI, NUMERACY CONSULTANT, WIGAN LOCAL AUTHORITY, UK "THE CLASSROOM INSTRUCTIONAL FRAMEWORK IN EARLY NUMBER IS RESEARCH-BASED AND PROVIDES A ROADMAP OF NOT ONLY THE WHAT, BUT THE WHEN AND THE HOW TO TEACH ALL ASPECTS OF EARLY NUMBER." - VICKI NALLY, MATHEMATICS CONSULTANT AT CATHOLIC EDUCATION OFFICE, MELBOURNE "THE STRUCTURED APPROACH OFFERS A WEALTH OF RICH AND EASILY IMPLEMENTED CLASSROOM-BASED ACTIVITIES THAT WORK - THOUSANDS OF TEACHERS IN IRELAND ATTEST TO THIS!" - NOREEN O'LOUGHLIN, DIRECTOR MATHS RECOVERY AND MATHS EDUCATION LECTURER, MARY IMMACULATE COLLEGE, LIMERICK, IRELAND

**MINILESSONS FOR OPERATIONS WITH FRACTIONS, DECIMALS, AND PERCENTS, GRADES 5-8** ANTONIA CAMERON 2006 CD-ROMS CONTAIN LESSONS AND VIDEOS OF SIXTH, SEVENTH, AND EIGHTH-GRADE CLASSROOMS.

**MEASURING FOR THE ART SHOW** CATHERINE TWOMEY FOSNOT 2008-03 MEASURING FOR THE ART SHOW: ADDITION ON THE OPEN NUMBER LINE AND SUBTRACTION IS ONE OF EIGHT UNITS IN THE CONTEXTS FOR LEARNING MATHEMATICS' INVESTIGATING NUMBER SENSE, ADDITION, AND SUBTRACTION (K-3) THE FOCUS OF THIS UNIT IS THE DEVELOPMENT OF THE OPEN NUMBER LINE MODEL WITHIN THE CONTEXT OF MEASUREMENT. AS THE UNIT PROGRESSES, THE NUMBER LINE IS USED AS A MODEL FOR DOUBLE-DIGIT ADDITION STRATEGIES. THE UNIT BEGINS WITH THE STORY OF A TEACHER WHO HAS OFFERED TO ORGANIZE AN ART SHOW OF CHILDREN'S WORK AS A SCHOOL FUND-RAISER. THE CHILDREN HAVE PRODUCED BEAUTIFUL PIECES OF ART AND THE TEACHER AND SEVERAL CHILDREN SET OUT TO MAKE SIGNS TO HANG UNDERNEATH EACH PIECE, LISTING THE TITLE OF THE PIECE, THE ARTIST'S NAME, AND THE PRICE. THEY WANT TO MEASURE EACH ART PIECE VERY CAREFULLY SO THAT THE SIGN WILL BE EXACTLY THE SAME LENGTH AS THE PIECE OF ART. BUT THIS HUGE PILE OF WORK IS DAUNTING. THANKFULLY, THE STUDENTS SOON FIGURE OUT A SOLUTION. THEY SORT THE ART BY SIZE, MEASURE EACH SIZE, AND MAKE A BLUEPRINT-A PATTERN STRIP-THAT WILL BE USED FOR CUTTING ALL THE SIGNS. THE STORY SETS THE CONTEXT FOR A SERIES OF INVESTIGATIONS IN THIS UNIT. CHILDREN MEASURE VARIOUS SIZES OF ART PAPER WITH CONNECTING CUBES AND THEN PLACE THE MEASUREMENTS ONTO A LONG STRIP OF ADDING MACHINE PAPER, TO BE USED AS A BLUEPRINT OR PATTERN FOR CUTTING THE SIGNS. AS THE UNIT PROGRESSES, LENGTHS OF FIVES AND TENS ARE INTRODUCED IN PLACE OF THE CUBES AND THE BLUEPRINT IS PROGRESSIVELY DEVELOPED INTO AN OPEN NUMBER LINE-A HELPFUL MODEL USED AS A TOOL TO EXPLORE AND REPRESENT STRATEGIES FOR DOUBLE-DIGIT ADDITION. IN CONTRAST TO A NUMBER LINE WITH

COUNTING NUMBERS WRITTEN BELOW, AN "OPEN" NUMBER LINE IS JUST AN EMPTY LINE USED TO RECORD CHILDREN'S ADDITION (AND LATER SUBTRACTION) STRATEGIES. ONLY THE NUMBERS CHILDREN USE ARE RECORDED AND THE ADDITION IS RECORDED AS LEAPS OR JUMPS. FOR EXAMPLE, IF A CHILD'S STRATEGY FOR ADDING  $18 + 79$  IS TO KEEP 79 WHOLE AND DECOMPOSE THE 18 INTO SMALLER PIECES, MOVING TO A LANDMARK NUMBER OF 80 ( $79 + 1 + 10 + 7$ ), IT WOULD BE RECORDED ON THE OPEN NUMBER LINE. SUCH REPRESENTATIONS HELP CHILDREN MOVE BEYOND TEDIOUS STRATEGIES LIKE COUNTING ONE BY ONE TO STRATEGIES SUCH AS TAKING LEAPS OF TEN, SPLITTING, AND USING LANDMARK NUMBERS. SEVERAL MINILESSONS FOR ADDITION ARE ALSO INCLUDED IN THE UNIT. THESE ARE STRUCTURED AS STRINGS OF RELATED PROBLEMS DESIGNED TO GUIDE LEARNERS MORE EXPLICITLY TOWARD COMPUTATIONAL FLUENCY WITH DOUBLE-DIGIT ADDITION. THE UNIT CULMINATES WITH AN ART SHOW. THUS, AS YOU PROGRESS THROUGH THE UNIT, YOU MAY FIND IT HELPFUL TO WORK WITH THE ART TEACHER IN YOUR SCHOOL TO COLLECT PIECES OF STUDENT ARTWORK. TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://www.contextsforlearning.com)

**EXPLORING PARKS AND PLAYGROUNDS** LYNN TARLOW-HELLMAN 2007 "CONTEXTS FOR LEARNING MATHEMATICS" SERIES IS DESIGNED TO SUPPORT A CONCEPTUAL UNDERSTANDING OF ESSENTIAL MATHEMATICAL IDEAS, STRATEGIES AND MODELS. EACH UNIT PROVIDES A TWO-WEEK SEQUENCE OF INVESTIGATION, MINILESSONS, GAMES, AND OTHER CONTEXTS FOR LEARNING. THE SERIES' 18 CLASSROOM-TESTED UNITS ARE ORGANIZED INTO GRADE-APPROPRIATE LEVELS.

**YOUNG MATHEMATICIANS AT WORK** CATHERINE TWOMEY FOSNOT 2002 IN THIS THIRD VOLUME IN A SERIES OF THREE, FOSNOT AND DOLK FOCUS ON HOW CHILDREN IN GRADES 5-8 CONSTRUCT THEIR KNOWLEDGE OF FRACTIONS, DECIMALS, AND PERCENTS.

**YOUNG MATHEMATICIANS AT WORK** CATHERINE TWOMEY FOSNOT 2001 EXPLAINS HOW CHILDREN BETWEEN THE AGES OF FOUR AND EIGHT CONSTRUCT A DEEP UNDERSTANDING OF NUMBERS AND THE OPERATIONS OF ADDITION AND SUBTRACTION.

**AGES AND TIMELINES** CATHERINE TWOMEY FOSNOT 2008-03 "CONTEXTS FOR LEARNING MATHEMATICS" SERIES IS DESIGNED TO SUPPORT A CONCEPTUAL UNDERSTANDING OF ESSENTIAL MATHEMATICAL IDEAS, STRATEGIES AND MODELS. EACH UNIT PROVIDES A TWO-WEEK SEQUENCE OF INVESTIGATION, MINILESSONS, GAMES, AND OTHER CONTEXTS FOR LEARNING. THE SERIES' 18 CLASSROOM-TESTED UNITS ARE ORGANIZED INTO GRADE-APPROPRIATE LEVELS.

**MINILESSONS FOR OPERATIONS WITH FRACTIONS, DECIMALS, AND PERCENTS** KARA LOUISE IMM 2008-03 MINILESSONS FOR OPERATIONS WITH FRACTIONS IS A YEARLONG RESOURCE GUIDE IN CONTEXTS FOR LEARNING MATHEMATICS' INVESTIGATING FRACTIONS, DECIMALS, AND PERCENTS (4-6) MINILESSONS FOR OPERATIONS WITH FRACTIONS, DECIMALS, AND PERCENTS IS A RESOURCE OF APPROXIMATELY 75 MINILESSONS THAT YOU CAN CHOOSE FROM THROUGHOUT THE YEAR. IN CONTRAST TO INVESTIGATIONS, WHICH CONSTITUTE THE HEART OF THE MATH WORKSHOP, THE MINILESSON IS MORE GUIDED AND MORE EXPLICIT, DESIGNED TO BE USED AT THE START OF MATH WORKSHOP AND TO LAST FOR TEN TO FIFTEEN MINUTES. EACH DAY, NO MATTER WHAT OTHER MATERIALS YOU ARE USING, YOU MIGHT CHOOSE A MINILESSON FROM THIS RESOURCE TO HELP YOUR STUDENTS DEVELOP EFFICIENT COMPUTATION. YOU CAN ALSO USE MINILESSONS WITH SMALL GROUPS OF STUDENTS AS YOU DIFFERENTIATE INSTRUCTION. THE MINILESSONS IN THIS GUIDE WERE DESIGNED TO BE USED IN GRADES 5-6. EACH MINILESSON IS CRAFTED AS A TIGHTLY STRUCTURED SERIES, OR "STRING," OF COMPUTATION PROBLEMS DESIGNED TO ENCOURAGE STUDENTS TO LOOK TO THE NUMBERS FIRST, BEFORE THEY DECIDE ON A COMPUTATION STRATEGY. THE STRINGS ARE LIKELY TO GENERATE DISCUSSION ON CERTAIN STRATEGIES OR BIG IDEAS UNDERLYING AN UNDERSTANDING OF OPERATIONS WITH RATIONAL NUMBERS. ALTHOUGH THE EMPHASIS IS ON THE DEVELOPMENT OF MENTAL ARITHMETIC STRATEGIES, THIS DOES NOT MEAN LEARNERS HAVE TO SOLVE THE PROBLEMS IN THEIR HEADS-BUT IT IS IMPORTANT FOR THEM TO DO THE PROBLEMS WITH THEIR HEADS! IN OTHER WORDS, AS YOU USE THIS GUIDE, ENCOURAGE STUDENTS TO EXAMINE THE NUMBERS IN EACH PROBLEM AND THINK ABOUT CLEVER, EFFICIENT WAYS TO SOLVE IT. THE RELATIONSHIPS BETWEEN THE PROBLEMS IN THE MINILESSON WILL SUPPORT STUDENTS AS THEY PROGRESS THROUGH THE STRING. SEVERAL MODELS ARE EMPLOYED THAT CAN BE HELPFUL FOR COMPUTATION. MONEY AND THE CLOCK ENABLE STUDENTS TO WORK WITH LANDMARK FRACTIONS EASILY. THE DOUBLE OPEN NUMBER LINE ALLOWS FOR GENERALIZABLE STRATEGIES SUCH AS THE USE OF COMMON DENOMINATORS FOR ADDITION AND SUBTRACTION. THE OPEN ARRAY AND THE RATIO TABLE ARE USED WITH MULTIPLICATION AND DIVISION THROUGHOUT TO REPRESENT STUDENT STRATEGIES. TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://www.contextsforlearning.com)

**MATH EXCHANGES** KASSIA OMOHUNDRO WEDEKIND 2011 TRADITIONALLY, SMALL-GROUP MATH INSTRUCTION HAS BEEN USED AS A FORMAT FOR REACHING CHILDREN WHO STRUGGLE TO UNDERSTAND. MATH COACH KASSIA OMOHUNDRO WEDEKIND USES SMALL-GROUP INSTRUCTION AS THE CENTERPIECE OF HER MATH WORKSHOP APPROACH, ENGAGING ALL STUDENTS IN RIGOROUS "MATH EXCHANGES." THE KEY CHARACTERISTICS OF THESE MATHEMATICAL CONVERSATIONS ARE THAT THEY ARE: 1) SHORT, FOCUSED SESSIONS THAT BRING ALL MATHEMATICAL MINDS TOGETHER, 2) RESPONSIVE TO THE NEEDS OF THE SPECIFIC GROUP OF MATHEMATICIANS, AND 3) DESIGNED FOR MEANINGFUL, GUIDED REFLECTION. AS IN READING AND WRITING WORKSHOP, STUDENTS IN

KASSIA'S MATH WORKSHOP ARE BECOMING SELF-DIRECTED AND INDEPENDENT WHILE PARTICIPATING IN A CLASSROOM COMMUNITY OF LEARNERS. THROUGH THE MATH EXCHANGES, STUDENTS FOCUS ON NUMBER SENSE AND THE BIG IDEAS OF MATHEMATICS. TEACHERS GUIDE THE CONVERSATIONS WITH SMALL GROUPS OF STUDENTS, MEDIATING TALK AND THINKING AS STUDENTS SHARE PROBLEM-SOLVING STRATEGIES, DISCUSS HOW MATH WORKS, AND MOVE TOWARD MORE EFFECTIVE AND EFFICIENT APPROACHES AND GREATER MATHEMATICAL UNDERSTANDING. ALTHOUGH GROUNDED IN THEORY AND RESEARCH, MATH EXCHANGES IS WRITTEN FOR PRACTICING TEACHERS AND ANSWERS SUCH QUESTIONS AS THE FOLLOWING: HOW CAN I USE A MATH WORKSHOP APPROACH AND FOLLOW A CERTAIN TEXTBOOK OR SET OF STANDARDS? HOW SHOULD I FORM SMALL GROUPS? AND HOW OFTEN SHOULD I MEET WITH SMALL GROUPS? WHAT SHOULD I FOCUS ON IN SMALL GROUPS? HOW CAN I TELL IF MY GROUPS ARE MAKING PROGRESS? WHAT DO SMALL-GROUP MATH EXCHANGES LOOK LIKE, SOUND LIKE, AND FEEL LIKE?

*THE DOUBLE-DECKER BUS* FOSNOT 2008 THE DOUBLE DECKER BUS: EARLY ADDITION AND SUBTRACTION IS ONE OF EIGHT UNITS IN THE CONTEXTS FOR LEARNING MATHEMATICS' INVESTIGATING NUMBER SENSE, ADDITION, AND SUBTRACTION (K-3) THIS UNIT BEGINS WITH THE STORY OF A DOUBLE-DECKER BUS-A BUS THAT HAS TWO DECKS WITH TEN SEATS ON EACH. FIVE SEATS ON EACH DECK ARE RED AND FIVE SEATS ARE WHITE. THE BUS GOES BY QUICKLY AND THE LITTLE GIRL IN THE STORY, SITTING AT HER BEDROOM WINDOW AND WATCHING, WORKS OUT WAYS TO USE THE COLORS OF THE SEATS TO CALCULATE QUICKLY HOW MANY PEOPLE ARE ON THE BUS. HER FATHER DRIVES A DOUBLE-DECKER BUS AND SHE HELPS HIM FIGURE OUT A WAY TO KNOW HOW MANY EMPTY SEATS THERE ARE ON THE TOP DECK EVEN THOUGH HE CAN'T SEE THEM. THE UNIT INTRODUCES THE ARITHMETIC RACK AS A POWERFUL MODEL AND TOOL TO ACT OUT THE STORY. THE ARITHMETIC RACK IS A CALCULATING FRAME CONSISTING OF TWO ROWS OF TEN BEADS-TWO SETS OF FIVE (ONE RED AND ONE WHITE) IN EACH ROW. (INSTRUCTIONS FOR CREATING OR BUYING YOUR OWN ARITHMETIC RACKS ARE INCLUDED.) COGNITIVE PSYCHOLOGISTS, SUCH AS SUSAN CAREY AND STANISLAS DEHAENE (1999), HAVE SHOWN THAT EVEN TODDLERS CAN RECOGNIZE SMALL AMOUNTS, SUCH AS TWO OR THREE, AS A UNIT AND THAT THIS ABILITY (KNOWN AS "SUBITIZING") IS PROBABLY INNATE. CHILDREN CAN EVEN DO ADDITION AND SUBTRACTION WITH AMOUNTS OF THIS SIZE BECAUSE THEY USE THIS INNATE PERCEPTUAL ABILITY TO SEE THAT THREE IS ONE MORE THAN TWO. USING THE ARITHMETIC RACK ALLOWS KINDERGARTENERS AND FIRST GRADERS TO BUILD ON THEIR NATURAL ABILITY AND SEE FIVE AS A UNIT. WHEN FIVE CAN BE SUBITIZED AS A WHOLE, IT CAN BE USED TO SUPPORT UNDERSTANDING OF 6 AS  $5 + 1$ , 8 AS  $5 + 3$ , OR 4 AS  $5 - 1$ . THE ARITHMETIC RACK ALSO SUPPORTS THE STRATEGIES OF DOUBLES AND NEAR DOUBLES,  $6 + 7 = 6 + 6 + 1$ , AND MAKING TENS,  $9 + 6 = 10 + 5$ . IN THIS UNIT, CHILDREN MOVE THE BEADS ON THE ARITHMETIC RACK TO REPRESENT PASSENGERS GOING FROM ONE DECK ON THE BUS TO THE OTHER, AND SITTING IN VARIOUS COMBINATIONS IN THE RED AND WHITE SEATS. THIS CONTEXT SUPPORTS THE DEVELOPMENT OF THE UNDERSTANDING THAT NUMBERS CAN BE NAMED IN MANY WAYS, FOR EXAMPLE 10 AS  $6 + 4$ ,  $7 + 3$ , OR  $5 + 5$ . THE UNIT ALSO INCLUDES MINILESSONS WITH QUICK IMAGES, AND STRINGS OF RELATED ADDITION AND SUBTRACTION PROBLEMS SOLVED WITH THE ARITHMETIC RACK TO HELP AUTOMATIZE THE BASIC FACTS. SEVERAL GAMES-PASSENGER PAIRS, RACK PAIRS, AND PASSENGER COMBOS-ARE ALSO INCLUDED IN THIS UNIT. THEY CAN BE PLAYED THROUGHOUT THE YEAR AS A WAY FOR CHILDREN TO EXTEND COMPOSING AND DECOMPOSING STRATEGIES AS THEY ESTABLISH EQUIVALENCE-FOR EXAMPLE, REPRESENTING 7 AS  $5 + 2$ ,  $3 + 4$ , OR  $1 + 6$  (TREFFERS, 1991). TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://www.contextsforlearning.com)

CONSTRUCTIVIST EDUCATION IN AN AGE OF ACCOUNTABILITY DAVID W. KRITT 2018-01-16 THIS BOOK CONTRASTS AUTHENTIC APPROACHES TO EDUCATION WITH CLASSROOM PRACTICES BASED PRIMARILY ON STANDARDS EXTERNAL TO THE INDIVIDUALS WHO ARE SUPPOSED TO LEARN. WHILE OTHER BOOKS TEND TO PROMOTE EITHER A DESPERATE SCRAMBLE FOR MEETING STANDARDS OR DETERMINED RESISTANCE TO NEOLIBERAL REFORMS, THIS BOOK FILLS THAT GAP IN WAYS THAT WILL INSPIRE PRACTITIONERS, PROSPECTIVE TEACHERS, AND TEACHER EDUCATORS. MANDATES PAY ONLY LIP SERVICE TO CONSTRUCTIVIST AND SOCIAL CONSTRUCTIVIST PRINCIPLES WHILE THWARTING THE VALUE OF BOTH STUDENTS AND TEACHERS ACTIVELY CREATING UNDERSTANDINGS. AUTHORS IN THIS BOOK ASSERT THE CENTRAL IMPORTANCE OF A RANGE OF CONSTRUCTIVIST APPROACHES TO TEACHING, LEARNING, AND THINKING, INVITING CAREFUL REFLECTION ON THE GOALS AND VALUES OF EDUCATION.

*MUFFLES' TRUFFLES* ANTONIA CAMERON 2008-03 MUFFLE'S TRUFFLES: MULTIPLICATION AND DIVISION WITH THE ARRAY IS ONE OF FIVE UNITS IN THE CONTEXTS FOR LEARNING MATHEMATICS' INVESTIGATING MULTIPLICATION AND DIVISION (3 - 5) THE FOCUS OF THIS UNIT IS THE DEVELOPMENT OF THE OPEN ARRAY AS A MODEL FOR MULTIPLICATION AND DIVISION. THIS UNIT USES A SERIES OF INVESTIGATIONS BASED ON THE CONTEXT OF MUFFLES' TRUFFLES SHOP. THE QUESTIONS POSED IN THE FIRST INVESTIGATION (HOW MANY BOXES OF TEN CAN BE MADE WITH A GIVEN QUANTITY OF TRUFFLES; HOW MANY LEFTOVERS WILL THERE BE FROM A GIVEN QUANTITY AND HOW CAN THEY BE COMBINED TO MAKE ASSORTMENT BOXES; AND WHAT IS THE COST OF A GIVEN QUANTITY OF TRUFFLES IF THEY COST \$1 EACH) GIVE STUDENTS AN OPPORTUNITY TO EXPLORE PLACE VALUE - THE MULTIPLICATIVE STRUCTURE OF OUR BASE-TEN SYSTEM AND QUOTATIVE DIVISION. IN THE SECOND AND THIRD INVESTIGATIONS, STUDENTS BUILD TWO-DIMENSIONAL BLUEPRINTS OF ONE-LAYER BOXES AND USE THESE ARRAYS TO EXPLORE SOME OF THE BIG IDEAS IN MULTIPLICATION (THE DISTRIBUTIVE, ASSOCIATIVE, AND COMMUTATIVE PROPERTIES). IN THE FOURTH AND FINAL INVESTIGATION, STUDENTS WORK WITH OPEN ARRAYS IN THE CONTEXT OF LABELING AND PRICING WRAPPED BOXES OF TRUFFLES. TO FIGURE OUT THE

DIMENSIONS OF THE WRAPPED BOXES (OR OPEN ARRAYS) AND THE COST, STUDENTS NEED TO APPLY A NUMBER OF BIG IDEAS PREVIOUSLY DEVELOPED IN THIS UNIT. THERE ARE THREE DIFFERENT KINDS OF MINILESSONS FOR MULTIPLICATION INCLUDED IN THE UNIT AS WELL: COUNTING AROUND THE CIRCLE, STRINGS OF RELATED PROBLEMS, AND QUICK IMAGES. THE COUNT-AROUND IS USED TO SUPPORT THE DEVELOPMENT OF PLACE VALUE AS IT RELATES TO MULTIPLICATION. THE STRINGS OF RELATED PROBLEMS ARE EXPLICITLY DESIGNED TO GUIDE LEARNERS TOWARD COMPUTATIONAL FLUENCY WITH WHOLE NUMBER MULTIPLICATION AND TO BUILD AUTOMATICITY WITH MULTIPLICATION FACTS BY FOCUSING ON RELATIONSHIPS. THE QUICK IMAGES USE  $2 \times 5$  AND  $1 \times 5$  ARRAYS AS UNITS TO BUILD LARGER ARRAYS. IN THE LAST DAYS OF THE UNIT, MORE COMPLEX MINILESSONS (DOUBLE-DIGIT MULTIPLICATION PROBLEMS) GENERATE A WIDER RANGE OF STUDENT STRATEGIES THAT CAN BE EXPLORED (AND MODELED) WITH THE OPEN ARRAY. TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://www.contextsforlearning.com)

**THE TEACHERS' LOUNGE** CATHERINE TWOMEY FOSNOT 2008-03 THE TEACHERS' LOUNGE: PLACE VALUE AND DIVISION IS ONE OF FIVE UNITS IN THE CONTEXTS FOR LEARNING MATHEMATICS' INVESTIGATING MULTIPLICATION AND DIVISION (3 - 5) THE FOCUS OF THIS UNIT IS DIVISION. IT BEGINS WITH THE STORY OF A TEACHER NOTICING A SERVICE PERSON IN THE TEACHERS' LOUNGE FILL TWO DIFFERENT VENDING MACHINES WITH BEVERAGES. IN THE FIRST MACHINE, THERE ARE BOTTLES OF WATER ONLY. THE MACHINE HOLDS 156 BOTTLES OF WATER WHEN FULL AND THE TEACHER WONDERS HOW MANY SIX-PACKS THAT MIGHT BE. THE SECOND PROBLEM INVOLVES THE JUICE MACHINE. IT ALSO HOLDS 156 BOTTLES WHEN FULL, BUT THE BOTTLES ARE PARTITIONED INTO SIX COLUMNS BECAUSE THERE ARE SIX DIFFERENT FLAVORS OF JUICE. THE TEACHER WONDERS HOW MANY THERE ARE OF EACH FLAVOR. ALTHOUGH MOST STUDENTS DO NOT REALIZE IT AT THE START, THE TWO PROBLEMS ARE RELATED. THE FIRST PROBLEM IS A QUOTATIVE DIVISION SITUATION - THE AMOUNT IN EACH GROUP IS KNOWN, THE NUMBER OF GROUPS IS NOT. THE SECOND PROBLEM IS A PARTITIVE DIVISION SITUATION - THE NUMBER OF GROUPS IS KNOWN, THE AMOUNT IN EACH GROUP IS NOT. THE PROBLEMS ARE JUXTAPOSED AND GIVEN TOGETHER TO ENCOURAGE STUDENTS TO EXAMINE THE RELATIONSHIP BETWEEN THE TWO KINDS OF DIVISION. THIS STORY CONTEXT OF THE TEACHERS' LOUNGE SETS THE STAGE FOR A SERIES OF INVESTIGATIONS DESIGNED TO SUPPORT THE DEVELOPMENT OF A REPERTOIRE OF STRATEGIES FOR MULTIPLICATION AND DIVISION, INCLUDING THE USE OF: \* THE TEN-TIMES STRATEGY \* PARTIAL PRODUCTS AND PARTIAL QUOTIENTS \* THE ASSOCIATIVE PROPERTY \* THE DISTRIBUTIVE PROPERTY OF MULTIPLICATION OVER ADDITION - THE BASIS FOR THE LONG DIVISION ALGORITHM SEVERAL MINILESSONS FOR MULTIPLICATION AND DIVISION ARE ALSO INCLUDED IN THE UNIT. THESE ARE STRUCTURED AS STRINGS OF RELATED PROBLEMS DESIGNED TO MORE EXPLICITLY GUIDE LEARNERS TOWARD COMPUTATIONAL FLUENCY. TOWARD THE END OF THE UNIT, DISCUSSION SHIFTS TO HOW THE CONTEXT OF A DIVISION PROBLEM INFLUENCES WHAT TO DO WITH THE REMAINDER. NOTE: THE CONTEXT FOR THIS UNIT ASSUMES THAT YOUR STUDENTS WILL HAVE HAD PRIOR EXPERIENCE USING ARRAYS FOR MULTIPLICATION. IF THIS IS NOT THE CASE, YOU MIGHT FIND IT HELPFUL TO USE THE UNIT MUFFLE'S TRUFFLES FIRST. TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://www.contextsforlearning.com)

**THE BIG DINNER** FOSNOT 2008-03 IN THE BIG DINNER THE PREPARATION OF A TURKEY DINNER INTRODUCES EARLY MULTIPLICATION STRATEGIES AND SUPPORTS AUTOMATIZING THE FACTS, USING THE RATIO TABLE, AND DEVELOPING THE DISTRIBUTIVE PROPERTY WITH LARGE NUMBERS. STRINGS OF PROBLEMS GUIDE LEARNERS TOWARD COMPUTATIONAL FLUENCY WITH WHOLE-NUMBER MULTIPLICATION AND BUILD AUTOMATICITY WITH MULTIPLICATION FACTS BY FOCUSING ON RELATIONSHIPS.

*LESSONS AND ACTIVITIES FOR BUILDING POWERFUL NUMERACY* PAMELA WEBER HARRIS 2014-06-24 BUILDING POWERFUL NUMERACY FOR MIDDLE AND HIGH SCHOOL STUDENTS BROUGHT THE WORLD OF RESEARCH ON NUMERACY AT THE ELEMENTARY LEVEL TO THE SECONDARY LEVEL, HELPING TEACHERS BUILD NUMERACY IN THEIR STUDENTS AND SHOWING HOW THAT WORK SUPPORTS STUDENTS IN UNDERSTANDING HIGHER MATH. NOW, PAM HARRIS CONTINUES HER WORK BY OFFERING LESSONS AND ACTIVITIES THAT PROMOTE HER STRATEGIES FOR TEACHING AS MUCH MATHEMATICS AS POSSIBLE WITH AS LITTLE MEMORIZATION AS POSSIBLE. TWO TYPES OF ACTIVITIES FOR BUILDING NUMERACY ARE INCLUDED IN THIS WORKBOOK: STUDENT WORKOUTS INCLUDE REPRODUCIBLE WORKSHEETS THAT STUDENTS CAN WORK ON INDEPENDENTLY OR IN PAIRS, FOLLOWED BY ROBUST CLASS DISCUSSION TO PROMOTE UNDERSTANDING OF THE IDEAS. TEACHER DIRECTED ACTIVITIES ARE WHOLE-CLASS MINI-LESSONS DESIGNED TO HELP STUDENTS CONSTRUCT NUMERICAL RELATIONSHIPS AS THEY WORK WITH THE TEACHER. WHILE THE STUDENT WORKOUTS PROVIDE STARTING POINTS FOR STUDENTS TO BUILD IMPORTANT NUMERICAL RELATIONSHIPS AND CHOOSE EFFECTIVE STRATEGIES, THE TEACHER DIRECTED ACTIVITIES PROVIDE OPPORTUNITIES FOR DISCUSSING, COMPARING, MODELING, VERBALIZING STRATEGIES, FINDING AND DESCRIBING PATTERNS, AND MAKING GENERALIZATIONS. TOGETHER THEY HELP DEVELOP THE MATHEMATICAL HABITS OF MIND THAT STUDENTS NEED FOR HIGHER MATH.

**INTENTIONAL TALK** ELHAM KAZEMI 2014 NOT ALL MATHEMATICS DISCUSSIONS ARE ALIKE. IT'S ONE THING TO ASK STUDENTS TO SHARE HOW THEY SOLVED A PROBLEM, TO GET IDEAS OUT ON THE TABLE SO THAT THEIR THINKING BECOMES VISIBLE; BUT KNOWING WHAT TO DO WITH STUDENTS' IDEAS--WHERE TO GO WITH THEM--CAN BE A DAUNTING TASK. INTENTIONAL TALK PROVIDES TEACHERS WITH A FRAMEWORK FOR PLANNING AND FACILITATING PURPOSEFUL MATHEMATICS DISCUSSIONS THAT ENRICH AND DEEPEN STUDENT LEARNING. ACCORDING TO ELHAM KAZEMI AND ALLISON HINTZ, THE CRITICAL FIRST STEP IS TO IDENTIFY A DISCUSSION'S

GOAL AND THEN UNDERSTAND HOW TO STRUCTURE AND FACILITATE THE CONVERSATION TO MEET THAT GOAL. THROUGH DETAILED VIGNETTES FROM BOTH PRIMARY AND UPPER ELEMENTARY CLASSROOMS, THE AUTHORS PROVIDE A WINDOW INTO WHAT TEACHERS ARE THINKING AS THEY LEAD DISCUSSIONS AND MAKE IMPORTANT PEDAGOGICAL AND MATHEMATICAL DECISIONS ALONG THE WAY. ADDITIONALLY, THE AUTHORS EXAMINE STUDENTS' ROLES AS BOTH LISTENERS AND TALKERS AND, IN THE PROCESS, OFFER A NUMBER OF STRATEGIES FOR IMPROVING STUDENT PARTICIPATION AND LEARNING. A COLLECTION OF PLANNING TEMPLATES INCLUDED IN THE APPENDIX HELPS TEACHERS APPLY THE RIGHT STRUCTURE TO DISCUSSIONS IN THEIR OWN CLASSROOMS. INTENTIONAL TALK PROVIDES THE PERFECT BRIDGE BETWEEN STUDENT ENGAGEMENT AND CONCEPTUAL UNDERSTANDING IN MATHEMATICAL DISCUSSIONS.

**The Box Factory** Fosnot 2008-03 The Box Factory: EXTENDING MULTIPLICATION WITH THE ARRAY IS ONE OF FIVE UNITS IN THE CONTEXTS FOR LEARNING MATHEMATICS' INVESTIGATING MULTIPLICATION AND DIVISION (3 - 5) THE FOCUS OF THIS UNIT IS THE DEEPENING AND EXTENDING OF STUDENTS' UNDERSTANDING OF MULTIPLICATION, SPECIFICALLY THE ASSOCIATIVE AND COMMUTATIVE PROPERTIES AND THEIR USE WITH COMPUTATION, SYSTEMATIC FACTORING, AND THE EXTENSION OF STUDENTS' UNDERSTANDING OF TWO-DIMENSIONAL RECTANGULAR ARRAYS TO THREE-DIMENSIONAL ARRAYS WITHIN RECTANGULAR PRISMS. THE UNIT INCLUDES A SERIES OF INVESTIGATIONS BASED ON THE CONTEXT OF A CARDBOARD BOX FACTORY. INITIALLY STUDENTS DESIGN A VARIETY OF BOXES (RECTANGULAR PRISMS) THAT HOLD 24 ITEMS ARRANGED IN ROWS, COLUMNS, AND LAYERS. THE QUESTIONS POSED IN THE FIRST INVESTIGATION (HOW MANY BOX ARRANGEMENTS ARE POSSIBLE, AND HOW DO WE KNOW FOR CERTAIN THAT WE HAVE FOUND ALL THE POSSIBILITIES) GIVE STUDENTS AN OPPORTUNITY TO EXPLORE THE ASSOCIATIVE AND COMMUTATIVE PROPERTIES, FACTOR PAIRS, DOUBLING AND HALVING STRATEGIES, AND SYSTEMATIC WAYS OF ORGANIZING THEIR WORK TO DETERMINE ALL POSSIBLE CASES. IN THE SECOND AND THIRD INVESTIGATIONS, STUDENTS ANALYZE THE AMOUNT AND COST OF THE CARDBOARD NEEDED FOR THEIR BOXES, DEEPENING THEIR UNDERSTANDING OF THE ASSOCIATIVE PROPERTY, EXAMINING CONGRUENCY VS. EQUIVALENCY, AND EXPLORING THE RELATIONSHIP OF SURFACE AREA TO THE SHAPE OF THE BOX. SUBSEQUENT INVESTIGATIONS INVOLVE USING TWO DIFFERENT CUBIC BOXES AS UNITS OF MEASUREMENT, AND DETERMINING THE VOLUME OF A SHIPPING BOX THAT MEASURES 4 FEET BY 6 FEET BY 4 FEET. BY THE END OF THE UNIT, FORMULAS FOR SURFACE AREA AND VOLUME OF RECTANGULAR PRISMS ARE THE FOCUS. SEVERAL MINILESSONS FOR MULTIPLICATION ARE INCLUDED IN THE UNIT AS WELL - THESE ARE STRUCTURES AS STRINGS OF RELATED PROBLEMS EXPLICITLY DESIGNED TO GUIDE LEARNERS TOWARD COMPUTATIONAL FLUENCY WITH WHOLE-NUMBER MULTIPLICATION, BY FOCUSING ON FACTORS AND EFFICIENT GROUPING. TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://www.contextsforlearning.com)

**FOSTERING CHILDREN'S MATHEMATICAL DEVELOPMENT, GRADES 3-5** CATHERINE TWOMEY FOSNOT 2005-07-26 DESIGNED FOR THE WORKSHOP PARTICIPANT OR PRESERVICE TEACHER, THIS CD-ROM ENABLES YOU TO WATCH AND INTERACT WITH VIDEO THAT DEPICTS CLASSROOM TEACHERS AS THEY LISTEN TO, QUESTION, AND INTERPRET STUDENTS' THINKING.

**UNPACKING FRACTIONS** MONICA NEAGOY 2017-03-10 FOR YEARS, THE TEACHING AND LEARNING OF FRACTIONS HAS BEEN ASSOCIATED WITH ROTE MEMORIZATION. BUT THIS MECHANICAL APPROACH TO INSTRUCTION—WHICH STRIPS STUDENTS OF AN ABILITY TO REASON OR MAKE SENSE OF MATH—HAS RESULTED IN A FAILURE OF UNDERSTANDING. AUTHOR MONICA NEAGOY, DRAWING ON DECADES OF RESEARCH STUDIES, EVIDENCE FROM TEACHER PRACTICE, AND 25 YEARS OF EXPERIENCE WORKING AROUND THE WORLD WITH TEACHERS, STUDENTS, AND PARENTS, ADDRESSES SEVEN BIG IDEAS IN THE TEACHING AND LEARNING OF FRACTIONS IN GRADES 2-6. EACH IDEA IS SUPPORTED BY A VIGNETTE FROM A REAL CLASSROOM, COMMON MISCONCEPTIONS, A THOROUGH UNPACKING OF PRODUCTIVE MATHEMATICAL THINKING, AND SEVERAL MULTISTEP AND THOUGHT-PROVOKING PROBLEMS FOR TEACHERS TO EXPLORE. SHE OFFERS THREE FUNDAMENTAL REASONS WHY IT'S IMPERATIVE FOR US TO TAKE A CLOSER LOOK AT HOW WE TEACH FRACTIONS: 1. FRACTIONS PLAY A KEY ROLE IN STUDENTS' FEELINGS ABOUT MATHEMATICS. 2. FRACTIONS ARE FUNDAMENTAL TO SCHOOL MATH AND DAILY LIFE. 3. FRACTIONS ARE FOUNDATIONAL TO SUCCESS IN ALGEBRA. WHILE A SOLID GROUNDING IN ALGEBRA IS NECESSARY FOR A STEM CAREER, THE WORTHY GOAL OF "ALGEBRA FOR ALL" WILL NOT BE POSSIBLE UNTIL "FRACTIONS FOR ALL" IS A REALITY. UNPACKING FRACTIONS PROVIDES TEACHERS WITH CONCRETE STRATEGIES FOR ACHIEVING THAT REALITY—IN SHORT, HELPING ALL STUDENTS GAIN THE KNOWLEDGE THEY NEED TO FEEL AT EASE WITH FRACTIONS.

**RHODA RED AND LORETTA LEGHORN** CATHERINE TWOMEY FOSNOT 2018-03-25 THIS KINDERGARTEN UNIT IN THE CONTEXTS FOR LEARNING MATHEMATICS SERIES INTRODUCES THE 5- AND 10-BEAD MATHRACKS(TM). THE UNIT BUILDS ON CHILDREN'S INNATE ABILITY TO SUBITIZE SMALL AMOUNTS (1, 2, AND 3) AND USES IT TO DEVELOP THE FIVE-STRUCTURE, EVENTUALLY SUPPORTING CHILDREN TO SEE 5 INSIDE OF 7, AND 5 INSIDE OF 8, FOR EXAMPLE. IN THE SECOND WEEK OF THE UNIT THE 10-STRUCTURE IS DEVELOPED, FIRST AS 5+5, AND THEN RELATIONSHIPS BETWEEN EQUIVALENT FACTS ARE EXPLORED AND DEVELOPED USING COMPENSATION AND ASSOCIATIVITY, FOR EXAMPLE, 3+7=4+6=5+5.

**NUMBER SENSE ROUTINES** JESSICA F. SHUMWAY 2011 JESSICA SHUMWAY HAS DEVELOPED A SERIES OF ROUTINES DESIGNED TO HELP YOUNG STUDENTS INTERNALIZE AND DEEPEN THEIR FACILITY WITH NUMBERS. THE DAILY USE OF THESE QUICK FIVE-, TEN-, OR

FIFTEEN-MINUTE EXPERIENCES AT THE BEGINNING OF MATH CLASS WILL HELP BUILD STUDENTS' NUMBER SENSE. --FROM PUBLISHER DESCRIPTION

**NUMBER TALKS** SHERRY PARRISH 2010-04-01 "THIS RESOURCE SUPPORTS NEW AND EXPERIENCED EDUCATORS WHO WANT TO PREPARE FOR AND DESIGN PURPOSEFUL NUMBER TALKS FOR THEIR STUDENTS; THE AUTHOR DEMONSTRATES HOW TO DEVELOP GRADE-LEVEL-SPECIFIC STRATEGIES FOR ADDITION, SUBTRACTION, MULTIPLICATION, AND DIVISION. INCLUDES CONNECTIONS TO NATIONAL STANDARDS, A DVD, REPRODUCIBLES, BIBLIOGRAPHY, AND INDEX"--PROVIDED BY PUBLISHER.

*FIELD TRIPS AND FUND-RAISERS* CATHERINE TWOMEY FOSNOT 2008-03 *FIELD TRIPS AND FUND-RAISERS: INTRODUCING FRACTIONS* IS ONE OF FIVE UNITS IN THE *CONTEXTS FOR LEARNING MATHEMATICS'* INVESTIGATING FRACTIONS, DECIMALS, AND PERCENTS (4 - 6) THE FOCUS OF THIS UNIT IS THE DEVELOPMENT OF FRACTIONS. IT BEGINS WITH THE STORY OF A CLASS FIELD TRIP. THE CLASS IS SPLIT INTO FOUR GROUPS AND EACH GROUP IS GIVEN SUBMARINE SANDWICHES TO SHARE FOR LUNCH. UPON RETURNING FROM THEIR TRIP, THE STUDENTS QUARREL OVER WHETHER SOME RECEIVED MORE TO EAT THAN OTHERS. NOTE: THIS UNIT BEGINS WITH THE FAIR SHARING OF SUBMARINE SANDWICHES ON A FIELD TRIP. THIS CONTEXT WAS FIELD-TESTED BY THE FREUDENTHAL INSTITUTE AND THE UNIVERSITY OF WISCONSIN, UNDER THE DIRECTION OF THOMAS ROMBERG AND JAN DE LANGE, IN PREPARATION FOR THE WRITING OF *MATHEMATICS IN CONTEXT: SOME OF THE PARTS* (VAN GALEN, WIJERS, BURRILL, AND SPENCE 1997) AND IT HAS BEEN RESEARCHED AND WRITTEN ABOUT EXTENSIVELY AS IT IS USED IN THIS UNIT BY FOSNOT AND DOLK (2002). THIS STORY SETS THE STAGE FOR A SERIES OF INVESTIGATIONS. FIRST, STUDENTS INVESTIGATE WHETHER THE SITUATION IN THE STORY WAS FAIR - WAS THE QUARRELING JUSTIFIED? - THEREBY EXPLORING THE CONNECTION BETWEEN DIVISION AND FRACTIONS, AS WELL AS WAYS TO COMPARE FRACTIONAL AMOUNTS. AS THE UNIT PROGRESSES, STUDENTS EXPLORE OTHER CASES TO DETERMINE FAIR SHARING AND THEN MAKE A RATIO TABLE TO ENSURE FAIR SHARING DURING THEIR FUTURE FIELD TRIPS. THEY ALSO DESIGN A 60k BIKE COURSE FOR A FUND-RAISER, A CONTEXT THAT INTRODUCES A BAR MODEL FOR FRACTIONS AND PROVIDES STUDENTS WITH ANOTHER OPPORTUNITY TO EXPLORE EQUIVALENT FRACTIONS. SEVERAL MINILESSONS FOR DIVISION OF WHOLE NUMBERS USING SIMPLIFIED EQUIVALENTS ARE ALSO INCLUDED IN THE UNIT. THESE ARE STRUCTURED USING STRINGS OF RELATED PROBLEMS AS A WAY TO MORE EXPLICITLY GUIDE LEARNERS TOWARD COMPUTATIONAL FLUENCY WITH WHOLE NUMBER DIVISION AND TO BUILD A CONNECTION TO EQUIVALENT FRACTIONS. NOTE: THE CONTEXT FOR THIS UNIT ASSUMES THAT YOUR STUDENTS HAVE HAD PRIOR EXPERIENCE WITH ARRAYS FOR MULTIPLICATION AND DIVISION, AS WELL AS PARTITIVE AND QUOTATIVE DIVISION WITH WHOLE NUMBERS. IF THIS IS NOT THE CASE, YOU MIGHT FIND IT HELPFUL TO FIRST USE *THE TEACHERS' LOUNGE AND MINILESSONS THROUGHOUT THE YEAR: MULTIPLICATION AND DIVISION* FROM *INVESTIGATIONS IN MULTIPLICATION AND DIVISION: GRADES 3 - 5*. TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://www.contextsforlearning.com)

**MINILESSONS FOR EXTENDING MULTIPLICATION AND DIVISION** CATHERINE TWOMEY FOSNOT 2008-03 *MINILESSONS FOR EXTENDING MULTIPLICATION AND DIVISION* IS ONE OF TWO YEARLONG RESOURCE GUIDES IN *CONTEXTS FOR LEARNING MATHEMATICS'* INVESTIGATING MULTIPLICATION AND DIVISION (3 - 5) *MINILESSONS FOR EXTENDING MULTIPLICATION AND DIVISION* CAN BE HELPFUL IN GRADES 4 - 5 AS STUDENTS WORK WITH MULTIPLICATION AND DIVISION BEYOND THE BASIC FACTS. THIS GUIDE CONTAINS 77 MINILESSONS STRUCTURED AS STRINGS OF RELATED COMPUTATION PROBLEMS. THEY ARE LIKELY TO GENERATE DISCUSSION OF CERTAIN STRATEGIES OR BIG IDEAS THAT ARE LANDMARKS ON THE LANDSCAPE OF LEARNING FOR MULTIPLICATION AND DIVISION, PARTICULARLY USING NUMBERS WITH TWO AND THREE DIGITS. ALTHOUGH THE EMPHASIS IS ON THE DEVELOPMENT OF MENTAL ARITHMETIC STRATEGIES, THIS DOES NOT MEAN LEARNERS HAVE TO SOLVE THE PROBLEMS IN THEIR HEADS - BUT IT IS IMPORTANT FOR THEM TO DO THE PROBLEMS WITH THEIR HEADS! IN OTHER WORDS, AS YOU USE THIS GUIDE, ENCOURAGE STUDENTS TO EXAMINE THE NUMBERS IN EACH PROBLEM AND THINK ABOUT CLEVER, EFFICIENT WAYS TO SOLVE IT. THE RELATIONSHIPS BETWEEN THE PROBLEMS IN THE MINILESSON WILL SUPPORT STUDENTS AS THEY PROGRESS THROUGH THE STRING. THE OPEN ARRAY IS USED THROUGHOUT TO REPRESENT STUDENT STRATEGIES. TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://www.contextsforlearning.com)

**CONTEXTS FOR LEARNING MATHEMATICS LEVEL 2 POSTERS** FOSNOT 2007-05-01 BUILDING LEARNING AROUND RICH, INSTRUCTIONALLY SOUND CONTEXTS WAS AN OVERARCHING GOAL DURING THE DEVELOPMENT OF THE *CONTEXTS FOR LEARNING MATHEMATICS* SERIES. THROUGHOUT THE SERIES CONTEXT IS USED TO SET THE STAGE FOR LEARNING. IT ESTABLISHES A TERRAIN THAT WILL INTRIGUE CHILDREN AND IGNITE THEIR IMAGINATIONS. THE CONTEXTS ARE SITUATIONS CHILDREN CAN IMAGINE - EITHER REALISTIC OR FICTIONAL - THAT ENABLE THEM TO REFLECT ON WHAT THEY ARE DOING AND APPLY MATHEMATICAL THINKING TO THEIR OWN WORLD. CONTEXTS FOR INVESTIGATIONS ARE TYPICALLY DEVELOPED WITH STORIES AND PICTURES. THESE ARE CAREFULLY CRAFTED TO INVOLVE STUDENTS IN MEANINGFUL INVESTIGATIONS OF THE BIG IDEAS, STRATEGIES, AND MODELS THAT SHAPE MATHEMATICAL THINKING. • THE IMAGES AND TEXTS ARE ENGAGING AND INCLUDE AGE-APPROPRIATE CHILDREN USING MATHEMATICS TO SOLVE REAL-WORLD PROBLEMS. • THE NUMBERS REFERENCED REPRESENT LANDMARK NUMBERS OR NUMBER RELATIONSHIPS THAT ARE SIGNIFICANT AND TELLING. • THE MODELS AND METAPHORS WITHIN A CONTEXT MAKE RELATIONSHIPS AND STRATEGIES MORE TANGIBLE AND EXPLICIT. THE CONTEXTS FOR THE FIVE UNITS IN *INVESTIGATING MULTIPLICATION AND DIVISION (GRADES 3 - 5)* ARE

ESTABLISHED THROUGH 17 VIBRANT POSTERS (15" x 24") THAT MELD HUMOR, INTRIGUE, AND GOOD MATH SENSE. TO LEARN MORE VISIT [WWW.CONTEXTSFORLEARNING.COM](http://WWW.CONTEXTSFORLEARNING.COM)

*CONTEXTS FOR LEARNING MATHEMATICS, LEVEL 1* CATHERINE TWOMEY FOSNOT 2006-03-15 CONTEXTS FOR LEARNING CONSISTS OF: INVESTIGATIONS AND RESOURCE GUIDES - WORKSHOP STRUCTURE INVOLVES STUDENTS IN INQUIRING, INVESTIGATING, DISCUSSING, AND CONSTRUCTING MATHEMATICAL SOLUTIONS AND STRATEGIES - INVESTIGATIONS ENCOURAGE EMERGENT LEARNING AND HIGHLIGHT THE DEVELOPMENTAL LANDMARKS IN MATHEMATICAL THINKING - STRINGS OF RELATED PROBLEMS DEVELOP STUDENTS' DEEP NUMBER SENSE AND EXPAND THEIR STRATEGIES FOR MENTAL ARITHMETIC READ-ALOUD BOOKS AND POSTERS - CREATE RICH, IMAGINABLE CONTEXTS--REALISTIC AND FICTIONAL--FOR MATHEMATICS INVESTIGATIONS - ARE CAREFULLY CRAFTED TO SUPPORT THE DEVELOPMENT OF THE BIG IDEAS, STRATEGIES, AND MODELS - ENCOURAGE CHILDREN TO EXPLORE AND GENERATE PATTERNS, GENERALIZE, AND DEVELOP THE ABILITY TO MATHEMATIZE THEIR WORLDS RESOURCES FOR CONTEXTS FOR LEARNING CD-ROM - AUTHOR VIDEOS DESCRIBE THE SERIES' PHILOSOPHY AND ORGANIZATION - VIDEO OVERVIEWS SHOW CLASSROOM FOOTAGE OF A MATH WORKSHOP, INCLUDING MINILESSONS, INVESTIGATIONS, AND A MATH CONGRESS - PRINT RESOURCES INCLUDE RESEARCH BASE, POSTERS, AND TEMPLATES

*PRINCIPLES TO ACTIONS* NATIONAL COUNCIL OF TEACHERS OF MATHEMATICS 2014-02 THIS TEXT OFFERS GUIDANCE TO TEACHERS, MATHEMATICS COACHES, ADMINISTRATORS, PARENTS, AND POLICYMAKERS. THIS BOOK: PROVIDES A RESEARCH-BASED DESCRIPTION OF EIGHT ESSENTIAL MATHEMATICS TEACHING PRACTICES ; DESCRIBES THE CONDITIONS, STRUCTURES, AND POLICIES THAT MUST SUPPORT THE TEACHING PRACTICES ; BUILDS ON NCTM'S PRINCIPLES AND STANDARDS FOR SCHOOL MATHEMATICS AND SUPPORTS IMPLEMENTATION OF THE COMMON CORE STATE STANDARDS FOR MATHEMATICS TO ATTAIN MUCH HIGHER LEVELS OF MATHEMATICS ACHIEVEMENT FOR ALL STUDENTS ; IDENTIFIES OBSTACLES, UNPRODUCTIVE AND PRODUCTIVE BELIEFS, AND KEY ACTIONS THAT MUST BE UNDERSTOOD, ACKNOWLEDGED, AND ADDRESSED BY ALL STAKEHOLDERS ; ENCOURAGES TEACHERS OF MATHEMATICS TO ENGAGE STUDENTS IN MATHEMATICAL THINKING, REASONING, AND SENSE MAKING TO SIGNIFICANTLY STRENGTHEN TEACHING AND LEARNING.

**BEADS AND SHOES, MAKING TWOS** MADELINE CHANG 2008-03 BEADS AND SHOES, MAKING TWOS: EXTENDING NUMBER SENSE IS ONE OF EIGHT UNITS IN THE CONTEXTS FOR LEARNING MATHEMATICS' INVESTIGATING NUMBER SENSE, ADDITION, AND SUBTRACTION (K - 3) THIS UNIT BEGINS WITH THE CONTEXT OF WALKING IN LINE - TWO LINES OF CHILDREN HOLDING HANDS. THE CONTEXT ENCOURAGES CHILDREN TO EXPLORE DOUBLES WHILE ALSO STRENGTHENING THEIR UNDERSTANDING OF ONE-TO-ONE CORRESPONDENCE. AS THE UNIT PROGRESSES, CHILDREN EXPLORE CONTAINERS THAT COULD HOLD DOUBLES (SUCH AS EGG CARTONS, ENGLISH MUFFIN PACKAGES, AND JUICE BOXES). THEN THE CONTEXT SHIFTS TO AN EXAMINATION OF PAIRS OF SHOES FOR VARYING NUMBERS OF PEOPLE. AS CHILDREN INVESTIGATE THESE SITUATIONS, THEY EXPLORE BOTH PAIRING AND DOUBLING - FOR INSTANCE, HOW SIX PAIRS OF SHOES CAN ALSO BE SEEN AS SIX RIGHT SHOES PLUS SIX LEFT SHOES (SIX SETS OF TWO OR TWO SETS OF SIX). LATER CHILDREN WORK WITH LARGER NUMBERS AND THE TERMINOLOGY OF ODDS AND EVENS IS INTRODUCED. IN THE SECOND WEEK, THE STORY GRANDMA'S NECKLACES IS USED TO DEVELOP A CONTEXT FOR SEVERAL INVESTIGATIONS RELATED TO PATTERNS MADE WITH TWO COLORS. THE FIRST NECKLACE (ONE BLUE/ONE GREEN REPEATING) CAN ONLY BE MADE WITH AN EVEN NUMBER OF OBJECTS, BECAUSE THE UNIT THAT REPEATS HAS TWO OBJECTS. THE SECOND NECKLACE (FIVE BLUE/FIVE GREEN REPEATING) AND THE THIRD NECKLACE (THREE BLUE/THREE GREEN REPEATING) CHALLENGE CHILDREN TO SEE A GROUP OF OBJECTS DOUBLED AS THE UNIT THAT REPEATS. MINILESSONS IN THE UNIT ARE CRAFTED TO SUPPORT THE AUTOMATIZING OF DOUBLES AND THEIR USE IN SOLVING NEAR DOUBLES - FOR EXAMPLE, USING  $6 + 6$  TO SOLVE  $6 + 7$ , OR  $10 + 10$  TO SOLVE  $9 + 10$ . QUICK IMAGES AND THE ARITHMETIC RACK ARE BOTH USED WITH STRINGS OF RELATED PROBLEMS. THE UNIT ALSO INCLUDES THE SHOE GAME. THIS GAME CAN BE PLAYED THROUGHOUT THE YEAR FOR FURTHER SUPPORT IN DEVELOPING THE USE OF DOUBLES AS AN ADDITION STRATEGY. TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://WWW.CONTEXTSFORLEARNING.COM)

*MATH IN THE CITY* ELISE CRAVER 2020-08-11 MATH IS EVERYWHERE - EVEN IN THE CITY! THE CITY IS A BUSY PLACE. IT'S FILLED WITH CARS, BUILDINGS, CROWDS, AND... MATH!

*CULTURALLY SPECIFIC PEDAGOGY IN THE MATHEMATICS CLASSROOM* JACQUELINE LEONARD 2008 CULTURE, COMMUNITY, AND MATHEMATICS ACHIEVEMENT -- COGNITION AND CULTURAL PEDAGOGY -- CULTURAL PEDAGOGY -- PROBLEM SOLVING, PROBLEM POSING, MULTI-CULTURAL LITERATURE AND COMPUTER SCAFFOLDING -- THE UNDERGROUND RAILROAD : A CONTEXT FOR LEARNING MATHEMATICS AND SOCIAL JUSTICE -- WOMEN IN AVIATION AND SPACE : THE IMPORTANCE OF GENDER ROLE MODELS IN MATHEMATICS EDUCATION -- LEARNING MATHEMATICS FOR EMPOWERMENT IN LINGUISTICALLY AND CULTURALLY DIVERSE CLASSROOMS -- RACE AND ACHIEVEMENT IN MATHEMATICS.

BEST BUYS, RATIOS, AND RATES BILL JACOB 2008-03 BEST BUYS, RATIOS, AND RATES: ADDITION AND SUBTRACTION OF

FRACTIONS IS ONE OF FIVE UNITS IN THE CONTEXTS FOR LEARNING MATHEMATICS' INVESTIGATING FRACTIONS, DECIMALS, AND PERCENTS (4 - 6) THE FOCUS OF THIS UNIT IS THE DEVELOPMENT OF EQUIVALENCE OF FRACTIONS, PROPORTIONAL REASONING, AND RATES. IT BEGINS WITH A COMPARISON OF THE COST OF CAT FOOD AT TWO STORES: BOB'S BEST BUYS WHERE IT IS ON SALE, \$15 FOR 12 CANS, AND MARIA'S PET EMPORIUM WHERE IT IS ON SALE, \$23 FOR 20 CANS. SEVERAL IMPORTANT IDEAS AND REPRESENTATIONS DEVELOP AS STUDENTS EXPLORE THIS PROBLEM, AMONG THEM FINDING WAYS TO DETERMINE THE COST OF A COMMON NUMBERS OF CANS FOR COMPARISON AND THE USE OF THE RATIO TABLE TO REPRESENT THEIR PROPORTIONAL REASONING ABOUT THE CONTEXT. THE DEVELOPMENT OF THE RATIO TABLE IS FURTHER SUPPORTED IN THE NEXT INVESTIGATION AS STUDENTS WORK TO DETERMINE THE COST OF SEVERAL DIFFERENT AMOUNTS OF BIRD SEED SOLD BY WEIGHT. AS THE UNIT PROGRESSES, PROPORTIONAL REASONING IS ONCE AGAIN THE FOCUS AS STUDENTS DEVELOP RECIPES FOR A VARIETY OF CONTAINERS, USING THE RECIPE OF MARIA'S GOURMET PUPPY SNACK MIX. IN THE SECOND WEEK THE DOUBLE NUMBER IS INTRODUCED FOR COMPUTATION AS STUDENTS INVESTIGATE THE READINGS ON A FARM TRUCK'S GAS TANK OVER THE COURSE OF TRIPS TO SEVERAL NEIGHBORING FARMS TO PICK UP PRODUCE. A TRIP ACROSS THE PENNSYLVANIA TURNPIKE IS ALSO EXPLORED. THIS UNIT ALSO INCLUDES SEVERAL MINILESSONS FOR ADDITION AND SUBTRACTION OF FRACTIONS. STRINGS OF RELATED PROBLEMS ARE USED INITIALLY USING MONEY AND CLOCK MODELS. DOUBLE NUMBER LINES ARE INTRODUCED LATER IN THE UNIT TO ENABLE STUDENTS TO DEVELOP GENERALIZABLE, STRATEGIES FOR ADDITION AND SUBTRACTION. THIS MODEL SUPPORTS STUDENTS TO CHOOSE A COMMON MULTIPLE (OR FACTOR) TO WORK WITH AS WELL AS FURTHER OPPORTUNITIES TO EXPLORE EQUIVALENT FRACTIONS. NOTE: THE CONTEXT FOR THIS UNIT ASSUMES THAT YOUR STUDENTS HAVE HAD PRIOR EXPERIENCE WITH FRACTIONS AND THEIR RELATIONSHIP TO DIVISION WITH WHOLE NUMBERS. IF THIS IS NOT THE CASE, YOU MIGHT FIND IT HELPFUL TO FIRST USE THE UNITS FIELD TRIPS AND FUND-RAISERS. TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://www.contextsforlearning.com)

THEORY AND PRACTICE: AN INTERFACE OR A GREAT DIVIDE? THE MATHEMATICS EDUCATION FOR THE FUTURE PROJECT – PROCEEDINGS OF THE 15TH INTERNATIONAL CONFERENCE ALAN ROGERSON THIS VOLUME CONTAINS THE PAPERS PRESENTED AT THE INTERNATIONAL CONFERENCE ON THEORY AND PRACTICE: AN INTERFACE OR A GREAT DIVIDE? AND HELD FROM AUGUST 4-9, 2019 AT MAYNOOTH UNIVERSITY, KILDARE, IRELAND. THE CONFERENCE WAS ORGANIZED BY THE MATHEMATICS EDUCATION FOR THE FUTURE PROJECT – AN INTERNATIONAL EDUCATIONAL PROJECT FOUNDED IN 1986 AND DEDICATED TO INNOVATION IN MATHEMATICS, STATISTICS, SCIENCE AND COMPUTER EDUCATION WORLD-WIDE. OUDER, FOUZE ABU; AMIT, MIRIAM: INCORPORATING ETHNOMATHEMATICAL RESEARCH IN CLASSROOM PRACTICE – THE CASE OF GEOMETRICAL SHAPES IN BEDOUIN TRADITIONAL EMBROIDERY. PP 1 – 4 ETHNOMATHEMATICS ASSERTS THAT IN ADDITION TO THE FORMAL MATHEMATICS TAUGHT IN SCHOOLS, THERE ARE OTHER FORMS OF MATHEMATICS, WHICH HAVE BEEN TAUGHT IN DIFFERENT SOCIETIES AND CULTURES AROUND THE WORLD. RESEARCH AND EDUCATIONAL EXPERIENCE HAS SHOWN THAT COMBINING ETHNOMATHEMATICS WITH THE FORMAL MATHEMATICS CURRICULUM IN THE CLASSROOM CAN IMPROVE STUDENTS' ACADEMIC ACHIEVEMENT, SINCE IT STRENGTHENS THEIR SELF-IMAGE AND REINFORCES THEIR MOTIVATION FOR STUDYING MATHEMATICS. WE ADOPTED THIS APPROACH WITH BEDOUIN STUDENTS WHO ARE DEFINED AS 'UNDERACHIEVERS' IN NATIONAL MATHEMATICS TESTS. IN THIS PAPER, WE OFFER AN ETHNOMATHEMATICAL ANALYSIS OF BEDOUIN EMBROIDERY SAMPLES TAKEN FROM TRADITIONAL DRESSES MADE BY BEDOUIN WOMEN. WE THEN DESCRIBE HOW ETHNOMATHEMATICAL ELEMENTS WERE INCORPORATED IN THE TEACHING OF MATHEMATICS FOR BEDOUIN STUDENTS, AND HOW DOING SO CONTRIBUTED TO THEIR LEARNING. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.01](https://doi.org/10.37626/GA9783959871129.0.01) ADAMS, NADINE; HAYES, CLINTON: PROVIDING SYNCHRONOUS MATHEMATICS INSTRUCTION TO DISTANCE STUDENTS- WORKSHOP. PP 5 – 8 IN THEORY TECHNOLOGY BREAKS DOWN BOUNDARIES AND ALLOWS US TO MORE EASILY CONNECT TO OUR STUDENTS. BUT IN PRACTICE DESPITE ALL OF THE TECHNOLOGY AVAILABLE MATHEMATICS INSTRUCTION IS STILL BEST GIVEN IN A "TALK AND CHALK" FORMAT. THE USE OF INSTRUCTIONAL VIDEOS, WHERE THE STUDENT IS ABLE TO WATCH HANDWRITTEN INSTRUCTION, HAS BECOME STANDARD. THESE ARE GREAT IN THAT THEY PROVIDE ASYNCHRONOUS INSTRUCTION AND ALLOW THE STUDENT TO LEARN AT A TIME THAT SUITS THEM. WHAT THESE VIDEOS LACK IS THE INTERACTIVE COMPONENT THAT MAKES FACE-TOFACE TEACHING PREFERABLE. TO OVERCOME THIS ONLINE LECTURES ARE CONDUCTED USING A COMBINATION OF ZOOM, PDF ANNOTATOR AND A TABLET PC. STUDENTS ARE PROVIDED WITH AN EXPERIENCE MUCH CLOSER TO THAT OF FACE-TO-FACE. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.02](https://doi.org/10.37626/GA9783959871129.0.02) ADENEGAN, KEHINDE EMMANUEL: MANAGING PUPILS WITH DYSGRAPHA IN EARLY CHILD NUMERACY. PP 9 – 13 DYSGRAPHA IS A SPECIFIC LEARNING DIFFICULTY WHICH IS A BRAIN-BASED DISORDER THAT IMPACTS ON WRITING SKILLS WHEREBY AFFECTED INDIVIDUALS HAVE DIFFICULTY WITH FORMING LETTERS, WRITING FIGURES, SPACING WORDS AND EVEN ORGANIZING TEXT INTO COMPLETE SENTENCES. EARLY CHILD NUMERACY IS A COMPETENCE BUILT IN THE YOUNG CHILD AT AN EARLY CHILDHOOD STAGE IN THE MATHEMATICAL SKILLS NEEDED TO COPE WITH EVERYDAY LIFE AND AN UNDERSTANDING OF INFORMATION PRESENTED MATHEMATICALLY. TO THIS END, THIS PAPER PRESENTS DYSGRAPHA, ITS SYMPTOMS IN PUPILS, OFFERS MEASURES ON HOW TO MANAGE DYSGRAPHA PUPILS BY TEACHERS AND PARENTS AND HIGHLIGHTS STRONG RECOMMENDATIONS TO ASSIST SUCH PUPILS IN PERFORMING AND COMPETING FAVOURABLY IN MATHEMATICS AND OTHER SUBJECTS WITH OTHER PUPILS IN THE CLASSROOM. KEYWORDS: DYSGRAPHA, EARLY CHILD NUMERACY (ECN), MATHEMATICS, PUPILS, NUMEROPHOBIA. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.03](https://doi.org/10.37626/GA9783959871129.0.03) ANHALT, CYNTHIA O.; CORTEZ, RICARDO: MATHEMATICAL MODELING THINKING: LAYING THE FOUNDATION FOR MATHEMATICAL MODELING COMPETENCY. PP 14 – 19

MATHEMATICAL MODELING COMPETENCY REQUIRES FREQUENT PRACTICE AND SUFFICIENT TIME TO DERIVE EXPERIENCE SOLVING OPEN-ENDED CONTEXTUAL PROBLEMS. SPECIFIC WAYS OF THINKING NECESSARY IN MODELING ARE IDENTIFIED BY CONTRASTING PLYA'S GENERAL PROBLEM-SOLVING FRAMEWORK, WHICH MAY BE FAMILIAR WORLDWIDE. THESE WAYS OF THINKING ARE DEVELOPED THROUGH MATHEMATICAL ACTIVITIES THAT PROMOTE DISPOSITIONS FOR EVENTUAL SUCCESS IN MODELING. WE POSIT THAT MATHEMATICAL MODELING THINKING (MMT) IS NECESSARY FOR BUILDING MODELING COMPETENCY. THIS PAPER DESCRIBES MMT AND ILLUSTRATES HOW IT CAN BE DEVELOPED THROUGH A WELL-KNOWN PROBLEM OF UNIVERSAL HUMAN CULTURAL GREETING EXCHANGE. WHILE CONNECTING TO WORLD CULTURES, WE EXAMINE WAYS TO PROMOTE MMT PRACTICES SUCH AS MAKING USEFUL SIMPLIFICATIONS, LOOKING FOR PATTERNS, UTILIZING MULTIPLE REPRESENTATIONS, MATHEMATIZING THE SITUATION, AND REFLECTING ON THE SOLUTION. WE CONCLUDE WITH PRACTICAL WAYS TO EFFECT MMT AS THE FOUNDATION FOR DEVELOPING MATHEMATICAL MODELING COMPETENCY. <https://doi.org/10.37626/GA9783959871129.0.04> ASHLEIGH, GLENDA JEAN: INDIVIDUAL DIFFERENCES IN COGNITION AND AFFECT IN MULTIPLICATIVE KNOWLEDGE IN BASIC MATHEMATICS PROBLEMS. PP 20 – 25 THIS PAPER DISCUSSES THE ROLES THAT INDIVIDUAL DIFFERENCES IN COGNITIVE AND AFFECTIVE VARIABLES PLAY IN THE FORMATION OF INCREASINGLY COMPLEX MULTIPLICATIVE KNOWLEDGE STRUCTURES IN BASIC MATHEMATICS PROBLEMS. THE EFFECTIVENESS OF LEARNER STRATEGIES AND TEACHING STRATEGIES TO OPTIMISE THE DEVELOPMENT OF AUTHENTIC MULTIPLICATIVE KNOWLEDGE WILL VARY ACCORDING TO THESE INDIVIDUAL DIFFERENCES. <https://doi.org/10.37626/GA9783959871129.0.05> BANACH, KATARZYNA: OK NOTEBOOK AS AN UNTYPICAL FORM OF STUDENT'S NOTEBOOK – OWN EXPERIENCE. PP 26 – 28 IN RECENT YEARS, THE METHODS OF WORK AT THE POLISH SCHOOL HAVE BEEN EVALUATED. FROM THE PRUSSIAN SCHOOL MODEL, WE ARE SLOWLY MOVING TO THE MODEL OF A MODERN SCHOOL MEETING CONTEMPORARY CHALLENGES. AT THE PRESENT TIME, MUCH ATTENTION IS DEVOTED TO THE SEARCH FOR NEW WORKING METHODS AND TEACHING TOOLS. WE DRAW ON THE EXPERIENCE OF OTHER COUNTRIES. WE TEST OUR OWN SOLUTIONS. THIS PAPER DEALS WITH THE USE OF FORMATIVE ASSESSMENT IN ASSOCIATION WITH THE UNTYPICAL FORMULA OF A STUDENT'S NOTEBOOK. <https://doi.org/10.37626/GA9783959871129.0.06> BATEIHA, SUMMER; MIR, SADIA: ENGAGING WITH MATHEMATICS THROUGH THREE TYPES OF STORYTELLING. PP 29 – 33 THROUGHOUT HISTORY, STORYTELLING HAS BEEN USED AS A WAY TO APPEAL TO PEOPLE'S IMAGINATION AND EMOTIONS. WHEN STORIES ARE TOLD IN THE MATHEMATICS CLASSROOM, THE SUBJECT COMES TO LIFE. STUDENTS BEGIN TO UNDERSTAND THE PURPOSE OF LEARNING THE CONTENT, AND MATHEMATICS BECOMES SOMETHING GREATER THAN A PLETHORA OF IRRELEVANT FACTS AND FORMULAS THAT ARE MEANT TO BE MEMORIZED, APPLIED, AND REPEATED. THIS WORKSHOP FOCUSES ON THE USE OF STORYTELLING AS A WAY TO ENGAGE STUDENTS IN A NONTRADITIONAL AND PERTINENT FORM OF LEARNING MATHEMATICS. IN THIS SESSION, PARTICIPANTS WILL LISTEN TO STORIES USED WITH PREDOMINANTLY ARAB STUDENTS IN AN AMERICAN UNIVERSITY IN QATAR AND PARTAKE IN DOING MATHEMATICAL TASKS RELATED TO THE STORIES PRESENTED. ALTHOUGH THE STORIES IN THIS WORKSHOP WERE APPLIED IN AN ARAB CONTEXT, THE IDEAS CAN BE EDITED FOR USE IN ANY CULTURAL CONTEXT. <https://doi.org/10.37626/GA9783959871129.0.07> BEDWELL, MIKE: FREEDOM OF SPEECH. PP 34 – 35 THIS PAPER RUES THE FACT THAT SUBMISSIONS TO SOME ACADEMIC JOURNALS ARE TREATED INCREASINGLY BADLY BY THE PUBLISHERS, WITH LITTLE SUCCOUR OFFERED BY THE EDITOR. THE WRITER GIVES AN EXAMPLE WHERE CHANGES IN TERMINOLOGY, SPELLING AND PUNCTUATION WERE INTRODUCED AFTER THE PAPER HAD BEEN ACCEPTED BY THE PEER APPRAISERS. THIS PAPER ALSO ARGUES FOR RIGID RULING ON THE GRAPHICAL PRESENTATION OF QUANTITATIVE DATA, SUCH AS THE DIMENSIONLESS LABELLING OF THE AXES IN CARTESIAN GRAPHS, AND THE DEFAULT RULE FOR ORDERING THE NOMINAL VARIABLES ON A BAR-CHART. <https://doi.org/10.37626/GA9783959871129.0.08> BENTLEY, BRIANNA: COLLEGE STUDENTS' VIEWS OF FRACTION ARITHMETIC. PP 36 – 41 COLLEGE STUDENTS VIEW MATHEMATICS, SPECIFICALLY FRACTION ARITHMETIC, AS A SERIES OF TRICKS THAT CAN LEAD THEM TO THE CORRECT ANSWER. THIS VIEW OF MATHEMATICS IS A DIRECT REFLECTION OF THEIR LACK OF CONCEPTUAL UNDERSTANDING OF FRACTION ARITHMETIC AND THEIR RELIANCE ON PROCEDURAL UNDERSTANDING. COLLEGE STUDENTS HAVE AN IMPRECISE REMEMBRANCE OF FRACTION ARITHMETIC AND INSTEAD RELY ON TRICKS THEY VAGUELY REMEMBER AND CANNOT EXPLAIN. THIS RELIANCE ON PROCEDURAL PROCESSES THAT THEY DO NOT FULLY UNDERSTAND CAUSES THEM TO MAKE MISTAKES IN THEIR ARITHMETIC. IF WE DO NOT REQUIRE STUDENTS TO THINK CRITICALLY ABOUT THE MATHEMATICAL PROCESSES THEY ARE COMPLETING WHEN FIRST TAUGHT A SUBJECT AND REQUIRE THIS CRITICAL THOUGHT AS STUDENTS PROGRESS THROUGH MATHEMATICS COURSES, MATHEMATICS LOSES MEANING AND OUR STUDENTS WILL NOT HAVE THE ABILITY TO THINK CRITICALLY OR CONCEPTUALLY ABOUT MATHEMATICS. <https://doi.org/10.37626/GA9783959871129.0.09> BETTS, PAUL; ET AL: FOUNDATIONAL EXPERIENCES AS A DESIGN PRINCIPLE FOR MATHEMATICS CURRICULUM FOR CHILDREN. PP 42 – 47 STUDENTS MUST MAKE SENSE OF THE MATHEMATICS THEY ARE LEARNING, IF THEY ARE TO UNDERSTAND IT. WHEN STUDENTS ARE ENCOUNTERING A MATHEMATICS TOPIC PRIMARILY THROUGH THAT TOPIC'S MATHEMATICAL FORMS—ITS SYMBOLS, TERMINOLOGY, DEFINITIONS, OPERATIONS, AND ALGORITHMS—THE RICHNESS, POTENCY, AND COMPLETENESS OF THEIR UNDERSTANDING WILL DEPEND ON THEIR PRIOR, PRE-FORMAL EXPERIENCES WITH THAT TOPIC. FOUNDATIONAL EXPERIENCES ACTIVITIES ENABLE STUDENTS TO CONSTRUCT IMAGES, PATTERNS, AND IDEAS—IN A WORD, MEMORIES—THAT WILL ENABLE THEM TO SEE THE SENSIBILITY OF THE TOPIC'S MATHEMATICAL FORMS WHEN THEY LEARN THEM. WE INVITE PARTICIPANTS TO EXPLORE SOME EXAMPLES OF INSTRUCTIONAL ACTIVITIES DESIGNED TO PROVIDE FOUNDATIONAL EXPERIENCES FOR MULTIPLICATION. WHAT ARE THE QUALITIES THAT WE SHOULD INVEST IN FOUNDATIONAL EXPERIENCE ACTIVITIES? HOW CAN SUCH ACTIVITIES BE POSITIONED WITHIN CURRICULUM DESIGN, WITH THE GOAL OF INCREASING THE QUALITY OF STUDENTS' UNDERSTANDINGS OF MATHEMATICS TOPICS, IN PURSUIT OF SUCCESS FOR ALL

PARTICIPANTS IN SCHOOL MATH? [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.10](https://doi.org/10.37626/GA9783959871129.0.10) BILLINGS, ESTHER; KASMER, LISA: LEARNING VIA TEACHING: EXAMPLES OF MEDIATED FIELD EXPERIENCES IN EARLY COURSEWORK OF PRE-SERVICE TEACHERS. PP 48 – 53 TWENTY YEARS AGO, BALL AND COHEN (1999) DESCRIBED A VISION FOR PRACTICEBASED PROFESSIONAL EDUCATION IN WHICH TEACHERS' LEARNING IS SITUATED WITHIN PRACTICE. WE HAVE PURPOSEFULLY DESIGNED PRACTICE-BASED EDUCATIONAL EXPERIENCES EARLY IN TEACHER PREPARATION COURSEWORK AROUND McDONALD ET AL.'S (2013) LEARNING CYCLE TO INCLUDE MEDIATED FIELD EXPERIENCES. SUCH EXPERIENCES ARE STRUCTURED TO EXPLICITLY CONNECT COURSEWORK AND FIELDWORK AND ARE ORGANIZED AROUND CORE PRACTICES; PRESERVICE TEACHERS (PSTs) DEEPEN THEIR LEARNING OF MATHEMATICS AND WAYS TO TEACH MATHEMATICS BY DOING THE WORK OF TEACHERS WITHIN AUTHENTIC K-12 CLASSROOM SETTINGS. IN THIS PAPER WE DESCRIBE EXAMPLES OF MEDIATED FIELD EXPERIENCES STRUCTURED ON McDONALD ET AL.'S (2013) LEARNING CYCLE THAT OCCUR EARLY IN PSTs' COURSEWORK, PRIOR TO STUDENT TEACHING. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.11](https://doi.org/10.37626/GA9783959871129.0.11)

BRAHIER, DANIEL J.: RESEARCH INTO PRACTICE: 29 YEARS OF CLASSROOM TEACHING. PP 54 – 59 THE PREPARATION AND PROFESSIONAL DEVELOPMENT OF MATHEMATICS TEACHERS REQUIRES INSTRUCTORS WHO ARE NOT ONLY PROFICIENT IN THEIR CONTENT AND PEDAGOGY BUT CAN BRING SUCCESSFUL TEACHING EXPERIENCES TO THE CLASSROOM. IN THIS PAPER, THE AUTHOR SHARES HIS EXPERIENCE OF 29 YEARS OF SIMULTANEOUSLY TEACHING IN A K-12 SECONDARY SCHOOL, WHILE ALSO SERVING AS A UNIVERSITY PROFESSOR WHO TEACHES MATHEMATICS METHODS COURSES. EXAMPLES OF CLASSROOM EXPERIENCES THAT ENHANCED UNIVERSITY METHODS COURSES ARE DESCRIBED, AS ARE SOME OF THE BENEFITS OF TEACHING IN BOTH SETTINGS TO CONNECT RESEARCH AND PRACTICE IN MATHEMATICS TEACHING. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.12](https://doi.org/10.37626/GA9783959871129.0.12)

BROWNING, SANDRA: ELEMENTARY PRESERVICE TEACHERS AND QUESTIONING STRATEGIES IN MATHEMATICS. PP 60 – 65 RESEARCH HAS DEMONSTRATED AN INTEREST IN THE RELATIONSHIP BETWEEN TEACHERS' QUESTIONING STRATEGIES AND CHILDREN'S ABILITY TO REASON AND LEARN (BAROODY & GINSBURG, 1990; BUSCHMAN, 2001; FENNEMA, FRANKE, CARPENTER & CAREY, 1993). HELPING PRESERVICE TEACHERS DEVELOP EFFECTIVE QUESTIONING STRATEGIES IS AN IMPORTANT COMPONENT OF A TEACHER EDUCATION PROGRAM. THIS SESSION DESCRIBES AN EXPLORATION DESIGNED TO DETERMINE IF EC-6 PRESERVICE TEACHERS CAN (A) RECOGNIZE EFFECTIVE QUESTIONING STRATEGIES WHEN OBSERVING INSERVICE TEACHERS AND (B) USE HESS'S COGNITIVE RIGOR MATRIX TO ANALYZE THE LEVEL AND EFFECTIVENESS OF THEIR OWN QUESTIONING STRATEGIES DURING FIELD EXPERIENCES. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.13](https://doi.org/10.37626/GA9783959871129.0.13)

BURRILL, GAIL: STATISTICAL LITERACY AND QUANTITATIVE REASONING. PP 66 – 71 GIVEN A WORLD AWASH WITH DATA, STUDENTS OF TODAY WILL BE CONSUMERS OF STATISTICAL INFORMATION WHATEVER THEIR FUTURE. WHAT CAN WE DO TO MAKE THEM CRITICAL CONSUMERS AS ARTICULATED BY RESEARCHERS SUCH AS GAL AND STEEN AND AS SUGGESTED IN THE NATIONAL COUNCIL OF TEACHERS OF MATHEMATICS CATALYZING CHANGE, ABLE TO PROCESS INFORMATION, ASK THE RIGHT QUESTIONS AND MAKE INFORMED DECISIONS? THIS PAPER EXPLORES WHAT IT MEANS TO BE STATISTICALLY LITERATE ABLE TO REASON WITH QUANTITATIVE INFORMATION IN TODAY'S WORLD AND WHY IT IS IMPORTANT FROM BOTH A PERSONAL AND PROFESSIONAL PERSPECTIVE. EXAMPLES FROM SEVERAL FIELDS ILLUSTRATE FEATURES OF ESSENTIAL CORE CONCEPTS THAT SHOULD BE COMPONENTS OF THE CURRICULUM FOR ALL STUDENTS IF WE ARE TO HAVE STATISTICALLY LITERATE CITIZENS CAPABLE OF THINKING AND REASONING IN QUANTITATIVE SITUATIONS. THE DISCUSSION WILL ALSO ADDRESS SOME OF THE CHALLENGES WE FACE IN MAKING THIS RECOMMENDATION A REALITY. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.14](https://doi.org/10.37626/GA9783959871129.0.14)

CAMETTI, CRISTINA; ET AL: ADVANTAGES, CHALLENGES AND OPPORTUNITIES IN TEACHING STATISTICS IN DOCTORAL TRAINING TO A HETEROGENEOUS GROUP: THE CASE OF FLAMES SUMMER SCHOOL. PP 72 – 77 FLAMES IS AN INTER-UNIVERSITY DOCTORAL TRAINING NETWORK IN WHICH ALL FLEMISH UNIVERSITIES OF BELGIUM COLLABORATE. IT AIMS TO SUPPORT YOUNG RESEARCHERS, IN NEED OF METHODOLOGICAL AND STATISTICAL INSIGHTS AND SKILLS, BY OFFERING THEM HIGH QUALITY TRAINING AT BASIC, INTERMEDIATE AND ADVANCED LEVELS. ONE OF OUR MOST SUCCESSFUL ACTIVITIES IS A YEARLY TWO-WEEK SUMMER SCHOOL WHICH FEATURES A RANGE OF MODULES ON RESEARCH DESIGN, STATISTICAL METHODOLOGY AND DATA ANALYSIS. EACH MODULE CONNECTS THEORY WITH HANDS-ON EXERCISES, FOCUSING ON VARIOUS DISCIPLINES AND USING DIFFERENT SOFTWARE PACKAGES. IN THIS PAPER, WE DISCUSS THE FLAMES APPROACH IN TEACHING STATISTICS TO A HETEROGENEOUS GROUP OF YOUNG RESEARCHERS FROM VARIOUS DISCIPLINES WITH A DIFFERENT BACKGROUND IN STATISTICS AND METHODOLOGY. FLAMES' 'MEASURING IS KNOWING' PRINCIPLE IS USED TO EVALUATE THE CONTENT, APPLICABILITY AND EDUCATIONAL ASPECTS OF THE CURRENT MODULES AND TO RECEIVE SUGGESTIONS FOR FUTURE TOPICS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.15](https://doi.org/10.37626/GA9783959871129.0.15)

CASTRO MIGUEZ, LUIS ALEXANDER; ET AL: DIAGRAMMATIC REASONING FROM REFLECTIONS ON PEIRCEAN SEMIOTICS. PP 78 – 83 THE DOCUMENT ILLUSTRATES SOME ELEMENTS OF REFLECTION ON PEIRCE'S SEMIOTICS FOCUSED ON REASONING THROUGH DIAGRAMS. THE SOLUTION OF A EUCLIDEAN GEOMETRY PROBLEM IS TAKEN AS A REFERENCE IN WHICH MATHEMATICAL DIAGRAMS ARE RECOGNIZED AS EPISTEMOLOGICAL TOOLS IN THE LEARNING AND TEACHING OF GEOMETRY. THIS IS HOW AN INTERPRETER, WHO SYSTEMATICALLY OBSERVES AND EXPERIMENTS WITH A GEOMETRIC DIAGRAM, GENERATES DIFFERENT INTERPRETANTS BY MEANS OF ABDUCTIVE, INDUCTIVE AND DEDUCTIVE REASONING. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.16](https://doi.org/10.37626/GA9783959871129.0.16)

CHAPMAN, OLIVE; BABB, PAULINO PRECIADO: PROSPECTIVE SECONDARY MATHEMATICS TEACHERS' DEVELOPMENT OF KNOWLEDGE OF MODELLING FOR TEACHING. PP 84 – 89 GIVEN THE GROWING ATTENTION ON MODELLING IN SCHOOL MATHEMATICS CURRICULUM, PROSPECTIVE TEACHERS ARE LIKELY TO NEED SPECIAL HELP TO DEVELOP A RICH SENSE OF MATHEMATICAL MODELLING [MM] AND EFFECTIVE CLASSROOM PRACTICES TO SUPPORT

STUDENTS' DEVELOPMENT OF MM COMPETENCIES. THIS PAPER IS BASED ON A STUDY INVOLVING THE USE OF INQUIRY-BASED ACTIVITIES TO ENGAGE PROSPECTIVE SECONDARY MATHEMATICS TEACHERS [PTS] IN DEVELOPING SUCH KNOWLEDGE OF MM FOR TEACHING. PARTICIPANTS WERE STUDENTS IN A MATHEMATICS EDUCATION COURSE. DATA SOURCES INCLUDED COURSE WORK AND FIELD NOTES. WE REPORT FINDINGS RELATED TO THE INQUIRYBASED ACTIVITIES AND THE LEARNING THEY AFFORDED IN THE PARTICIPANTS' UNDERSTANDING OF SPECIFIC COMPONENTS OF PROBLEM-SOLVING [PS] AND MM KNOWLEDGE FOR TEACHING AND THE RELATIONSHIP BETWEEN THEM. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.17](https://doi.org/10.37626/GA9783959871129.0.17) CHIN, KIN ENG; JIEW, FUI FONG: MISCONCEPTIONS OR PRECONCEPTIONS IN MAKING SENSE OF DECIMALS. PP 90 – 95 THIS PAPER AIMS TO EXPLORE THE ROOT CAUSES OF STUDENTS' MISCONCEPTIONS IN DECIMALS. A SET OF DECIMAL TASKS AND FOLLOW-UP INTERVIEWS WERE USED TO GATHER THE RELEVANT DATA. EIGHT YEAR SIX PRIMARY SCHOOL STUDENTS PARTICIPATED IN THIS STUDY ON A VOLUNTARY BASIS. IN THIS PAPER, DATA COLLECTED FROM TWO STUDENTS WERE REPORTED BECAUSE THEY SHOWED QUALITATIVELY DISTINCT RESPONSES AND COULD COVER THE SPECTRUM OF RESPONSES OF THIS GROUP OF PARTICIPANTS. FINDINGS REVEALED THAT STUDENTS' MISCONCEPTIONS MAYBE REGARDED AS PRECONCEPTIONS THAT WERE DEVELOPED FROM WORK EXPERIENCES IN OTHER CONTEXTS SUCH AS INTEGERS. THIS SHOWS THAT THE LEARNING EXPERIENCES FROM OTHER CONTEXTS MAY IMPEDE FUTURE LEARNING OF STUDENTS IN NEW CONTEXTS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.18](https://doi.org/10.37626/GA9783959871129.0.18) CIVIL, MARTA; HUNTER, ROBERTA: SUPPORTING MATHEMATICS TEACHERS TO BUILD DEEP UNDERSTANDINGS OF THE HOME CONTEXTS OF THEIR STUDENTS. PP 96 – 99 TEACHERS FACE MANY CHALLENGES IN MEETING THE CULTURAL DIVERSITY THEY ENCOUNTER IN CURRENT MATHEMATICS CLASSROOMS. TO AVOID MARGINALISATION OF SPECIFIC GROUPS OF STUDENTS WE ADVOCATE FOR A STRENGTH-BASED APPROACH IN WHICH TEACHERS ARE SUPPORTED TO BUILD DEEP UNDERSTANDINGS OF THE LIVED HOME CONTEXT OF THEIR STUDENTS. WE DISCUSS FINDINGS FROM OUR RESEARCH PROJECTS WITH IMMIGRANT STUDENTS (PŪ SIFIKA) IN NEW ZEALAND AND WITH MEXICAN AMERICAN STUDENTS IN THE UNITED STATES. WHILE OUR CONTEXTS ARE QUITE DIFFERENT, OUR APPROACHES HAVE MUCH IN COMMON, IN PARTICULAR THROUGH THEIR FOCUS ON TEACHERS LEARNING FROM AND ABOUT THEIR STUDENTS' COMMUNITIES TO THEN BUILD ON THIS LEARNING IN THEIR MATHEMATICS TEACHING. BRIDGING THEORY AND PRACTICE, WE SHARE SPECIFIC STRATEGIES THAT WE HAVE USED TO SUPPORT TEACHERS AS LEARNERS OF THEIR STUDENTS' HOME CONTEXTS (E.G., HOME VISITS; PARENTS' CLASSROOM VISITS; SCHOOL MEETINGS LED BY PARENTS). [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.19](https://doi.org/10.37626/GA9783959871129.0.19) CLEMMER, KATHARINE; ET AL: COLLABORATIVE SOLUTION DISCOVERY: A PROBLEM SOLVING PROCESS. PP 100 – 103 LOYOLA MARYMOUNT UNIVERSITY (LMU) HAS DEVELOPED A NEW APPROACH TO PROBLEM SOLVING, COLLABORATIVE SOLUTION DISCOVERY (CSD), TO HELP PRACTITIONERS IN A SCHOOL SYSTEM LEVERAGE THEIR INDIVIDUAL PASSIONS IN A WAY THAT GROWS STUDENTS' POSITIVE MATH IDENTITY THROUGH MATHEMATICAL THINKING, PROBLEM SOLVING, AND SELF-REGULATION. BY FOCUSING ON HOW STUDENTS AND TEACHERS INTERACT WITH EACH OTHER IN REAL-TIME IN AN IDEAL CLASSROOM, PRACTITIONERS TAKE OWNERSHIP OF A PROCESS TO GUIDE THEIR STUDENTS IN GROWING THEIR POSITIVE MATH IDENTITY AND THUS TAKING OWNERSHIP OF THEIR OWN MATH LEARNING. PRACTITIONERS MEASURE PROGRESS ALONG THE WAY THROUGH METRICS THAT ARE CREATED, DEFINED, USED, AND CONTINUALLY REFINED BY THEMSELVES TO ATTAIN THEIR IDEAL MATH LEARNING ENVIRONMENT. THE ENTIRE CSD PROCESS RESULTS IN A SYSTEM THAT OWNS IST IMPROVEMENT EFFORTS—IMPROVEMENT EFFORTS THAT ARE FLEXIBLE, ADAPTABLE, AND SUSTAINABLE. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.20](https://doi.org/10.37626/GA9783959871129.0.20) COGGINS, PORTER; ET AL: THE MATHEMATICAL CULTURE OF OJIBWE STUDENTS – AN ETHNOGRAPHIC STUDY. PP 104 – 109 HUMAN BEINGS HAVE AN INNATE CAPACITY TO COMMUNICATE, COUNT, DETECT PATTERNS, LOCATE, AND CREATE. WITH THESE CAPACITIES WE INVENT, DESIGN, PLAY, AND EXPLAIN. REGARDLESS OF ACADEMIC BACKGROUND, WE ALSO HAVE THE INNATE CAPACITY TO USE MATHEMATICS IN MEANINGFUL WAYS. HOWEVER, IN SPITE OF THIS INNATE CAPACITY, THERE IS A LARGE DISCONNECT BETWEEN INNATE FUNCTION AND SUCCESS IN ACADEMIC MATHEMATICS. OUR RESEARCH IS BASED ON INTERVIEWS OF 14 OJIBWE-IDENTIFYING TRIBAL COLLEGE STUDENTS. THE INSTRUMENT WAS CONSTRUCTED BASED ON BISHOP'S (1988) SET OF SIX UNIVERSALS OR ACTIVITIES PEOPLE HAVE ALWAYS DONE. WE PRESENT THE DEVELOPMENT OF THE INSTRUMENT, INTERVIEW PROCESS, AND INITIAL FINDINGS. FINDINGS INCLUDE COMMON ETHNOMATHEMATICAL THREADS FOUND AMONG THE INTERVIEWED STUDENTS. OUR GOAL IS TO USE THIS RESEARCH TO IMPROVE OURPREK-12 PROFESSIONAL EDUCATION TEACHER PROGRAM AND POSITIVELY IMPACT OJIBWE STUDENT LEARNING. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.21](https://doi.org/10.37626/GA9783959871129.0.21) COLLINS, KEN: USING CAS TO IMPROVE STUDENT UNDERSTANDING OF CALCULUS CONCEPTS. PP 110 – 114 THIS SESSION WILL EXPLORE TWO AREAS OF APPLICATION OF CAS: ONE FOCUSING ON HOW TEACHERS CAN IMPROVE STUDENT LEARNING USING CAS, THE OTHER FOCUSING ON HOW STUDENTS CAN USE CAS DIRECTLY TO HELP THEM IMPROVE THEIR UNDERSTANDING OF CALCULUS CONCEPTS. WE WILL ILLUSTRATE THE FIRST AREA BY SHARING SOME EXAMPLES OF CALCULUS TEACHING LESSONS THAT USE CAS TO HELP STUDENTS UNDERSTAND OR APPLY A PARTICULAR CONCEPT. WE WILL ILLUSTRATE THE SECOND AREA BY SHARING SOME EXAMPLES OF STUDENT EXPLORATIONS THAT UTILIZE CAS. THESE ALLOW STUDENTS TO EXPLORE SOME RELATIONSHIPS AND APPLICATIONS WE USE IN CALCULUS THAT WOULD BE DIFFICULT TO DO OTHERWISE. FOR EXAMPLE, THE MEAN VALUE THEOREM (MVT) IS ONE OF THE MOST IMPORTANT THEOREMS IN CALCULUS. MANY FIRST YEAR CALCULUS STUDENTS HAVE DIFFICULTIES REALLY UNDERSTANDING OR APPLYING THE MVT. USING CAS, A STUDENT CAN EXPLORE HOW TO APPLY THE MVT TO A DIFFERENTIABLE FUNCTION AND DEVELOP A BETTER UNDERSTANDING OF THE MVT AND ITS GRAPHICAL INTERPRETATION. THIS SESSION WILL FOCUS ON FIRST YEAR CALCULUS TOPICS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.22](https://doi.org/10.37626/GA9783959871129.0.22) CURRY, MARJORIE: CULTURALLY RESPONSIVE MATH. PP 115 –

117 USING THE READY FOR RIGOR FRAMEWORK, ZARETTA HAMMOND'S BOOK CULTURALLY RESPONSIVE TEACHING AND THE BRAIN: PROMOTING AUTHENTIC ENGAGEMENT AND RIGOR AMONG CULTURALLY AND LINGUISTICALLY DIVERSE STUDENTS GIVES EDUCATORS A NEUROSCIENCE-BASED APPROACH TO CLOSING THE ACHIEVEMENT GAP. THE READY FOR RIGOR FRAMEWORK CONSISTS OF FOUR STRANDS: AWARENESS, LEARNING PARTNERSHIPS, INFORMATION PROCESSING, AND COMMUNITY BUILDING. ACKNOWLEDGING THAT ALL FOUR STRANDS ARE PARAMOUNT TO CULTURALLY RESPONSIVE TEACHING BUT RESTRICTING FOCUS TO INFORMATION PROCESSING, THIS SESSION WILL GIVE PARTICIPANTS EXAMPLES OF AND STRATEGIES FOR MAKING THEIR MATHEMATICS LESSONS MORE CULTURALLY RESPONSIVE. MORE SPECIFICALLY, PARTICIPANTS WILL LEARN TO GAME-IFY IT, STORY-IFY IT, AND MAKE IT SOCIAL. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.23](https://doi.org/10.37626/GA9783959871129.0.23) CZARNOCHA, BRONISLAW: CONSTRUCTIVIST TEACHING EXPERIMENT: CONSTRUCTIVIST RESEARCH AND CONSTRUCTIVIST TEACHING. PP 118 – 123 THE AIM OF THE DISCUSSION IS TWOFOLD: FIRST, WE FORMULATE AND PRESENT EXAMPLES OF THE CREATIVE BISOCIATIVITY INHERENT IN TEACHING-RESEARCH TR/NY CITY MODEL (SECTION 1). SECOND, WE BRING THE CREATIVE MODEL OF TEACHING-RESEARCH AS THE PRECISE SOLUTION TO THE DIFFICULTIES EXPERIENCED BY COMMON CURRICULUM STANDARDS IN MATHEMATICS (CCSM). SECTION 2 ANALYZES THE REASON FOR EXTRAORDINARY DIFFICULTIES IN SUCCESSFUL INTRODUCTION OF THE CURRICULUM INTO PRACTICE, WHICH MANIFEST THEMSELVES AMONG OTHERS, BY THE NECESSITY OF SCRIPTED LESSONS TELLING TEACHERS EXACTLY WHAT TO DO IN ALL DIFFERENT MOMENTS OF THE LESSON TIME. THE ROOT REASON FOR THE CONTEMPORARY DIFFICULTIES IS THE ABSENCE OF TEACHERS INVOLVEMENT IN THE DESIGN PROCESS IT IS IN CONTRADICTION WITH THE IRREDUCIBLE PRESENCE OF TEACHING WITHIN THE CENTRAL CONSTRUCTIVIST INSTRUMENT OF RESEARCH- CONSTRUCTIVIST TEACHING EXPERIMENT OF COBB AND STEFFE (1983). [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.24](https://doi.org/10.37626/GA9783959871129.0.24) DAS, MILI: CURRICULUM FOR MATHEMATICS EDUCATION – AN APPROACH TO DISCUSS RELATION BETWEEN THEORY AND PRACTICE. PP 124 – 129 A NEW CURRICULUM HAS BEEN INTRODUCED IN TEACHERS' TRAINING COURSE AS THE COURSE IS SHIFTED FROM ONE YEAR TO TWO-YEAR COURSE IN WEST BENGAL, A STATE OF INDIA. IN THIS CURRICULUM IN EACH COURSE-PAPER THEORY AND PRACTICUM ARE GIVEN EQUAL IMPORTANCE SO IS IN MATHEMATICS EDUCATION ALSO. IN THIS NEW APPROACH MOST OF THE EDUCATIONAL EXPERIENCES IN MATHEMATICS EDUCATION, GATHERED BY THE TRAINEES ARE SET AND ORGANIZED BY COMBINING THEORY AND PRACTICUM. SO, INSTEAD OF ONLY THEORY IN THIS PAPER RELATIONSHIP IS DISCUSSED ON INTERTWINED FUNCTION OF THEORY AND PRACTICUM WITH PRACTICE. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.25](https://doi.org/10.37626/GA9783959871129.0.25) DE LANGE, JAN: CURIOUS MINDS: SERIOUS PLAY. PP 130 – 135 WE DESCRIBE THE BACKGROUND, THEORY, IMPLEMENTATION AND RESULTS SO FAR OF THE CURIOUS MINDS PROJECT, CARRIED OUT BY SEVEN DUTCH AND BELGIAN UNIVERSITIES. THE PRESENT ARTICLE FOCUSES ON THE UTRECHT UNIVERSITY'S INVOLVEMENT AND RESULTS. ISSUES ADDRESSED ARE: HYPOTHESIS, ROLE OF MANIPULATIVES (TOYS), DESIGNING STUDENT ACTIVITIES FROM PRE-PRIMARY TO PRIMARY, CREATIVITY AND CURIOSITY, THE ROLE OF ADULTS AND THE CHALLENGES FOR PROFESSIONAL DEVELOPMENT. KEYWORDS: EARLY CHILDHOOD, CURIOSITY, SCIENTIFIC REASONING, PRACTICE. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.26](https://doi.org/10.37626/GA9783959871129.0.26) DEMIRBEC, MAIFER REMZIE: PUERTO RICO GAS PRICES FALL – „THE MATH OF CHEAP OIL“. PP 136 – 138 THIS PROJECT IS AN APPLICATION OF “RATE OF CHANGE” AND “EQUATION OF THE LINE” IN BUSINESS AND FINANCE FIELD, AS PART OF COLLEGE ALGEBRA AND TRIGONOMETRY SYLLABUS. THE GOAL OF THIS PROJECT IS TO DEVELOP STUDENTS' SKILLS TO UNDERSTAND AND INTERPRET GRAPHS, TABLES, MATH CONCEPTS AS ABSOLUTE VALUE AND PERCENT CHANGE BY SHOWING THEM HOW MATH IS CONNECTED WITH REAL LIFE ISSUES. ALSO, IS TO ENGAGE STUDENTS WITH THE TOPIC AND THROUGH THAT HOW TO USE THEIR MATH KNOWLEDGE OF READING TABLES, COMPLETE TABLES, CALCULATE THE ABSOLUTE AND PERCENT CHANGE, CONSTRUCT AND INTERPRET GRAPHS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.27](https://doi.org/10.37626/GA9783959871129.0.27) DICK, THOMAS P.; PILGRIM, MARY E.: LEARNING (AND LEARNING TEACHING) BY DOING PROBLEMS. PP 139 – 144 ACTIVE LEARNING IS OFTEN A CHALLENGE TO FIND IN MATHEMATICS CLASSROOMS AT THE POST-SECONDARY LEVEL. STILL, TEACHERS ARE EXPECTED TO BE EXPERTS IN STUDENT-CENTERED APPROACHES DESPITE NOT HAVING EXPERIENCES WITH SUCH APPROACHES AS STUDENTS. THE AIM OF THIS WORKSHOP IS TO INTRODUCE PARTICIPANTS TO A TOTALLY PROBLEM-BASED INSTRUCTIONAL EXPERIENCE, WITH THE OPPORTUNITY TO ACTIVELY ENGAGE IN MATHEMATICS AS STUDENTS. DURING THE WORKSHOP, PARTICIPANTS WILL ENGAGE IN DISCOURSE AND REFLECTION – REFLECTION ON BOTH MATHEMATICS AS WELL AS THE IMPACT SUCH A PROBLEM-BASED INSTRUCTIONAL EXPERIENCE COULD HAVE ON THEIR PRACTICE. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.28](https://doi.org/10.37626/GA9783959871129.0.28) DORRINGTON, PAM: FAMILY MATHS: EXPERIENTIAL LEARNING. PP 145 – 149 THE INTERNATIONAL FAMILY MATHS PROGRAMME ADOPTS AN INQUIRY TEACHING AND LEARNING APPROACH AND IT ENCOURAGES LEARNERS, OFTEN FROM DIVERSE BACKGROUNDS, TO PARTICIPATE FULLY IN THE LEARNING PROCESS. THE PROGRAMME ALSO AIMS TO DEVELOP THE VOCABULARY NECESSARY FOR MEANINGFUL COMMUNICATION IN MATHEMATICS, DEVELOP PROBLEM SOLVING SKILLS AND INCREASE CONFIDENCE AND ENJOYMENT OF MATHEMATICS. THE PROGRAMME HAS PROVEN TO BE A POWERFUL CATALYST IN THIS REGARD AND HOLDS IMPORTANT LESSONS FOR BOTH CURRICULUM DEVELOPMENT AND DEVELOPING POSITIVE ATTITUDES TOWARDS MATHEMATICS TEACHING AND LEARNING. THIS EXPERIENTIAL LEARNING, INTERACTIVE WORK-SESSION FOCUSES ON PRIMARY SCHOOL MATHEMATICS CURRICULA (FOR PUPILS APPROXIMATELY 9 – 13 YEARS OF AGE) AND AIMS AT GIVING PARTICIPATING CONFERENCE DELEGATES AN OPPORTUNITY TO ENGAGE WITH AND EXPERIENCE SOME OF THE HANDS-ON PROBLEM SOLVING ACTIVITIES USED IN THE FAMILY MATHS PROGRAMME. DISCUSSION WILL BE ENCOURAGED AROUND THE RELEVANCE OF THESE ACTIVITIES FOR THE TEACHING AND LEARNING OF MATHEMATICS. OUR CONFERENCE ORGANISERS ENCOURAGE PRESENTERS TO CONSIDER THE RELATIONSHIP BETWEEN RESEARCH AND CLASSROOM TEACHING,

AND HOW, AND IF, THESE RELATE TO EACH OTHER IN PRACTICE. CAN THE FAMILY MATHS PHILOSOPHY AND PRACTICE BE A CATALYST IN NARROWING THE DIVIDE BETWEEN THE THEORY AND PRACTICE OF EFFECTIVE MATHEMATICS TEACHING AND LEARNING? <https://doi.org/10.37626/GA9783959871129.0.29> FERRARELLO, DANIELA; ET AL: SERIOUS GAMES IN TEACHING/LEARNING MATHEMATICS: THE EXPERIENCE OF FUNGo. PP 150 – 155 IN THIS PAPER WE PRESENT A GENERAL OVERVIEW OF SERIOUS GAMES AND THEIR EDUCATIONAL POTENTIAL. WE FOCUS IN PARTICULAR ON SERIOUS GAMES FOR THE TEACHING/LEARNING OF MATHEMATICS, HIGHLIGHTING HOW THE METHOD OF HORIZONTAL TEACHING IS EFFECTIVE IN ENABLING STUDENTS TO ACHIEVE THE LEARNING OBJECTIVES SET BY THE TEACHER. FUNGo, A SERIOUS GAME DESIGNED BY THE AUTHORS (RESEARCHERS IN MATHEMATICS EDUCATION) IN SYNERGY WITH A GROUP OF GRAPHIC DESIGNERS AND COMPUTER SCIENTISTS, IS PART OF THIS LINE OF IDEAS. WE WILL SHOW HOW FUNGo HAS A MULTIPLE USABILITY: IT HAS, IN FACT, A DOUBLE DIDACTIC USE AND HAS BEEN USED IN PUBLIC EVENTS OF DISSEMINATION OF MATHEMATICS, REPORTING IN BOTH CASES POSITIVE RESULTS. <https://doi.org/10.37626/GA9783959871129.0.30> FINE, BENJAMIN; ET AL: THE IMPACT OF MATHEMATICS AND MATHEMATICIANS. PP 156 – 160 THE 1600'S USHERED IN OUR MODERN WORLD, BUT NOT IN THE WAY MOST PEOPLE LEARN IN SCHOOL. THERE WAS A REVOLUTION; STARTED BY KEPLER, CONTINUED BY GALILEO, DESCARTES AND FERMAT AND CULMINATING IN NEWTON AND LEIBNIZ. THIS REVOLUTION ALLOWED FOR THE DEVELOPMENT OF MODERN MATHEMATICS WHICH IN TURN LED TO MODERN SCIENCE AND ENGINEERING TO ADVANCE. HENCE, THE TECHNOLOGICAL REVOLUTION OCCURRED WHICH HAS SHAPED OUR PRESENT-DAY EXISTENCE MUCH MORE THAN ANYTHING ELSE. IN THIS ARTICLE WE EXAMINE THESE DEVELOPMENTS DURING THE AMAZING SEVENTEENTH CENTURY. WE KEEP AN EYE ON THE FACT THAT FOR WHATEVER REASON HUMAN BEINGS FOR THE MOST PART SEEM NOT TO DO HARD ENGINEERING UNTIL THE HARD SCIENCE IS DEVELOPED AND NOT TO DO THE HARD SCIENCE UNTIL THE CORRECT MATHEMATICS HAS BEEN DISCOVERED. <https://doi.org/10.37626/GA9783959871129.0.31> FOX, COURTNEY: CLEAN WATER FOR WOMEN AND CHILDREN. PP 161 – 163 THIS WORKSHOP GIVES PARTICIPANTS AN OUTLINE OF A FULL UNIT IN TRIGONOMETRY THAT COVERS RIGHT TRIANGLE TRIGONOMETRY, THE LAW OF SINES, AND THE LAW OF COSINES. ATTENDEES WILL PARTICIPATE IN ABBREVIATED STUDENT TASKS. IN THE UNIT STUDENTS ARE INTRODUCED TO THE WORLD WATER CRISIS AND HOW IT AFFECTS WOMEN AND CHILDREN THE MOST AND WHY THIS IS. USING THEIR KNOWLEDGE OF TRIGONOMETRY AND THE DESMOS (OR OTHER GRAPHING) CALCULATOR TO “SOLVE” A WATER CRISIS IN A TOWN AND BRING CLEAN SANITATION TO A REMOTE ISLAND. THIS UNIT HELPS STUDENTS DEVELOP CRITICAL THINKING AND PROBLEM-SOLVING SKILLS, NUMERICAL LITERACY, AND GLOBAL AWARENESS. STUDENTS MAKE CONNECTIONS TO THE “REAL WORLD” USING MATHEMATICS AND BECOME WORLD CITIZENS. <https://doi.org/10.37626/GA9783959871129.0.32> GALLUZZO, BEN; KAVANAGH, KATIE: GETTING STARTED GETTING STUDENTS MODELING: DESIGNING AND FACILITATING OPEN-ENDED MATH MODELING EXPERIENCES. PP 164 – 167 “MODELING” IS A TERM THAT HAS SEVERAL MEANINGS IN GENERAL, BUT PARTICULARLY IN MATHEMATICS. HERE MATH MODELING REFERS TO THE PROCESS OF CREATING A MATHEMATICAL REPRESENTATION OF A REAL-WORLD SCENARIO TO MAKE A PREDICTION OR PROVIDE INSIGHT. THERE IS A DISTINCTION BETWEEN USING A FORMULA THAT ARISES FROM AN APPLICATION (FOR EXAMPLE, DISTANCE EQUALS RATE TIMES TIME) AND THE ACTUAL CREATION OF A MATHEMATICAL RELATIONSHIP ITSELF THAT CAN BE USEFUL IN AN APPLIED SETTING. IN THIS TWO PART WORKSHOP, WE DEMONSTRATE HOW TO DEVELOP AUTHENTIC MATH MODELING CHALLENGE PROBLEMS THAT ARE ACCESSIBLE AND RELEVANT TO STUDENTS. IN THE SECOND PART OF THE WORKSHOP WE TALK ABOUT HOW TO FACILITATE MATH MODELING SO THAT STUDENTS HAVE AN OPPORTUNITY TO BE CREATIVE AND INNOVATIVE IN THEIR MODELING PROCESS WHILE HAVING OWNERSHIP OVER THEIR SOLUTION. <https://doi.org/10.37626/GA9783959871129.0.33> GAZIT, AVIKAM: MATHE TEACHERS' ATTITUDES TOWARD INTEGRATING HUMOR IN MATH LESSONS. PP 168 – 172 THE PURPOSE OF THIS STUDY WAS TO EXAMINE THE ATTITUDES MATHEMATICS TEACHERS TOWARD INTEGRATING HUMOR IN MATH LESSONS. MATHEMATICS AND HUMOR ARE NOT SEEN AS CONSISTENT WITH EACH OTHER. MATHEMATICS IS SEEN AS A SUBJECT IS DIFFICULT TO UNDERSTAND AND ITS SUBJECT MATTER IS ISOLATED WITHOUT ANY HUMANISTIC ELEMENTS. INTEGRATING HUMOR IN MATH LESSONS MAY CREATE A PLEASANT ATMOSPHERE AND REDUCE MATH ANXIETY. HUMOR CAN INCREASE MOTIVATION AS WELL AS PROMOTING CREATIVE THINKING. A SAMPLE OF 25 MATH TEACHERS, MOST OF THEM FROM ELEMENTARY SCHOOLS, ANSWERED A QUESTIONNAIRE. AN IMPORTANT CONCLUSION TO BE DRAWN FROM THE FINDINGS IS THE POSITIVE ATTITUDES OF THE TEACHERS REGARDING THE INTEGRATION OF HUMOR IN MATH LESSONS. IT RECOMMENDED STRENGTHEN MATH TEACHER TO INTEGRATE HUMOR IN THEIR LESSONS. <https://doi.org/10.37626/GA9783959871129.0.34> GILL, EOIN: MATHS WEEK IRELAND: PROMOTING A POSITIVE ATTITUDE TO MATHEMATICS IN IRELAND. PP 173 – 176 MATHS WEEK IRELAND IS AN ANNUAL FESTIVAL ESTABLISHED IN 2006 BY PEOPLE IN THE STEM COMMUNITY AS AN ALL-ISLAND EVENT INCLUDING THE REPUBLIC OF IRELAND AND NORTHERN IRELAND. PARTICULAR EFFORT IS MADE TO HIGHLIGHT MATHS FOR LIFE, FOR CAREERS AND AS PART OF OUR CULTURE. WHILE THE CORE PRINCIPLE IS “MATHS FOR ALL” THE MAIN ENGAGEMENT IS WITH SCHOOLS. IN 2018 TEACHERS REPORTED 354,000 PRIMARY AND SECOND LEVEL PUPILS PARTICIPATING THROUGH IN-SCHOOL ACTIVITIES, ONLINE ACTIVITIES AND EVENTS AT PARTNER CENTRES. MATHS WEEK CREATES AN OPPORTUNITY TO DISSEMINATE NEW IDEAS IN MATHS EDUCATION. IT ALSO CREATES A SPACE WHEREBY TEACHERS CAN TRY OUT NEW IDEAS AND INVENT AND CREATE NEW ACTIVITIES WITH THEIR PUPILS. THIS PAPER DESCRIBES THE ORGANISATION AND ACTIVITIES OF MATHS WEEK AND DISCUSSES THE IMPACT OF THE INITIATIVE WITH PARTICULAR REFERENCE TO EVALUATION WITH TEACHERS. <https://doi.org/10.37626/GA9783959871129.0.35> GOODELL, JOANNE E.: LEARNING TO TEACH MATHEMATICS THROUGH PROJECT-BASED INSTRUCTION. PP 177 – 182 PROJECT-BASED INSTRUCTION (PBI) IS GAINING

PROMINENCE IN THE USA AS AN INSTRUCTIONAL INNOVATION THAT PROMOTES DEEP AND CONNECTED UNDERSTANDING IN MATHEMATICS. IN THIS PAPER, I DESCRIBE A PROGRAM DEVELOPED AT THE UNIVERSITY OF TEXAS AT AUSTIN KNOWN AS UTEACH THAT IS BEING REPLICATED IN 45 UNIVERSITIES ACROSS THE USA. CONCEPTS OF INQUIRY TEACHING, PROBLEM-BASED AND PROJECTBASED INSTRUCTION ARE DEVELOPED ACROSS THE PROGRAM. IN THIS PAPER I ARGUE THAT THE STRUCTURE, TIMING AND LOCATION OF STUDENT TEACHING IMPACTS WHETHER OR NOT PRE-SERVICE TEACHERS ARE ABLE TO IMPLEMENT PBI DURING STUDENT TEACHING, WHICH IN TURN IMPACTS SATISFACTION WITH THE STUDENT TEACHING EXPERIENCE AND ULTIMATELY THE INTENTION TO ENTER AND CONTINUE IN THE TEACHING PROFESSION. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.36](https://doi.org/10.37626/GA9783959871129.0.36) GORDON, JOHN; ET AL: A PROBLEM-SOLVING APPROACH TO THE INTRODUCTION TO ORDINARY DIFFERENTIAL EQUATIONS FOR UNDERGRADUATE STUDENTS AT AN AMERICAN TWO-YEAR COLLEGE. PP 183 – 188 UNDERGRADUATE STUDENTS IN STEM (SCIENCE, TECHNOLOGY, ENGINEERING, AND MATHEMATICS) AT CITY UNIVERSITY OF NEW YORK (CUNY)-QUEENSBOROUGH COMMUNITY COLLEGE (QCC) WORKING TOWARD A BACCALAUREATE DEGREE AT ONE OF CUNY'S SENIOR COLLEGES ARE REQUIRED TO TAKE AN INTRODUCTORY COURSE IN ORDINARY DIFFERENTIAL EQUATIONS (ODE). FACULTY IN THE MATHEMATICS DEPARTMENT AT QCC ARE EXPERIMENTING WITH A PROBLEM-SOLVING APPROACH TO THIS COURSE IN WHICH STUDENTS ENGAGE IN LEARNING COURSE MATERIAL THROUGH THE DEVELOPMENT OF MATHEMATICAL MODELS OF REAL-WORLD PROBLEMS. THE RESULTS SEEM PROMISING AND WE OUTLINE THEM IN THIS PAPER. KEY-WORDS: FIRST-ORDER, LINEAR SYSTEM, INTEGRATING FACTOR, HOMOGENEOUS EQUATION, RESEARCH-BASED. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.37](https://doi.org/10.37626/GA9783959871129.0.37) GRZEGORCZYK, IVONA: MAGIC TRICKS AND ACTIVITIES SUPPORTING ABSTRACT THINKING IN MATHEMATICS. PP 189 – 192 THIS WORKSHOP WILL INVOLVE YOU IN MATHEMATICS BASED MAGIC TRICKS ACTIVITIES PROMOTING PATTERN RECOGNITION AND ALGEBRAIC MODELING IN VARIOUS CONTEXTS. THE INTERACTIVE, HANDS-ON ACTIVITIES ARE DESIGNED FOR INTRODUCTORY ALGEBRA COURSES, BUT THEY CAN BE MODIFIED TO GENERATE MORE COMPLEXITY AND ADVANCED MATHEMATICAL THINKING. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.38](https://doi.org/10.37626/GA9783959871129.0.38) GUREVICH, IRINA: DO FUTURE MATHEMATICS TEACHERS NEED THE COURSE „INTEGRATION OF DIGITAL TECHNOLOGIES IN TEACHING MATHEMATICS“, AND IF SO, WHAT EXACTLY CAN IT HELP THEM WITH? PP 193 – 198 IN THE CURRENT RESEARCH WE ANALYSED OUR TEACHING EXPERIENCE IN THE COURSE “INTEGRATION OF DIGITAL TECHNOLOGIES IN TEACHING MATHEMATICS”. THE STUDENTS WERE MATHEMATICS STUDENT TEACHERS. THE MAIN GOAL OF THE COURSE WAS TO DEMONSTRATE THE POTENTIAL OF DIGITAL TECHNOLOGIES IN TEACHING MATHEMATICS AND TO PROVIDE THE STUDENTS WITH BASIC SKILLS IN THE INTELLECTUAL USE OF THESE TECHNOLOGIES. DURING THE COURSE THE STUDENTS, AFTER GETTING ACQUAINTED WITH VARIOUS MATHEMATICAL SOFTWARE PACKAGES, BUILD AND PRESENT THEIR OWN TEACHING UNITS. WE WERE INTERESTED TO ANALYSE THE STUDENTS' ATTITUDES TOWARDS THE COURSE. A MULTIPLE-CHOICE QUESTIONER WAS FORMULATED, AND THE COLLECTED DATA WERE ANALYSED. WE OBSERVED THAT MOST OF THE STUDENTS FOUND THE COURSE BEING HELPFUL FOR THEIR FUTURE TEACHING. THE OBTAINED RESULTS INDICATED THAT THE DESCRIBED COURSE PROVIDED THEM A DIDACTIC MODEL TO EMULATE. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.39](https://doi.org/10.37626/GA9783959871129.0.39) HANSEN, HEIDI B.; MAGIERA, MARTA T.: WORKING TOGETHER: A CROSS-CULTURAL STUDY ADDRESSING MATHEMATICS ANXIETY IN K-8 PRE-SERVICE TEACHERS. PP 199 – 204 THIS STUDY WILL PRESENT DATA FROM RESEARCH ON K-8 PRE-SERVICE TEACHERS' MATH ANXIETY ACROSS THREE UNIVERSITIES: ONE PUBLIC, ONE PRIVATE AND ONE NON-U.S. THE ARTICLE DISCUSSES BACKGROUND RATIONALE, LITERATURE, TOOLS USED AND RESULTS OF THIS STUDY. THE RESULTS OF THE STUDY INDICATED THAT SIMILAR MATH ANXIETY LEVELS EXIST IN STUDENTS IN ALL THREE TYPES OF ACADEMIC INSTITUTIONS. THE PAPER ALSO INCORPORATES DISCUSSION OF THE IMPORTANCE OF INCLUDING THE TOPIC IN PRE-SERVICE TEACHER TRAINING, AND POSSIBLE INTERVENTIONS FOR ALLEVIATING MATH ANXIETY. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.40](https://doi.org/10.37626/GA9783959871129.0.40) HANSEN-SMITH, BRADFORD: WHY THE CIRCLE CANNOT BE SQUARED. PP 205 – 210 SQUARING THE CIRCLE USING COMPASS AND STRAIGHT EDGE IN SUCH A WAY THAT BOTH HAVE THE SAME AREA IS NOT POSSIBLE. THE QUESTION IS, WHY NOT? MATH LOGIC ASSUMES THERE MUST BE AN AREA EQUAL TO BOTH. PRESUMABLY THERE IS A NEED TO MAKE THESE VERY DIFFERENT 2-D SHAPES EQUAL, POSSIBLY TO FIND A GEOMETRIC PROOF TO AN INVERSE MATHEMATICAL CONCEPT ABOUT DIFFERENCES. TO “SQUARE THE CIRCLE” GIVES PREFERENCE TO THE SQUARE, FOUR STRAIGHT LINES AND FOUR  $90^\circ$  ANGLES, OVER A SINGLE LINE OF THE CIRCLE WITHOUT ANGLES. MAYBE THE EMPHASIS MORE CORRECTLY IS ABOUT THE RELATIONSHIP OF DIFFERENCE. LOGICALLY THE TRUNCATION PROCESS SUGGESTS THE CIRCLE IS ORIGIN TO THE SQUARE, MEANING THERE CAN BE NO POLYGON EQUAL TO THE CIRCLE. FOLDING THE CIRCLE GIVES A UNIQUE PERSPECTIVE ABOUT THE RELATIONSHIP OF CIRCLE TO SQUARE, REVEALING  $90^\circ$  TO BE AN ANGLE OF CHANGE, OF DIRECTIONAL MOVEMENT BETWEEN TWO POINTS BEFORE ANY CONSTRUCTION OF A FIXED ANGLE OR MEASURING OF LINES AND AREAS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.41](https://doi.org/10.37626/GA9783959871129.0.41) HERRELKO, JANET M.: CHANGE THE PARADIGM OF SOLITARY LESSON PLANNING TO COLLABORATIVE PLANNING THAT UNITES RESEARCH AND PRACTICE. PP 211 – 216 TEACHERS ARE PLANNING MATHEMATICS LESSONS USING A BASIC PROTOCOL CREATED IN THE 17TH CENTURY. THE RESULTS OF THE PROGRAMME FOR INTERNATIONAL STUDENT ASSESSMENT PROVIDE EVIDENCE THAT THIS IS NOT A SUCCESSFUL APPROACH TO TEACHING STUDENTS MATHEMATICAL CONCEPTS TODAY. RESEARCH IN COGNITIVE SCIENCES HAS ESTABLISHED HOW PEOPLE ATTEND TO, SORT, AND STORE NEW CONTENT. EDUCATIONAL RESEARCH PROVIDES CASE STUDIES OF SUCCESSFUL PEDAGOGICAL METHODS THAT HELP STUDENTS LEARN. IT IS TIME FOR MATHEMATICS EDUCATORS TO UNITE THESE RESOURCES TO CREATE INTEGRATED LESSONS THAT FOCUS ON PROBLEM SOLVING WITH EXPERIENTIAL LEARNING. THIS IS A PROPOSAL TO HAVE TEACHERS INTEGRATE EDUCATIONAL AND COGNITIVE RESEARCH CREATING LESSONS THAT IMPROVE ACCESS AND EQUITY TO HELP STUDENTS LEARN MATHEMATICS.

<https://doi.org/10.37626/GA9783959871129.0.42> HORWITZ, KENNETH: UTILIZING ANALYTICS TO SHOW REPRESENTATIONS USED IN COMPARING AND ORDERING UNIT FRACTIONS. PP 217 – 222 VIDEO ANALYTICS BRING TOGETHER THE WORLD OF EDUCATIONAL RESEARCH AND CLASSROOM TEACHING WITH TECHNOLOGY AND THE INTERNET. THROUGH USE OF MORE THAN 4500 HOURS OF VIDEO DATA, AN OPEN SOURCE ANALYTIC CREATION TOOL, THIS STUDY CREATES A VIDEO ANALYTIC THAT SUPPORTS A RESEARCH PAPER. IN ADDITION TO SUPPORTING RESEARCH, ANALYTICS CAN BE A REFLECTIVE TOOL FOR TEACHERS, AS WELL AS SUPPORT PROFESSIONAL DEVELOPMENT AS ALL LEVELS. THIS REPORT ILLUSTRATES THE VIDEO ANALYTIC, USING MEREDITH'S MODELS TO REASON ABOUT COMPARING AND ORDERING UNIT FRACTIONS, (HORWITZ, 2015, AVAILABLE AT [HTTP://DX.DOI.ORG/DOI:10.7282/T33J3FQG](http://dx.doi.org/doi:10.7282/T33J3FQG)), AS WELL AS THE METHODS USED IN THE CREATION OF THE ANALYTIC USED TO SUPPORT RESEARCH IN STUDENT USE OF REPRESENTATIONS TO MAKE SENSE OF FRACTIONS.

<https://doi.org/10.37626/GA9783959871129.0.43> HUANG, Hsin-Mei E.; ET AL: INVESTIGATING JUNIOR HIGH SCHOOL STUDENTS' LENGTH ESTIMATION ABILITY AND STRATEGIES. PP 223 – 228 THIS STUDY INVESTIGATED JUNIOR HIGH SCHOOL STUDENTS' LENGTH ESTIMATION ABILITY WITH RESPECT TO EVERYDAY OBJECTS WITH LENGTHS BETWEEN 1 MILLIMETRE AND 1 METER. STUDENTS' STRATEGIES USED FOR ESTIMATING THE LENGTH OF THE LONGER SIDE OF A BASKETBALL COURT IN SCHOOL WERE ANALYSED. A TOTAL OF 240 GRADE 7-9 STUDENTS FROM CITIES IN NORTHERN TAIWAN COMPLETED A PAPER-AND-PENCIL TEST ASSESSING LENGTH ESTIMATION ABILITIES. RESULTS SHOWED A SIGNIFICANT GENDER EFFECT ON LENGTH ESTIMATION, BUT NEITHER EFFECTS OF GRADE LEVEL NOR ANY INTERACTION BETWEEN GRADE LEVEL AND GENDER ON LENGTH ESTIMATION. ABOUT 40% OF THE STUDENTS USED EFFECTIVE STRATEGIES FOR ESTIMATING LENGTH MEASURES, INCLUDING VISUALIZING, UTILIZING BODY PARTS, APPLYING PREVIOUS EXPERIENCES, USING A MENTAL RULER, AND MAKING USE OF OBJECTS NEARBY. STILL, ABOUT 60% OF THE STUDENTS USED INEFFECTIVE STRATEGIES SUCH AS GUESSING. IMPLICATIONS FOR RESEARCH AND EDUCATION PRACTICES ARE DISCUSSED. <https://doi.org/10.37626/GA9783959871129.0.44> HUMAR<sup>2</sup> N MART<sup>2</sup> NEZ, YUITZA T.: USING MANIPULATIVES TO DEVELOP THE UNDERSTANDING OF THE CONCEPT OF THE FRACTION OF PRESERVICE ELEMENTARY TEACHERS: THE MEANING OF MEASURE. PP 229 – 234 MANIPULATIVES ARE A TOOL WHEN THAT WELL-IMPLEMENTED CAN CONTRIBUTE TO THE DEVELOPMENT OF MATHEMATICAL CONCEPTS AND PROCESSES, AND IS A POPULAR STRATEGY IN ELEMENTARY SCHOOL. HOWEVER, EDUCATORS USUALLY DON'T USE THIS TECHNIQUE EFFICIENTLY FOR SEVERAL REASONS. FOR EXAMPLE, THEY HAD NEVER USED MANIPULATIVES BEFORE STARTING TO WORK AT SCHOOL. IN THIS QUASI-EXPERIMENTAL RESEARCH, THE UNDERSTANDING OF PRESERVICE ELEMENTARY SCHOOL TEACHERS OF THE CONCEPT OF THE FRACTION, SPECIFICALLY, THE MEANING OF MEASURE, WAS STUDIED. STATISTICALLY SIGNIFICANT EVIDENCE WAS GATHERED TO CONCLUDE THAT THE UNDERSTANDING OF THE MEANING OF MEASURE IMPROVES AFTER THE IMPLEMENTATION OF THE LESSON WITH TANGIBLE MANIPULATIVES.

<https://doi.org/10.37626/GA9783959871129.0.45> HYDORN, DEBRA L.: TOOLS FOR MODERN MATHEMATICS: A COURSE TO INTRODUCE EXPERIMENTAL MATHEMATICS. PP 235 – 239 THE ACCESSIBILITY OF COMPUTATIONAL METHODS AND RESOURCES HAS MADE IT EASIER TO INCLUDE UNDERGRADUATES IN MATHEMATICAL RESEARCH PROJECTS. HOWEVER, BASED ON THE TRADITIONAL FORM OF MATHEMATICS EDUCATION, MANY STUDENTS AREN'T CONFIDENT IN DEVELOPING THEIR OWN RESEARCH QUESTIONS OR CONJECTURES. ORIGINALLY CREATED TO INTRODUCE STUDENTS TO PROGRAMMING TOOLS (R, MATHEMATICA AND MATLAB), THIS COURSE HAS EVOLVED INTO AN INTRODUCTION TO EXPERIMENTAL MATHEMATICS. STUDENTS FIRST LEARN THE FUNDAMENTALS OF PROGRAMMING ALONG WITH ALGORITHMIC STRUCTURES AND METHODS OF SIMULATION. THEN, FOLLOWING THE APPROACH USED BY THE SUMMER UNDERGRADUATE RESEARCH INSTITUTE IN EXPERIMENTAL MATHEMATICS AT MICHIGAN STATE UNIVERSITY, STUDENTS PARTICIPATE IN (1) AN EXPERIMENTAL PHASE, WHERE THEY USE ALGORITHMS AND SIMULATIONS TO PRODUCE OUTPUT, (2) A CONJECTURE PHASE, WHERE THEY REVIEW THEIR OUTPUT TO IDENTIFY POTENTIAL RELATIONSHIPS AND PATTERNS, AND (3) A 2ND EXPERIMENTAL PHASE WHERE ADDITIONAL OUTPUT IS PRODUCE TO DETERMINE IF ANY OF THEIR CONJECTURES ARE STILL VIABLE. THE FOCUS OF THE COURSE IS ON DEVELOPING STUDENTS' ABILITY TO POSE RESEARCH QUESTIONS AND THEIR ABILITY TO USE COMPUTATIONAL TOOLS TO ADDRESS THOSE QUESTIONS. <https://doi.org/10.37626/GA9783959871129.0.46> IJI, CLEMENT O.; ANDORTAN, JOSEPH A.: BRANDISHING ETHNO-MATHEMATICS APPROACH AS AN INTERFACE FOR IMPROVING UPPER BASIC EDUCATION (UBE) STUDENTS' INTEREST AND ACHIEVEMENT IN NUMBER AND NUMERATION. PP 240 – 244 THE STUDY CONSIDERED HOW ETHNO-MATHEMATICS APPROACH COULD BE BRANDISHED TO SERVE AS AN INTERFACE TO IMPROVING UBE STUDENTS' INTEREST AND ACHIEVEMENT IN NUMBER AND NUMERATION (NN). THE STUDY WAS CARRIED OUT IN OBUDU, A RURAL COMMUNITY IN CROSS RIVER STATE OF NIGERIA. IT ADOPTED A QUASI-EXPERIMENTAL OF PRE-TEST POST-TEST CONTROL GROUPS DESIGN WITH INTACT CLASSES USED. POPULATION OF STUDY COMPRISED ALL THE 6,226 UPPER BASIC EDUCATION STUDENTS FROM THE 23 GOVERNMENT CONTROLLED BASIC EDUCATION SCHOOLS IN THE STUDY AREA. TWO INSTRUMENTS WERE USED FOR DATA COLLECTION. THE STUDY FOUND AMONG OTHER THINGS THAT WHEN ETHNOMATHEMATICS WAS PROPERLY BRANDISHED, THE UBE STUDENTS IMPROVED IN THEIR INTEREST AND ACHIEVEMENT IN THE NN CONCEPTS TAUGHT DURING THE PERIOD OF THIS STUDY. IT WAS ALSO FOUND THAT THE INITIAL NOTED GAP BETWEEN THE MALE AND FEMALE UBE STUDENTS' INTEREST AND ACHIEVEMENT IN NN WAS DRASTICALLY REDUCED. KEY WORDS: BRANDISHING, ETHNOMATHEMATICS, INTERFACE, NUMBER AND NUMERATION, UPPER BASIC EDUCATION, INTEREST AND ACHIEVEMENT <https://doi.org/10.37626/GA9783959871129.0.47> INNABI, HANAN; ET AL: PATTERNS OF VARIATION IN THE WORK OF „MATHEMATICS IN THE CITY PROJECT“: A SUGGESTED RESEARCH QUESTION. PP 245 – 250 THE FRAMEWORK OF THIS PAPER IS BASED ON THE VARIATION THEORY (VT), WHICH EXPLAINS THE NECESSARY CONDITIONS

FOR LEARNING. ACCORDING TO THIS THEORY, STUDENTS HAVE TO EXPERIENCE PATTERNS OF VARIATION FOR LEARNING TO TAKE PLACE. THIS PAPER HIGHLIGHTS THE PATTERNS OF VARIATION THAT CAN BE FOUND IN THE WORK OF THE “MATHEMATICS IN THE CITY” (MITC) PROJECT. SOME EXAMPLES ARE PRESENTED, AND A RESEARCH QUESTION IS PROPOSED RELATED TO USING VT AS A TOOL TO ANALYZE STUDENTS’ LEARNING IN THE MITC CLASSROOMS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.48](https://doi.org/10.37626/GA9783959871129.0.48)

JACKSON, COLIN: GOING AGAINST THE GRAIN: CRITICAL THINKING IN AND BEYOND MATHEMATICS. PP 251 – 256 IN THE UK, IT IS ALMOST UNIVERSAL THAT SECONDARY MATHEMATICS IS TAUGHT IN CLASSES ORGANISED ON THE BASIS OF DIFFERENTIAL ‘ABILITY’: ALL-ATTAINMENT TEACHING IS RARE. THIS PAPER IS BASED ON DATA COLLECTED FROM IN-DEPTH INTERVIEWS WITH A SMALL NUMBER OF TEACHERS WHOSE BELIEFS AND PRACTICES DEFY THIS NORM. A NUMBER OF THEMES EMERGED IN THEIR TEACHING, BUT IN THIS PAPER I EXPLORE, VERY BRIEFLY, HOW THE TEACHERS ENACTED THEIR BELIEF IN THE IMPORTANCE OF DEVELOPING THEIR STUDENTS’ CRITICAL THINKING SKILLS AS WELL AS THEIR MATHEMATICS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.49](https://doi.org/10.37626/GA9783959871129.0.49)

JIEW, FUI FONG; CHIN, KIN ENG: THE EMBODIMENT OF MATHEMATICAL MEANINGS WITH SPECIAL REFERENCE TO MULTIPLICATION: ISSUES AND CHALLENGES. PP 257 – 262 THIS PAPER AIMS TO ILLUSTRATE HOW TWO PRIMARY SCHOOL TEACHERS (DOREEN AND EDWIN – PSEUDONYMS) MAKE SENSE OF MATHEMATICS IN PARTICULAR THE MULTIPLICATION OF FRACTIONS AND DECIMALS. THE MEANING OF A PARTICULAR MATHEMATICAL EXPRESSION AND SYMBOL COULD BE CONVEYED THROUGH LANGUAGE HOWEVER A MATHEMATICAL PROCEDURE THAT IS PERFORMED FOR A PURPOSE MAY BE DIFFICULT TO MAKE SENSE SOMETIMES. DATA WERE COLLECTED THROUGH SEMISTRUCTURED INTERVIEWS. FINDINGS REVEALED THAT DOREEN RECOGNISED THE MEANING OF MULTIPLICATION AS THE NOTION “OF” IN THE CONTEXTS OF FRACTIONS. BOTH OF THEM ROTE LEARNED THE MATHEMATICAL PROCEDURES IN THE MULTIPLICATION OF FRACTIONS AND DECIMALS AND THEY COULD NOT MAKE SENSE OF THEM. ONE OF THE MAIN REASONS FOR THIS WAS BECAUSE THEY WERE NOT AWARE OF THE CHANGES OF MATHEMATICAL MEANINGS ACROSS DIFFERENT CONTEXTS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.50](https://doi.org/10.37626/GA9783959871129.0.50)

JOHNSTON, PETER; ET AL: SUPPORTING TRANSITION FOR MATHEMATICS AND SCIENCE STUDENTS UNDER AN ASSUMED KNOWLEDGE APPROACH. PP 263 – 268 IN AUSTRALIA THERE IS CONCERN OVER THE POOR MATHEMATICAL SKILLS OF STUDENTS ENTERING UNIVERSITY STEM DEGREES (KING & CATTLIN, 2015). CHALLENGED BY THE INTRODUCTION OF AN ASSUMED KNOWLEDGE APPROACH FOR MATHEMATICS DEPENDENT UNIVERSITY DEGREES, WE NOTED DIAGNOSTIC TESTING APPROACHES (N<sub>2</sub> FHLOINN ET AL., 2014) AND SOUGHT TO ADAPT THE SUCCESSFUL GETSET2 QUIZ THAT PREVIOUSLY HAD BEEN APPLIED ONLY TO PRE-REQUISITE MATHEMATICS UNIVERSITY ENTRY (BURTON ET AL., 2013). WE INTRODUCED THE ON-LINE SELF-ASSESSMENT GET READY MATHS/SCIENCE QUIZZES FOR COMMENCING SCIENCE AND MATHEMATICS STUDENTS. THIS ALLOWED STUDENTS TO RECEIVE TIMELY PERSONALISED FEEDBACK ON THEIR LEVEL OF KNOWLEDGE AND SKILLS COMPARED WITH THE EXPECTED ASSUMED/PRE-REQUISITE KNOWLEDGE FOR UNIVERSITY ENTRY. THIS PAPER REVIEWS THE DESIGN, DEVELOPMENT AND INITIAL IMPLEMENTATION OF TRANSITION QUIZZES UNDER THE CHALLENGES OF AN ASSUMED KNOWLEDGE FRAMEWORK, INSTEAD OF A PRE-REQUISITE FRAMEWORK. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.51](https://doi.org/10.37626/GA9783959871129.0.51)

JOHNSTON-WILDER, SUE; LEE, CLARE: HOW CAN WE ADDRESS MATHEMATICS ANXIETY MORE EFFICIENTLY AS A COMMUNITY? PP 269 – 274 MATHEMATICS ANXIETY HAS BEEN DISCUSSED FOR OVER 60 YEARS. THE MAJORITY OF THOSE SUFFERING BELONG TO AN IDENTIFIABLE SUBGROUP, OFTEN IDENTIFIED AS ‘FEMALE’, OR LEARNERS WITH A ‘FEELING’ RATHER THAN A ‘THINKING’ PREFERENCE, OR EMPATHISERS. THESE LEARNERS PREFER TO UNDERSTAND THE VALUE, MEANING, PURPOSE AND NARRATIVE OF THE MATHEMATICAL TOOLS THEY ARE REQUIRED TO LEARN. TEN YEARS AGO, WE PLANTED A SEED FOR A CHANGE IN PRACTICES THAT ENGENDER ANXIETY TO THOSE THAT BUILD A POSITIVE STANCE. THIS SEED HAS GROWN INTO A GROUP OF TEACHER AND RESEARCH PRACTITIONERS WORKING TO OVERCOME MATHEMATICS ANXIETY AND BUILD MATHEMATICAL RESILIENCE. THE PAPER DISCUSSES WHAT IS KNOWN, BY THESE RESEARCHERS AND TEACHERS, AND HOW TO DEVELOP INNOVATIVE COMMUNICATION IN ORDER TO WORK INTERNATIONALLY TOWARD ELIMINATION OF THE ACQUIRED, DISABLING CONDITION OF MATHEMATICS ANXIETY. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.52](https://doi.org/10.37626/GA9783959871129.0.52)

KAINO, LUCKSON MUGANYIZI: ENHANCING MATHEMATICAL MODELING ACTIVITIES IN CLASSROOM INSTRUCTION. PP 275 – 280 THE ABILITY OF STUDENTS IN MATHEMATICAL MODELING WAS ENHANCED THROUGH ACTIVITIES THAT INVOLVED SYSTEMS OF LINEAR EQUATIONS WITH TWO VARIABLES. STUDENTS INVOLVED WERE IN FORM FOUR, AT THE FINAL YEAR OF THE ORDINARY SECONDARY SCHOOL LEVEL WHERE THEY WERE EXPECTED TO HAVE MASTERED THE KNOWLEDGE ON SYSTEMS OF LINEAR EQUATIONS WITH TWO VARIABLES. STUDENTS’ KNOWLEDGE ON ILL-CONDITIONED LINEAR SYSTEMS WAS EXPLORED AS WELL AS THEIR KNOWLEDGE ON PRACTICAL PROBLEMS IN LINEAR EQUATIONS. THEN AFTER, MATHEMATICS SUBJECT TEACHERS GUIDED STUDENTS TO IDENTIFY PRACTICAL PROBLEMS IN LINEAR EQUATIONS OF TWO VARIABLES. STUDENTS WERE PUT INTO GROUPS TO THINK OF PROBLEMS IN REAL LIFE AND COME UP WITH SOLUTIONS. THE SOLUTIONS WERE RELATED TO THE REAL SITUATIONS IN THE ENVIRONMENT AND EACH GROUP HAD TO MAKE A PRESENTATION IN THE CLASS. PROBLEMS IN TRANSPORTATION, MANUFACTURING, PRODUCTION AND DIET WERE IDENTIFIED BY STUDENTS AND THE RESULTS PRESENTED FOR DISCUSSION. IT CAME OUT CLEARLY THAT STUDENTS ACQUIRED KNOWLEDGE ON SOLVING REAL LIFE PROBLEMS AT THE END OF THE ACTIVITIES. BEFORE THESE ACTIVITIES, STUDENTS HAD THEORETICAL KNOWLEDGE ON SOLVING PROBLEMS WITH TWO UNKNOWNNS WITHOUT RELATING THESE TO REAL LIFE PROBLEMS. WHILE KNOWLEDGE ON INDEPENDENT AND INCONSISTENT SYSTEMS WAS KNOWN TO STUDENTS, ENTHUSIASM WAS NOTED AMONG STUDENTS AT THE END OF THE ACTIVITIES WHEN THEY GOT INVOLVED IN REAL ASPECTS OF SOLUTIONS OBTAINED. IT WAS CONCLUDED THAT WITH MORE TIME AVAILED IN THE SCHOOL CURRICULA, STUDENTS CAN ACQUIRE USEFUL KNOWLEDGE ON MATHEMATICAL MODELING TO ACHIEVE PROBLEM-THINKING SKILLS THAT INVOLVE REAL LIFE

SITUATIONS. <https://doi.org/10.37626/GA9783959871129.0.53> KANIA, SYLWIA: SOLVING MATHEMATICAL PROBLEMS IN THE CONTEXT OF SOME OBSTACLES BETWEEN TEACHERS AND STUDENTS. PP 281 – 286 GREAT MATHEMATICAL DISCOVERIES ARE MOSTLY BASED ON HUGE KNOWLEDGE OF THEIR EXPLORERS AND LONG, SOLID WORK LEADING SLOWLY TO THE FINDING. THERE ARE ALSO WELL KNOWN CASES OF THE “ACCIDENTAL” DISCOVERIES THAT HAPPENED QUICKLY, INTENSE AND THEIR FOUNDERS DID NOT EVEN REALIZE THE RANGE OF THE DISCOVERY, BECAUSE THEY WERE WORKING ON SOMETHING ELSE AT THE TIME. NEVERTHELESS, EACH FINDING REQUIRES ENERGY, DEVOTION AND CONCENTRATION OF ITS DISCOVERER. SOLVING MATHEMATICAL PROBLEMS DEMANDS QUITE THE SAME THINGS, THUS TEACHERS MAY FIND SOME OPPORTUNITIES TO CREATE CURIOUS, OPEN-MINDED YOUNG DISCOVERERS. IT IS NOT AN EASY JOB TO DO THOUGH, BECAUSE THERE IS A GREAT RISK OF KILLING PUPILS’ ENTHUSIASM BY TEACHER’S SKEPTICISM, THERE IS A LARGE CHANCE TO NIP PUPILS’ ENERGY IN THE BUD BY ROUTINE OPERATIONS AND THERE IS A HUGE POSSIBILITY TO DISCOURAGE PUPILS’ ENDEAVORS BY GIVING THEM WRONG-CHOSEN PROBLEMS TO SOLVE.

<https://doi.org/10.37626/GA9783959871129.0.54> KENNEDY, TIERNEY: EXPLORING THE NATURE OF TEACHER QUESTIONING WITHIN CHALLENGING TASKS FOR INDUCING CONCEPTUAL CHANGE. PP 287 – 292 RECENT RESEARCH HAS CONSIDERED HOW TO SUPPORT TEACHERS USING CHALLENGING TASKS IN MATHEMATICS WITH STUDENTS WHO STRUGGLE. TEACHER QUESTIONING IN RESPONSE TO CORRECT OR INCORRECT ANSWERS HAS BEEN IDENTIFIED AS AN IMPORTANT ELEMENT FOR MAINTAINING THE COGNITIVE LOAD. THIS PAPER EXAMINES THE NATURE OF TEACHER QUESTIONING WITHIN CHALLENGING TASKS IN WHICH STRUGGLING STUDENTS WERE NOTED TO CHANGE THEIR OWN CONCEPTIONS AND PROPOSES A MINOR CHANGE TO INCLUDE A QUESTIONING PHASE WITHIN THE LAUNCH-EXPLORE-SUMMARISE STRUCTURE BY LAPPAN ET AL. (2006). IT PRESENTS EVIDENCE FROM A TWO-YEAR STUDY IN WHICH THE COMBINATION OF CONCEPTUAL CHANGE QUESTIONING WITH CHALLENGING TASKS LED TO SUBSTANTIAL GAINS FOR LOW-PERFORMING STUDENTS ACROSS SIX PRIMARY SCHOOLS ON STANDARDISED TESTS COMPARED WITH EDUCATION DEPARTMENT EXPECTATIONS ( $d = 0.7$ ). <https://doi.org/10.37626/GA9783959871129.0.55> KLYMCHUK, SERGIY; WILSON, DAVID: INTEGRATING PEN-ENABLED TABLET PCs IN TEACHING ENGINEERING MATHEMATICS. PP 293 – 298 THE PAPER ANALYSES THE ATTITUDES AND EXPERIENCES OF TWO UNIVERSITY LECTURERS INVOLVED IN INTEGRATING PEN-ENABLED TABLET PCs (PENTPCs) IN TEACHING ENGINEERING MATHEMATICS. THE FIRST LECTURER HAS AN ENGINEERING BACKGROUND AND TEACHES AN ADVANCED ENGINEERING MATHEMATICS COURSE (YEAR FOUR). THE SECOND LECTURER HAS A MATHEMATICS BACKGROUND AND TEACHES A SECOND YEAR ENGINEERING MATHEMATICS COURSE. TWO ROUNDS OF INTERVIEWS WITH THE LECTURERS ON USING PENTPCs WERE CONDUCTED IN 2015 AND 2019. ANALYSIS OF THESE INTERVIEWS SUGGESTS THAT, FOR THE LECTURER IN MATHEMATICAL DISCIPLINES, A KEY FACTOR IN THEIR INITIAL ADOPTION OF PENTPC TECHNOLOGY MAY BE THEIR PERCEPTION OF THE USEFULNESS OF THE TECHNOLOGY IN ENHANCING DELIVERY WITHIN THE CONTEXT OF EXISTING PEDAGOGICAL APPROACHES IN A CLASSROOM/LECTURE SETTING. <https://doi.org/10.37626/GA9783959871129.0.56> KREVISKY, STEVE: USING SPORTS DATA IN STATISTICS AND MATH CLASSES: AN OVERVIEW AND UPDATE. PP 299 – 300 SPORTS DATA CAN BE A VERY GOOD WAY TO MOTIVATE STUDENTS, IN BOTH STATISTICS AND MATH CLASSES. BACKGROUND TO THIS USAGE WILL BE DISCUSSED, ALONG WITH SOME NEW IDEAS ON HOW TO EMPLOY THIS IN THE CLASSROOM.

<https://doi.org/10.37626/GA9783959871129.0.57> KUSAKA, SATOSHI: ANALYSIS OF THE CHARACTERISTICS OF MOZAMBICAN PRIMARY MATHEMATICS TEXTBOOKS COMPARED WITH JAPANESE TEXTBOOKS FOCUSING ON TASKS AND PROBLEMS RELATED TO THE REAL WORLD. PP 301 – 305 THIS STUDY AIMS TO CLARIFY THE PERTINENT CHARACTERISTICS OF MOZAMBICAN PRIMARY MATHEMATICS TEXTBOOKS FROM A SOCIOCULTURAL PERSPECTIVE (IN COMPARISON TO JAPANESE ONES) BY FOCUSING ON HOW THEY TREAT ‘REAL-WORLD’ MATHEMATICS. THE FOLLOWING FOUR PERSPECTIVES ARE DISCUSSED: (1) PROPORTION OF THE TASKS RELATED TO THE REAL WORLD VIA THE INTRODUCTION OF NEW LEARNING CONTENT (2) PROPORTION OF PROBLEM SOLVING EXERCISES RELATED TO THE REAL WORLD (3) CATEGORIZATION OF THE SITUATION OF THE TASKS AND PROBLEMS RELATED TO THE REAL WORLD (4) APPEARANCE OF SOCIALLY OPEN-ENDED PROBLEMS AND THEIR CONTENT. AS A RESULT, WE FOUND THAT THERE ARE FEW PROBLEMS WHICH ARE RELATED DIRECTLY TO THE REAL WORLD IN THE MOZAMBICAN PRIMARY MATHEMATICS TEXTBOOKS. THE CONTENT OF THE PROBLEMS RELATED TO THE REAL WORLD ARE ABOUT THE TAX SYSTEM AND SALARIES, WHICH MEANS STUDENTS ARE GIVEN OPPORTUNITIES TO VIEW AND THINK MATHEMATICALLY ABOUT THEIR SOCIAL SYSTEM RIGHT FROM THE PRIMARY SCHOOL AGE. <https://doi.org/10.37626/GA9783959871129.0.58> LASKASKY, KATIE; ET AL: INNOVATIVE PROBLEM SOLVING: WHAT HAPPENS WHEN MATH EDUCATION, BUSINESS, AND ENGINEERING PERSPECTIVES INTERACT. PP 306 – 311 FOR YEARS, PRACTITIONERS AND RESEARCHERS HAVE ATTEMPTED TO SOLVE THE SAME MATH EDUCATION PROBLEM. THOUGH THE APPROACH VARIES, THEY USE OUTDATED PROCESSES AND SEE FEW RESULTS. THUS, THERE IS AN OVERALL NEED TO USE NEW STRATEGIES. THIS PAPER EXPLORES HOW ONE K-12 SCHOOL DISTRICT USES AN INNOVATIVE, COLLABORATIVE, PROBLEM SOLVING PROCESS TO UNDERSTAND ITS MATH LEARNING PROBLEM. STAKEHOLDERS ENGAGE DIVERSE VIEWPOINTS, USE RESEARCH-BASED RECOMMENDATIONS TO DEFINE SUCCESS IN HOW STUDENTS LEARN MATHEMATICS, DEVELOP CONTEXT-SENSITIVE SOLUTION OPTIONS, AND EVALUATE THOSE OPTIONS’ ADAPTABILITY. THIS INNOVATIVE PROBLEM SOLVING PROCESS’ FOUNDATION EMERGES FROM RESEARCH AND BEST PRACTICE RECOMMENDATIONS FOUND AT THE INTERSECTION OF MULTIPLE DISCIPLINES: MATH EDUCATION, BUSINESS, SYSTEMS ENGINEERING, AND IMPLEMENTATION SCIENCE. THE CURRENT OBSERVATION AND INTERVIEW DATA INDICATE THAT STAKEHOLDERS FEEL A SENSE OF OWNERSHIP, EMBRACE VARIABILITY IN PROBLEM SOLVING, AND UNDERSTAND HOW TO COLLECT DATA ABOUT STUDENTS’ MATH LEARNING. <https://doi.org/10.37626/GA9783959871129.0.59> LEMIEUX, COLLETTE; ROETTGER, ERIC: STUDENTS’

REASONING DURING A CALCULUS TWO-STAGE EXAM. pp 312 – 317 FOR A TWO-STAGE EXAM, STUDENTS FIRST WRITE THEIR EXAM INDIVIDUALLY AND THEN REPEAT IT IN A SMALL GROUP. THIS STUDY ANALYZED THE DISCUSSIONS THAT STUDENTS HAD DURING THE GROUP STAGE OF A TWO-STAGE EXAM IN A FIRST-YEAR CALCULUS COURSE IN ORDER TO INVESTIGATE STUDENTS' REASONING AND HOW THEY ARRIVED AT THEIR ANSWERS. DATA, CONSISTING OF 14 TRANSCRIPTS OF AUDIO-RECORDINGS OF THE STUDENTS' DISCUSSIONS, WERE ANALYZED QUALITATIVELY, GUIDED BY LITHNER'S (2007) CONCEPTUAL FRAMEWORK ON MATHEMATICAL REASONING. THE RESULTS SUGGEST THAT, THOUGH STUDENTS PRIMARILY USED IMITATIVE REASONING OR ROTE LEARNING TO ANSWER MANY QUESTIONS, THEY ALSO DEMONSTRATED CREATIVE REASONING BY USING A NOVEL & PLAUSIBLE APPROACH AND GROUNDING THEIR REASONING IN MATHEMATICS. FURTHER, THOUGH THE IMITATIVE REASONING RELIED PRIMARILY ON REMEMBERING A THEOREM OR TERM IN CALCULUS, CREATIVE REASONING WAS DEMONSTRATED IN MULTIPLE WAYS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.60](https://doi.org/10.37626/GA9783959871129.0.60)

CORREDOR, OLGA LEÓN; ET AL: INTEGRATING TECHNOLOGY AND DIDACTIC RESOURCES FOR ENHANCING LEARNING PROCESSES. AN EXPLORATORY STUDY. pp 318 – 323 SOME LIMITATIONS THAT AFFECT THE LEARNING OF MATHEMATICS ARE RELATED TO TWO DYSFUNCTIONAL ISSUES: LACK OF ACKNOWLEDGMENT OF STUDENTS' DIFFERENCES IN THE DIDACTIC DESIGNS AND OF THE STUDENTS' AWARENESS ABOUT THEIR LEARNING SKILLS. ACCESSIBLE AND AFFECTIVE DIDACTIC DESIGNS AIM TO OVERCOME SUCH DYSFUNCTIONAL ISSUES. IN THIS DIRECTION, THE DOCUMENT PRESENTS THREE CONTRIBUTIONS: FIRST, THE EXPLORATION OF TECHNOLOGICAL RELATIONSHIPS THAT FOSTER COGNITIVE CONVERGENCE BETWEEN THE STUDENT AND TOOLS; SECOND, A REVISION OF HYPOTHESES THAT GIVE SUPPORT TO ACCESSIBLE AND AFFECTIVE DIDACTIC DESIGNS; AND THIRD, THE DOCUMENTATION OF THE LEARNING TRAJECTORIES THAT SOME DIVERSE COLOMBIAN POPULATIONS MADE WHILE THEY WERE PLAYING THE GAME CALLED THE JUMPER. THE METHODOLOGIES USED IN THE RESEARCH WERE DESIGN SCIENCE RESEARCH AND TEACHING EXPERIMENTS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.61](https://doi.org/10.37626/GA9783959871129.0.61)

LIANG, SU: ENQUIRY-BASED LEARNING IN COLLEGE MATHEMATICS EDUCATION: THEORY AND PRACTICE. pp 324 – 329 THE PRACTICE OF INQUIRY-BASED LEARNING (IBL) HAS A VERY LONG HISTORY. IN THE WESTERN WORLD, THE ANCIENT GREEK PHILOSOPHER, SOCRATES (469 – 399 B.C.) HAD UTILIZED IBL TO ENGAGE HIS INTERLOCUTORS IN DIALOGUE FOR DISCOVERING BASIC TRUTH AND PRINCIPLES. IN THE EASTERN WORLD, THE ANCIENT CHINESE PHILOSOPHER AND EDUCATOR CONFUCIUS (551 -479 B.C.) HAD ALSO RAISED THE IDEA OF IBL APPROACH FOR TEACHING AND LEARNING. CONFUCIUS HAD SAID: "I HEAR, I FORGET; I SEE, I REMEMBER; I DO, I UNDERSTAND". ACTIVE LEARNING IS THE ESSENCE OF IBL WAY OF TEACHING. THE IBL DISCUSSED IN THE PAPER IS GUIDED IBL. IN THE RESEARCH LITERATURE, MANY RESEARCH SHOWED EVIDENCE THAT GUIDED IBL PRODUCED BETTER LEARNING OUTCOMES COMPARING TO PURE LECTURE APPROACH. IN RECENT YEARS, PROMOTING IBL IN THE FIELD OF EDUCATION BECOMES A TREND, BECAUSE RESEARCHERS BELIEVE THAT THE FEATURES OF IBL CAN FULFILL THE 21ST CENTURY EDUCATION THROUGH CULTIVATING STUDENTS' CRITICAL AND CREATIVE THINKING, NURTURING INQUIRY MIND OF PROBLEM-SOLVING, AND PREPARING LIFE-LONG LEARNERS, FOR OUR SOCIETY. HOWEVER, IN REALITY, THE TRADITIONAL WAY OF TEACHING – LECTURE IS STILL DOMINATED AT SCHOOL TEACHING. WHY HAS IBL BEEN PROMOTED IN THE EDUCATIONAL RESEARCH BUT MOST TEACHERS STILL NEVER EMPLOY IT IN THEIR TEACHING PRACTICE YET? IN THIS PAPER, I WILL DISCUSS THE CHALLENGING WE ARE FACING AND PROPOSE SOME IDEAS FOR IBL IMPLEMENTATION. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.62](https://doi.org/10.37626/GA9783959871129.0.62)

LIPOVEC, ALENKA; FERME, JASMINA: SOME FACTORS INFLUENCING EFFECTIVENESS OF MATHEMATICS HOMEWORK. pp 330 – 335 EMPIRICAL RESEARCH, WHICH EXAMINES THE RELATIONSHIP BETWEEN MATHEMATICAL ACHIEVEMENT OF ELEMENTARY SCHOOL STUDENTS AND MATHEMATICS HOMEWORK ASSIGNMENTS, GIVES INCONSISTENT RESULTS. WE PRESENT THE RESULTS OF THE CROSSCULTURAL STUDY (N = 1061) WITH 12-15 YEARS OLD STUDENTS FROM SLOVENIA, CROATIA AND SLOVAKIA. THE RESULTS SHOW THAT HOMEWORK FREQUENCY, TEACHER RESPONSES, AND THE SUPPORT OF PARENTS ARE NOT RELATED TO STUDENTS' MATHEMATICS ACHIEVEMENTS; BUT PARENTAL CONTROL AND THE TIME SPENT DOING HOMEWORK ARE NEGATIVELY RELATED TO THOSE ACHIEVEMENTS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.63](https://doi.org/10.37626/GA9783959871129.0.63)

LOUISIS, MICHAEL: RECOMMENDATIONS FOR INSTRUCTIONAL DESIGNERS AND TEXTBOOK WRITERS CONCERNING THE CORRECTION OF SIGNIFICANT AND PERSISTENT ERRORS IN ARITHMETIC AND ALGEBRA. pp 336 – 342 AN ERROR ANALYSIS OF THE 200 ENGLISH AND 150 GREEK LEARNERS' TESTS IN ARITHMETIC AND ALGEBRA WAS ACCOMPLISHED. THOSE TESTS STEMMED FROM THE KASSEL PROJECT. FOLLOWING THIS ERROR ANALYSIS, SPECIFIC RECOMMENDATIONS ARE PRESENTED IN EACH DOMAIN OF ARITHMETIC AND ALGEBRA THAT SHOULD BE TAKEN INTO ACCOUNT BY INSTRUCTIONAL DESIGNERS AND TEXTBOOK WRITERS. THESE RECOMMENDATIONS WERE FOUNDED ON TERMS OF PSYCHOLOGY AND COGNITIVE SCIENCE AS APPLIED TO INFORMATION-PROCESSING. THE STUDY HAS SHOWN THE EDUCATIONAL MEDIA (TEXTBOOKS ETC.), AS BEING RESPONSIBLE FOR THE EMERGENCE AND PERSISTENCE OF THESE ERRORS IN THE LEARNERS' MINDS TOO, SINCE INSTRUCTION IS MOSTLY BASED ON THE USE OF THOSE MEDIA. KEY WORDS: ERROR ANALYSIS, KASSEL PROJECT, TEXTBOOKS, EDUCATIONAL MEDIA, RECOMMENDATIONS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.64](https://doi.org/10.37626/GA9783959871129.0.64)

MARCHAND, PATRICIA: INTERFACE BETWEEN THEORETICAL GUIDELINES AND CLASSROOM PRACTICES TO CREATE ACTIVITIES THAT ENHANCE THE DEVELOPMENT OF SPATIAL REASONING IN ELEMENTARY SCHOOL. pp 343 – 346 THE SPATIAL REASONING HAS BEEN IDENTIFIED BY MANY RESEARCHERS AS BEING LINKED TO POSITIVE MATHEMATICAL PERFORMANCE AND, THEREFORE, IS A DETERMINING FACTOR IN MATHEMATICS AND SCIENTIFIC SUCCESS AT ELEMENTARY, SECONDARY AND UPPER LEVELS (DAVIS & THE SPATIAL REASONING STUDY GROUP, 2015). ALSO, SPATIAL REASONING HAS BEEN PROVEN TO BE A TYPE OF REASONING THAT IS MALLEABLE AND CAN BE DEVELOP, IMPLYING THAT TEACHERS ARE EMPOWERED IN THIS DEVELOPMENT (MOSS, BRUCE, CASWELL, FLYNN & HAWES, 2016;

WAI, LUBINSKI & BENBOW, 2009; MARCHAND, 2009A; BERTHELOT & SALIN, 1992). THE GOAL OF THIS WORKSHOP IS TO EXPOSE THEORETICAL GUIDELINES TO ANALYSE AND TO CREATE CLASSROOM ACTIVITIES FOCUSING ON DEVELOPING SPATIAL REASONING IN ELEMENTARY SCHOOL. THE INTERFACE BETWEEN THESE THEORETICAL GUIDELINES AND CLASSROOMS ACTIVITIES ALLOWS US TO UNFOLD NEW IDEAS TO DEAL WITH SPATIAL REASONING AT THE ELEMENTARY LEVEL.  
[HTTPS://DOI.ORG/10.37626/GA9783959871129.0.65](https://doi.org/10.37626/GA9783959871129.0.65) MARKUN, URSKA; KOS, JASNA: RESEARCH WORK IN A SECONDARY SCHOOL CLASSROOM: HOW WELL ARE TEACHERS EQUIPPED FOR IT? PP 347 – 352 A UNIVERSITY DEGREE IS NOT ENOUGH IN ITSELF TO EQUIP A MATHEMATICS TEACHER FOR SUCCESSFUL SECONDARY SCHOOL-TEACHING IN THE LONGER TERM. WITHOUT CONTINUOUS TRAINING AND CAREER-LONG LEARNING, A TEACHER WILL NOT BE ABLE TO PROVIDE ADEQUATE SUPPORT FOR STUDENTS IN ACTIVITIES SUCH AS EXTENDED ESSAYS OR EXPLORATIONS, BOTH OF WHICH ARE COMPULSORY COMPONENTS OF THE IB PROGRAMME. IN THIS PAPER, WE PRESENT SOME EXAMPLES OF SUCH WORK BY IB STUDENTS AT OUR SCHOOL. IN ADDITION, SOME SLOVENIAN SECONDARY SCHOOL STUDENTS REGULARLY PARTICIPATE IN A NATIONAL RESEARCH COMPETITION FOR WHICH THEY MUST SUBMIT PROJECT-BASED WORK IN VARIOUS FIELDS. THE PRESENT ARTICLE DESCRIBES HOW UNIVERSITY DEPARTMENTS CO-OPERATED WITH OUR SECONDARY SCHOOL IN THE COURSE OF SUCH RESEARCH. EXAMPLES OF RESEARCH CARRIED OUT BY A NUMBER OF 16-YEAR-OLD STUDENTS AT OUR SCHOOL ARE ALSO PRESENTED HERE.  
[HTTPS://DOI.ORG/10.37626/GA9783959871129.0.66](https://doi.org/10.37626/GA9783959871129.0.66) MART, MALGORZATA: THE IMPACT OF TEACHER SELF-EFFICACY ON THE LEVEL OF IMPLEMENTATION OF GRAPHING TECHNOLOGY IN TEACHING FACTORING QUADRATIC FUNCTIONS IN INTRODUCTORY ALGEBRA. PP 353 – 357 THE PURPOSE OF THE STUDY WAS TO DETERMINE WHETHER THERE IS A RELATIONSHIP BETWEEN SELF-EFFICACY OF GLOBAL AND LOCAL ALGEBRA TEACHERS AND THEIR LEVEL OF INCORPORATING TECHNOLOGY IN TEACHING FACTORING QUADRATIC FUNCTIONS TO INTRODUCTORY ALGEBRA STUDENTS. THE PARTICIPANTS (54 MATHEMATICS EDUCATORS FROM 15 COUNTRIES AND FIVE CONTINENTS) REPLIED TO THE UVGIA SURVEY INSTRUMENT. QUANTITATIVE ANALYSIS OF DATA BROUGHT THE CONCLUSION THAT THERE IS A STRONG POSITIVE RELATIONSHIP BETWEEN THE LEVEL OF SELF-EFFICACY OF TEACHERS AND THEIR LEVEL OF IMPLEMENTATIONS OF TECHNOLOGY REGARDLESS OF COUNTRY OF ORIGIN.  
[HTTPS://DOI.ORG/10.37626/GA9783959871129.0.67](https://doi.org/10.37626/GA9783959871129.0.67) MASON, RALPH; ET AL: FOUNDATIONAL EXPERIENCES AS A CURRICULUM DESIGN PRINCIPLE FOR SECONDARY MATHEMATICS. PP 358 – 363 STUDENTS MUST MAKE SENSE OF THE MATHEMATICS THEY ARE LEARNING, IF THEY ARE TO UNDERSTAND IT. WHEN STUDENTS ARE ENCOUNTERING A MATHEMATICS TOPIC PRIMARILY THROUGH THAT TOPIC'S MATHEMATICAL FORMS—ITS SYMBOLS, TERMINOLOGY, DEFINITIONS, OPERATIONS, AND ALGORITHMS—THE RICHNESS, POTENCY, AND COMPLETENESS OF THEIR UNDERSTANDING WILL DEPEND ON THEIR PRIOR, PRE-FORMAL EXPERIENCES WITH THAT TOPIC. FOUNDATIONAL EXPERIENCES ACTIVITIES ENABLE STUDENTS TO CONSTRUCT IMAGES, PATTERNS, AND IDEAS—IN A WORD, MEMORIES—THAT WILL ENABLE THEM TO SEE THE SENSIBILITY OF THE TOPIC'S MATHEMATICAL FORMS WHEN THEY LEARN THEM. WE INVITE PARTICIPANTS TO EXPLORE SOME EXAMPLES OF INSTRUCTIONAL ACTIVITIES DESIGNED TO PROVIDE FOUNDATIONAL EXPERIENCES FOR THE MATHEMATICS OF POWERS, FROM POWER LAWS THROUGH GEOMETRIC SEQUENCES TO EXPONENTIAL FUNCTIONS. WITH THESE EXAMPLES, PARTICIPANTS WILL CONSIDER THESE QUESTIONS: HOW CAN FOUNDATIONAL EXPERIENCES CONTRIBUTE TO STUDENTS' UNDERSTANDINGS OF THE MATH BEHIND THE TOPIC'S FORMAL CONTENT? WHAT ARE THE QUALITIES THAT WE SHOULD INVEST WHEN DESIGNING FOUNDATIONAL EXPERIENCE ACTIVITIES?  
[HTTPS://DOI.ORG/10.37626/GA9783959871129.0.68](https://doi.org/10.37626/GA9783959871129.0.68) MAY, BERNIE (DOV): ENGAGE STUDENTS MORE HOPSCOTCH MATHE HAS STUDENTS JUMPING FOR JOY. PP 364 – 367 THE GOAL WAS TO CREATE A SYSTEM TO TEACH CHILDREN DEEP THINKING SKILLS, AS WELL AS PROBLEM SOLVING SKILLS WHICH THEY COULD LATER USE IN TOMORROW'S INNOVATION ECONOMY. THE BY-PRODUCT IS THEY LEARN THE TIMES TABLE. WE COVER MORE IN LESS TIME...UNDER 5 HOURS, WE GO UP TO 20x20, AND INTRODUCE THE CHILDREN TO COMPLEX ALGEBRAIC EQUATIONS, TOO. GUESS WHAT? THEY LOVE IT – AND ASK FOR MORE! THE TIMES TABLE REPRESENTS THE PROBLEM TO BE SOLVED. EACH INTERSECTION REPRESENTS A SMALLER ASPECT OF THE PROBLEM. THEY LEARN VARIOUS TECHNIQUES. NO DUMB SING-SONG MELODIES. THEY BUILD ON WHAT THEY KNOW. WE DO NOT GO LINEARLY THROUGH THE TABLE. WE JUMP AROUND...AND COVER WHATEVER WE CAN. WHEN WE ARE THROUGH I SHOW THEM THAT IF THEY ONLY KNEW  $7 \times 4 = 28$ , THEY HAVE THE PROBLEM SOLVING SKILLS WHERE THEY CAN SOLVE THE WHOLE TABLE. THE IDEA BEHIND KINESTETIC MATH IS TO GET INTO THEIR WORLD, AND REACH THEM AT THEIR LEVEL. CHILDREN LIKE TO RUN, JUMP, COLOUR AND MOVE AROUND – SO DO WE. WE USE OUR FINGERS, OUR KNUCKLES, AND OUR LEGS TO LEARN THE TIMES TABLE. THIS PAPER COVERS A SMALL SECTION OF THE PROGRAM, MAGIC SQUARES AND HOPSCOTCH MATH, AS AN INTRODUCTION TO A DIFFERENT KIND OF THINKING AND HOW INNOVATIVE THINKING CAN BE APPLIED TO TEACHING. I INTRODUCE THE PROGRAM WITH A 10x10 GRID REPRESENTING THE TIMES TABLE. EVERY TIME WE SOLVE ONE OF THE BLOCKS ON THE TABLE, THEY GET TO COLOR THE BLOCK HOWEVER THEY WANT.  
[HTTPS://DOI.ORG/10.37626/GA9783959871129.0.69](https://doi.org/10.37626/GA9783959871129.0.69) MENZ, PETRA; MULBERRY, NICOLA: OPEN SOURCE DIFFERENTIAL AND INTEGRAL CALCULUS MATERIAL DEVELOPMENT TO SUPPORT STUDENT ACCESSIBILITY AND LEARNING. PP 368 – 373 EDUCATIONAL RESOURCES IN MATHEMATICS ARE AN IMPORTANT ASPECT OF THE TEACHING AND LEARNING LANDSCAPE. MOREOVER, RESOURCES HAVE COME A LONG WAY FROM THE SPOKEN WORD WITH SUCH INVENTIONS AS PAPER AND THE COMPUTER TO THE POINT WHERE THERE IS NOW AN INFRASTRUCTURE AROUND OPEN EDUCATIONAL RESOURCES (OER) THAT HAS MATURED INTO VIABLE ALTERNATIVES TO TRADITIONAL RESOURCES. THE NEWFOUND PREVALENCE OF THESE MATERIALS PROVIDES OPPORTUNITIES TO CUSTOMIZE OER TO THE SPECIFIC NEEDS OF STUDENTS AND INSTITUTIONS. WE DESIGNED OPEN SOURCE MATERIAL FOR THE SOCIAL

SCIENCE STRAND OF DIFFERENTIAL AND INTEGRAL CALCULUS BY ADOPTING AN OPEN SOURCE TEXTBOOK AND ADAPTING IT FOR OUR NEEDS. ALONG WITH THE COURSE NOTES, WE DEVELOPED LECTURE NOTES, STUDENT NOTES BASED ON THE CORNELL NOTE-TAKING SYSTEM, AND ASSIGNMENTS WITH SOLUTIONS. STUDENTS ARE APPRECIATIVE OF FREE MATERIAL, BUT MOREOVER, THE COHESIVENESS AND INTERCONNECTIVITY AMONG THE VARIOUS COURSE MATERIALS PROVIDES FOR A SMOOTHER LEARNING JOURNEY THROUGH OUR COURSES. THIS PAPER PRESENTS OUR PHILOSOPHY, AN OVERVIEW OF OUR OPEN SOURCE MATERIAL, AND THE OPERATION OF BOTH COURSES. <https://doi.org/10.37626/GA9783959871129.0.70> MICHELSEN, CLAUS: THE MACAS SYMPOSIUMS 2005 – 2019. MATHEMATICS EDUCATION IN AN INTERDISCIPLINARY CONTEXT. PP 374 – 379 THE SYMPOSIUM SERIES MATHEMATICS AND ITS CONNECTIONS TO THE ARTS AND SCIENCES (MACAS) HAS BEEN HELD SINCE 2005. THE VISION WHICH THE MACAS INITIATIVE IS BASED UPON IS TO DEVELOP A HUMANISTIC APPROACH TO EDUCATION THAT COMBINES VARIOUS DISCIPLINES IN A SINGLE CURRICULUM. ACCORDING TO THIS VISION THE AIM IS TO EDUCATE STUDENTS BY ENABLING THEM TO PURSUE DIVERSE FIELDS OF RESEARCH, WHILE AT THE SAME TIME EXPLORING THE AESTHETIC AND SCIENTIFIC CONNECTIONS BETWEEN THE ARTS AND SCIENCE. IN VIEW OF THE CHALLENGES OF THE 21ST CENTURY, A MODERN APPROACH TO EDUCATION WITH A FOCUS ON MULTI- AND INTERDISCIPLINARITY IS MORE IMPORTANT THAN EVER. FIVE MACAS SYMPOSIUMS HAVE BEEN HELD SINCE 2005, AND THE PROCEEDINGS OF THE SYMPOSIUMS PROVIDE AN INSIGHT INTO IDEAS, EXPERIENCES, CONCEPTUAL FRAMEWORKS, AND THEORIES TO CONNECT MATHEMATICS EDUCATION TO THE ARTS AND SCIENCES. BASED ON THE SYMPOSIUMS PROCEEDINGS WE PROVIDE AN OVERVIEW OF FIVE MAIN THEMES ADDRESSED AT THE MACAS SYMPOSIUMS (i) MATHEMATICS AND SCIENCE (ii) MATHEMATICS AND ART (iii) MATHEMATICS AND TECHNOLOGY, (iv) MATHEMATICS AND LITERATURE, AND (v) EDUCATIONAL PERSPECTIVES ON INTERDISCIPLINARITY. THE OVERVIEW HIGHLIGHTS THE NEED FOR JOINT EMPIRICAL INVESTIGATIONS THAT OPERATIONALIZE, MODEL AND STUDY THE RICH IDEAS PRESENTED IN AT THE SYMPOSIUMS. <https://doi.org/10.37626/GA9783959871129.0.71> MIHESON, O'CONNOR, MARGUERITE K.: TEACHING MATHEMATICS THROUGH HISTORIC ENVIRONMENT. A TIME-TRAVEL GROUNDED PEDAGOGY. PP 380 – 385 MATHEMATICS HAS BEEN USED BY GENERATIONS TO MAKE IMPORTANT DECISIONS FOR A LONG PERIOD OF TIME. HISTORY IS LITTERED WITH PROBLEM SOLVING EVENTS WHICH ARE RESULTS OF MATHEMATIZATION OF TASKS BASED ON AVAILABLE TOOLS IN ANY GIVEN GENERATION. WHILE HISTORY OF MATHEMATICS FOCUSES ON WHAT EACH CULTURE CONTRIBUTED TO PRESENT DAY CONVENTIONAL MATHEMATICS AS TAUGHT IN SCHOOLS AS A SUBJECT, MATHEMATICS IN A HISTORIC ENVIRONMENT FOCUSES ON IDENTIFYING MATHEMATICAL THINKING THAT EXISTS IN ALL HISTORICAL EVENTS. HISTORICAL EVENTS WHEN ENACTED THROUGH THE TIME TRAVEL APPROACH LEARNERS GET THE OPPORTUNITY TO RELIVE PAST EVENTS IN THE PRESENT CONTEXT. TEACHING MATHEMATICS IN HISTORIC ENVIRONMENT USES THE TIME TRAVEL EVENTS THAT ARE PRACTISED BY BRIDGING AGES INTERNATIONAL, TO PROVIDE A REFLECTIVE MEANINGFUL CONCEPTUALIZATION OF MATHEMATICS IS A LIVING SUBJECT. THE STRATEGY ILLUMINATES THE CENTRALITY OF MATHEMATICAL THINKING IN ALL HISTORICAL EVENTS. THIS PAPER SHARES FINDINGS FROM A STUDY CARRIED OUT ON THE EFFECTIVENESS OF THIS APPROACH FOR TEACHING MATHEMATICS AND PROVIDES AN OPPORTUNITY TO DISCUSS THE APPROACH AS A VIABLE PEDAGOGIC STRATEGY THAT CAN BE REPLICATED ACROSS THE CURRICULUM <https://doi.org/10.37626/GA9783959871129.0.72> MISSEN, JENNY: RESEARCHING AND IMPLEMENTING IN THE MATHEMATICS CLASSROOM AUSTRALIAN CURRICULUM GENERAL CAPABILITIES. PP 386 – 391 THE AUSTRALIAN CURRICULUM (AC) PROVIDES TEACHERS WITH A GREAT AMOUNT OF DETAIL IN EACH CURRICULUM AREA. IN ADDITION TO TEACHING THESE CURRICULA, THE AC REQUIRES INCORPORATION OF CROSS-CURRICULUM PRIORITIES AND GENERAL CAPABILITIES. THIS PAPER DOCUMENTS THE WORK DONE ON AN ACTION RESEARCH PROJECT CONSIDERING WAYS IN WHICH THE GENERAL CAPABILITIES (GCs) OF THE AUSTRALIAN CURRICULUM COULD BE INCORPORATED INTO TEACHING MATHEMATICS AND THE DIFFICULTIES I FACED AS A TEACHER RESEARCHING DURING THE TEACHING TERM. <https://doi.org/10.37626/GA9783959871129.0.73> MORGE, SHELBY: ADDRESSING TEACHERS' CULTURALLY RESPONSIVE TEACHING BELIEFS THROUGH COURSE ACTIVITIES. PP 392 – 397 MAKING DATA-BASED DECISIONS ABOUT COURSE CONTENT IS A DIFFICULT PROCESS FOR TEACHER EDUCATORS. THIS DIFFICULTY IS AMPLIFIED WHEN CONSIDERING COMPLEX ISSUES FOCUSED ON DIVERSITY. IN ORDER TO UNDERSTAND AND ADDRESS PRE- AND IN-SERVICE TEACHERS' CULTURALLY RESPONSIVE TEACHING BELIEFS, THE CULTURALLY RESPONSIVE TEACHING OUTCOME EXPECTANCY SCALE (SIWATU, 2007) WAS ADMINISTERED DURING GRADUATE AND UNDERGRADUATE COURSES IN MATHEMATICS EDUCATION AT TWO SOUTHEASTERN US UNIVERSITIES. FROM THE SURVEY RESULTS INSTRUCTORS IDENTIFIED ITEMS WITH HIGH AND LOW MEANS (ON A 100 POINT SCALE). THE LOWEST ITEMS PROVIDED A BASIS FOR CONSTRUCTING FUTURE COURSE ACTIVITIES. IN THIS PAPER WE SHARE THE EXPECTANCY SCALE RESULTS AND COURSE ACTIVITIES THAT WERE IMPLEMENTED. WE ALSO DISCUSS OPPORTUNITIES FOR IMPROVING THE CULTURALLY RELEVANT PRACTICES AND ACTIVITIES IN OUR COURSES IN ORDER TO ENSURE THE TRANSFER TO CLASSROOM PRACTICE. <https://doi.org/10.37626/GA9783959871129.0.74> MORSKA, JANINA: FROM THE PURPOSE OF THE LESSON TO SUCCESS. PP 398 – 400 THIS PAPER DEALS WITH EFFICIENCY IN TEACHING. THE PURPOSE OF THE LESSON AND THE CRITERION OF SUCCESS ARE COMPLEX ELEMENTS IN THE DIDACTIC PROCESS. BETWEEN THESE ELEMENTS ARE THEORY AND PRACTICE, VARIOUS FORMS OF WORK, FEEDBACK AND STUDENT SELF – EVALUATION. I WOULD LIKE TO SHARE MY PROFESSIONAL EXPERIENCE AS AN APPRENTICESHIP TEACHER, AS WELL AS A DEPUTY HEAD TEACHER (VICE-DIRECTOR) OBSERVING THE WORK OF OTHER TEACHERS IN FORMATIVE ASSESSMENT. <https://doi.org/10.37626/GA9783959871129.0.75> MOSCARDINI, LIO; ET AL: COLLABORATING ACROSS THE POND: COGNITIVELY GUIDED INSTRUCTION PROJECT. PP 401 – 405 THIS PAPER DESCRIBES A PRIMARY-SCHOOL (AGES 5-11) PROJECT IMPLEMENTED IN SCOTLAND, BASED ON THE UNITED STATES RESEARCH FROM COGNITIVELY

GUIDED INSTRUCTION (CGI), AND AS ENVISIONED BY DR. LIO MOSCARDINI. THREE SCHOOLS, TWO PUBLIC AND ONE PRIVATE, PARTICIPATED IN THIS TWO-YEAR LONG INITIAL STUDY THAT FOCUSED ON HELPING TEACHERS TO UNDERSTAND THE DEVELOPMENTAL STAGES PUPILS NATURALLY PROGRESS THROUGH IN ORDER TO UNDERSTAND THE MATHEMATICS FOR THEIR CLASS LEVEL AS DEFINED BY THE SCOTTISH GOVERNMENT. THIS PROJECT PROVIDES EVIDENCE THAT A RISE IN ATTAINMENT CAN OCCUR BY FOCUSING ON TEACHERS' KNOWLEDGE, PEDAGOGY, AND PEDAGOGICAL CONTENT KNOWLEDGE IN RELATION TO MATHEMATICS RATHER THAN BY FOCUSING ON ATTAINMENT ITSELF. ADDITIONALLY, THIS PROJECT ADDRESSES THE TEACHING AND LEARNING OF A DIVERSE GROUP OF STUDENTS, I.E. INCLUSION, LOW SOCIO-ECONOMICS. <https://doi.org/10.37626/GA9783959871129.0.76> MOVSHOVITZ-HADAR, NITSA; ET AL: BRIDGING BETWEEN SCHOOL MATHEMATICS AND CONTEMPORARY MATHEMATICS: TURNING A DREAM INTO REALITY. PP 406 – 411 IN MANY COUNTRIES, SCHOOL MATHEMATICS CURRICULUM DOES NOT GO BEYOND THE 18TH CENTURY MATHEMATICS. ANY SOLUTION FOR BRIDGING THIS GAP MUST CONSIDER STUDENTS' LIMITED BACKGROUND, AS WELL AS TEACHERS' TIME CONSTRAINTS. OUR 'BRIDGE' CONSISTS OF PERIODICALLY INTERWEAVING MATHEMATICS-NEWS SNAPSHOTS (MNSs), I.E., SHORT DESCRIPTIVE PRESENTATIONS OF RECENT MATHEMATICAL RESULTS, THROUGHOUT THE TEACHING OF THE ORDINARY MATH CURRICULUM DURING THE THREE YEARS OF SENIOR HIGH SCHOOL. MORE THAN 20 MNSs ARE ALREADY AVAILABLE (SEE <https://MNS.CO.IL>). OUR TWO-PART WORKSHOP IS AIMED AT SHARING OUR SOLUTION. THIS WILL INCLUDE A DISCUSSION OF ITS UNDERLYING PRINCIPLES, A REVERSE ENGINEERING ANALYSIS OF SAMPLE MNSs VIS-À-VIS THE MNS AUTHORIZING GUIDELINES, AN OVERVIEW OF THREE TEACHER PREPARATION MODELS, AND RESULTS OF OUR IMPLEMENTATION FOLLOW-UP STUDIES. FINALLY, IN THE SPIRIT OF THE CONFERENCE, WE'LL INVITE ATTENDEES TO ADOPT OUR SOLUTION, AND POSSIBLY ALSO TO PARTICIPATE IN DEVELOPING MORE MNSs, THUS TURNING OUR DREAM OF BRIDGING THE GAP INTO REALITY. <https://doi.org/10.37626/GA9783959871129.0.77> NARAYANAN, AJAYAGOSH: PEER TUTORING: DEVELOPING AND SUSTAINING EFFECTIVE TEACHING PRACTICES WITH MATHEMATICS TEACHERS IN LESOTHO. PP 412 – 417 THIS PAPER SHOWS HOW A GROUP OF EDUCATORS INITIATED IN-SERVICE WORKSHOPS FOR PRIMARY AND SECONDARY MATHEMATICS TEACHERS SINCE 2012 IN COLLABORATION WITH THE MINISTRY OF EDUCATION AND TRAINING (MoET) IN LESOTHO. THE PRIME FOCUS OF THESE WORKSHOPS WAS TO DEVELOP TEACHERS' CAPACITY BUILDING IN MATHEMATICS THROUGH PEER-SUPPORT. THE PAPER ALSO NARRATES HOW A CHAIN OF THESE WORKSHOPS EVOLVED TO A CAPACITY BUILDING PROGRAM WITH INNOVATIVE APPROACHES IN CLASSROOMS. THESE WORKSHOPS EXPLORED IDEAS ON NUMBERS, SHAPES (THROUGH THE USE OF ORIGAMI) AND PROBLEM SOLVING FOR EFFECTIVE TEACHING/LEARNING OF MATHEMATICS. THE CONCEPT OF PEER TUTORING/LEARNING HAD EMERGED FROM THESE WORKSHOPS AS AN IDEA THAT SUITS LESOTHO EDUCATION SYSTEM. A CAPACITY BUILDING PROGRAM WAS THUS RECOMMENDED FOR THE SUSTAINABILITY OF THESE ACTIVITIES. <https://doi.org/10.37626/GA9783959871129.0.78> NAVARRO ROBLES, MARÍA ESTELA: VARIATION THEORY USED TO MAKE A PERSONALIZED DIAGNOSTIC IN THE LEVEL OF KNOWLEDGE OF FUNDAMENTAL CONCEPTS ABOUT RATIONAL NUMBERS AND THEIR OPERATIONS IN UNDERGRADUATE STUDENTS. PP 418 – 421 THIS LECTURE EXPLAINS HOW THROUGH MARTON VARIATION THEORY WAS DESIGNED AND EVALUATED A TEST ABOUT RATIONAL NUMBERS TO IDENTIFY FOR EACH STUDENT THE SPECIFIC KNOWLEDGE AND SKILLS ABOUT THE THEME TO SOLVE PROBLEMS AND TO MAKE OPERATIONS AND THUS WHICH CONCEPTS THEY NEED TO LEARN OR WHAT SKILLS THEY NEED TO DEVELOP. THE VARIATION THEORY WAS USED IN THE SENSE OF ONE PROBLEM, MULTIPLE CHANGES. THE TEST WAS ANSWERED BY 115 STUDENTS OF 7 GROUPS OF A PRIVATE UNIVERSITY, WHO ARE ENROLLED IN A LEVELING COURSE. FROM THE ANSWERS OF THE STUDENTS IT WAS CHARACTERIZED THE LIVED OBJECT OF LEARNING AND THIS WAS THE START POINT TO CLASSIFY THE CONCEPTUAL OR OPERATIONAL NEEDS OF EACH STUDENT. WITH THE DETAILED RESULTS IT WAS POSSIBLE TO DESIGN A PERSONALIZED ROUTE OF LEARNING. KEY WORDS: RATIONAL NUMBERS, VARIATION THEORY, UNDERGRADUATE STUDENT, PERSONALIZED COURSE <https://doi.org/10.37626/GA9783959871129.0.79> NIESS, MARGARET L.: ONLINE STRATEGIES ENHANCING MATHEMATICS TEACHER KNOWLEDGE FOR THE DIGITAL AGE: DISCOURSE AND CRITICAL REFLECTION. PP 422 – 427 THIS STUDY DESIGNED ONLINE GRADUATE COURSES TO ENRICH INSERVICE MATHEMATICS TEACHERS' TECHNOLOGICAL PEDAGOGICAL CONTENT KNOWLEDGE (TPACK). THE EFFORT IDENTIFIED KEY EXPERIENCES TO ENGAGE TEACHERS IN DISCOURSE AND CRITICAL REFLECTIONS FOR RELEARNING, RETHINKING, AND REDEFINING TEACHING AND LEARNING AS THEY KNOW AND LEARNED IT, TRANSFORMING THEIR TPACK WITH RESPECT TO TEACHING WITH DIGITAL TECHNOLOGIES. THE EXPERIENCES MODELED INQUIRY TASKS MERGING CONTENT, TECHNOLOGY AND PEDAGOGY AS DESCRIBED IN TPACK, CONNECTING TEACHERS WITH EXPERIENCES AS STUDENTS LEARNING ABOUT AND WITH TECHNOLOGIES. CRITICAL REFLECTIONS ON THE EXPERIENCES AS LEARNERS AND AS TEACHERS COMBINED WITH THE ONLINE COMMUNITY OF LEARNERS' DISCOURSE, TRANSFORMING THEIR TEACHER KNOWLEDGE. THE COLLECTION OF STRATEGIES INVOLVING DISCOURSE AND CRITICAL REFLECTION DID ENHANCE THE PARTICIPANTS' TPACK, PROVIDING RECOMMENDATIONS FOR DESIGNING ONLINE INSERVICE TEACHER EDUCATION COURSES. <https://doi.org/10.37626/GA9783959871129.0.80> O' DELL, JENNA R.; FRAUENHOLTZ, TODD R.: AN UNSOLVED GRAPH THEORY PROBLEM: COMPARING SOLUTIONS OF GRADES 4, 6, & 8. PP 428 – 433 THIS STUDY INVESTIGATED HOW STUDENTS IN GRADES 4, 6, AND 8 REASONED THROUGH A NON-ROUTINE, UNSOLVED PROBLEM. THE STUDY TOOK PLACE AT A K-8 SCHOOL IN THE MIDWESTERN UNITED STATES. EACH GRADE PARTICIPATED IN TWO OR THREE TASK-BASED SESSIONS LASTING BETWEEN 45 AND 60 MINUTES WITH THE RESEARCHERS. DURING THE SESSIONS, STUDENTS ENGAGED IN THE GRACEFUL TREE CONJECTURE WHERE THEY EXAMINED GRACEFUL LABELLING FOR STAR, PATH, AND CATERPILLAR GRAPHS. WE EXAMINED DIFFERENCES IN STUDENTS' GENERALIZED SOLUTIONS ACROSS THE GRADES AND HOW THEY WERE ABLE TO PROVIDE

JUSTIFICATIONS AND STATE GENERALIZATIONS OF A GRACEFUL LABELLING FOR THE GRAPHS IN THE PATH CLASS. DESCRIPTIONS OF STUDENTS' GENERALIZED SOLUTIONS ARE INCLUDED FOR EACH GRADE LEVEL.

<https://doi.org/10.37626/GA9783959871129.0.81> O' MEARA, NIAMH; FAULKNER, FIONA: PROFESSIONAL DEVELOPMENT FOR OUT-OF-FIELD POST-PRIMARY TEACHERS OF MATHEMATICS: A PRE AND POST ANALYSIS OF THE IMPACT OF MATHEMATICS SPECIFIC PEDAGOGICAL TRAINING. PP 434 – 439 THE PROFESSIONAL DIPLOMA IN MATHEMATICS FOR TEACHING IS A 2-YEAR PART-TIME PROGRAMME DEDICATED TO OUT OF FIELD TEACHERS OF MATHEMATICS IN SECOND LEVEL EDUCATION IN IRELAND. THE PROGRAMME WAS INTRODUCED IN IRELAND AFTER A REPORT HIGHLIGHTED THAT 48% OF SECOND LEVEL TEACHERS OF MATHEMATICS IN IRELAND WERE NOT QUALIFIED TO TEACH MATHEMATICS (N<sub>2</sub> R<sub>2</sub> ORD<sub>2</sub> IN € HANNIGAN 2011). THE PROGRAMME HAS BEEN RUNNING SINCE 2012 AND IS CURRENTLY UPSKILLING ITS 6TH COHORT OF OUT-OF-FIELD TEACHERS. AS PART OF THE PROGRAMME, TEACHERS ARE REQUIRED TO UNDERTAKE MATHEMATICS CONTENT MODULES AS WELL AS MATHEMATICS SPECIFIC PEDAGOGY MODULES. ONE SUCH MATHEMATICS SPECIFIC PEDAGOGY MODULE REQUIRES STUDENTS TO UNDERTAKE FIVE 3-HOUR WORKSHOPS WHICH EXAMINE MATHEMATICS CONTENT CONTAINED ON THE SECOND LEVEL CURRICULUM AND OFFERS SUGGESTIONS ON HOW TO TEACH IT FOR CONCEPTUAL UNDERSTANDING. TEACHERS IN COHORT 5 OF THE PROGRAMME COMPLETED A QUESTIONNAIRE PRIOR TO COMPLETING THE 5 WORKSHOPS TO OUTLINE HOW CONFIDENT THEY FELT TEACHING PARTICULAR ASPECTS OF THE SECOND LEVEL MATHEMATICS CURRICULUM. THEY WERE ALSO ASKED TO BEST DESCRIBE THE TEACHING APPROACHES THAT THEY FAVOURED AT THAT POINT IN TIME. UPON COMPLETION OF THE 5 WORKSHOPS, THIS SAME COHORT OF TEACHERS COMPLETED A SIMILAR QUESTIONNAIRE INVESTIGATING THEIR LEVEL OF CONFIDENCE IN TEACHING THE CURRICULUM AND ANY CHANGES IN THEIR TEACHING PRACTICES THAT OCCURRED AS A RESULT OF PARTICIPATION IN THIS MODULE. <https://doi.org/10.37626/GA9783959871129.0.82> PAGGE, JENNY: EFFECTIVE USE OF ICT AND STORYTELLING TO TEACH STATISTICS IN THE PRESCHOOL CLASSROOM. PP 440 – 444 NEW SCHOOL CURRICULA AND MODERN TEACHERS ARE TRYING TO GET THE CHILD ENGAGED AND INTERESTED IN STATISTICS THROUGH ACCESSIBILITY AND ENJOYMENT. THIS HAS BEEN BACKED UP BY MUCH RESEARCH INTO THE CORRELATION OF A CHILD'S ENGAGEMENT AND THEIR ACADEMIC ACHIEVEMENT (GUNUC, € KUZU, 2014). USING STORYTELLING AS A TEACHING METHOD, TEACHERS CAN PROVIDE A MEANINGFUL CONTEXT FOR STATISTICS WHICH CAN CHANGE THIS PREJUDICE FROM A YOUNG AGE (CASEY ET AL., 2004, WALTERS ET AL 2018) AND IS SHOWN TO HAVE MANY EDUCATIONAL BENEFITS FOR CHILDREN (SHERWOOD, 2018). IN THE LAST YEARS ICT TOOLS, GAMES AND STORYTELLING HAVE BEEN USED TO ACHIEVE THIS ENGAGEMENT (LEKKA ET AL, 2017, WALTERS 2018). ICT PROVIDES CHILDREN WITH THE OPPORTUNITY TO ENHANCE THEIR COMMUNICATION SKILLS, CREATIVITY, HIGH-ORDER THINKING AND PRACTICAL TECHNOLOGICAL SKILLS WHICH ARE NEEDED IN A MODERN SOCIETY (COREL, 2019). THIS PAPER INCLUDES A BRIEF OVERVIEW OF RESEARCH THAT LOOKS AT THE USE OF ICT APPLICATIONS, AND USE OF STORYTELLING TO TEACH DESCRIPTIVE STATISTICS IN THE PRESCHOOL CLASSROOM. <https://doi.org/10.37626/GA9783959871129.0.83> PAOLUCCI, CATHERINE: SUPPORTING PRE-SERVICE MATHEMATICS TEACHER DEVELOPMENT THROUGH TRANSFORMATIVE COMMUNITY ENGAGEMENT. PP 445 – 449 OPPORTUNITIES FOR FIELD-BASED TRANSFORMATIVE LEARNING ARE A CRITICAL PART OF MATHEMATICS TEACHER EDUCATION, YET SEVERAL FACTORS LIMIT THE EXTENT TO WHICH TEACHER PREPARATION PROGRAMS CAN OFFER THEM. THIS PAPER DISCUSSES THE VALUE OF TRANSFORMATIVE LEARNING FOR PRE-SERVICE MATHEMATICS TEACHERS AND PRESENTS AN EXAMPLE OF AN INTERNATIONAL COMMUNITY ENGAGEMENT PROGRAM THAT WAS SPECIFICALLY DESIGNED TO SUPPORT TRANSFORMATIVE LEARNING FOR PRE-SERVICE TEACHERS IN BOTH THE UNITED STATES AND SOUTH AFRICA. IT HIGHLIGHTS EVIDENCE OF KEY ASPECTS OF TRANSFORMATIVE LEARNING IN THE REFLECTIONS OF BOTH THE PRE-SERVICE TEACHERS AND THE STUDENTS IN THE PROGRAM AND DISCUSSES THE IMPLICATIONS OF THIS FOR FUTURE RESEARCH AND PROGRAM DEVELOPMENT.

<https://doi.org/10.37626/GA9783959871129.0.84> PEARN, CATHERINE; ET AL: DEVELOPING AND ASSESSING ALGEBRAIC REASONING IN THE MIDDLE YEARS. PP 450 – 455 NEW SCHOOL CURRICULA AND MODERN TEACHERS ARE TRYING TO GET THE CHILD ENGAGED AND INTERESTED IN STATISTICS THROUGH ACCESSIBILITY AND ENJOYMENT. THIS HAS BEEN BACKED UP BY MUCH RESEARCH INTO THE CORRELATION OF A CHILD'S ENGAGEMENT AND THEIR ACADEMIC ACHIEVEMENT (GUNUC, € KUZU, 2014). USING STORYTELLING AS A TEACHING METHOD, TEACHERS CAN PROVIDE A MEANINGFUL CONTEXT FOR STATISTICS WHICH CAN CHANGE THIS PREJUDICE FROM A YOUNG AGE (CASEY ET AL., 2004, WALTERS ET AL 2018) AND IS SHOWN TO HAVE MANY EDUCATIONAL BENEFITS FOR CHILDREN (SHERWOOD, 2018). IN THE LAST YEARS ICT TOOLS, GAMES AND STORYTELLING HAVE BEEN USED TO ACHIEVE THIS ENGAGEMENT (LEKKA ET AL, 2017, WALTERS 2018). ICT PROVIDES CHILDREN WITH THE OPPORTUNITY TO ENHANCE THEIR COMMUNICATION SKILLS, CREATIVITY, HIGH-ORDER THINKING AND PRACTICAL TECHNOLOGICAL SKILLS WHICH ARE NEEDED IN A MODERN SOCIETY (COREL, 2019). THIS PAPER INCLUDES A BRIEF OVERVIEW OF RESEARCH THAT LOOKS AT THE USE OF ICT APPLICATIONS, AND USE OF STORYTELLING TO TEACH DESCRIPTIVE STATISTICS IN THE PRESCHOOL CLASSROOM.

<https://doi.org/10.37626/GA9783959871129.0.85> PEARSON, ESTHER: „STEPS“ TO A BRIGHTER FUTURE. PP 456 – 461 THE „SCIENCE, TECHNOLOGY, ENGINEERING, PRECOLLEGE STUDIES“ (STEPS) PROGRAM WAS DEVELOPED IN 1988 BY DR. ESTHER PEARSON. THE STEPS PROGRAM HAS SERVED THOUSANDS OF YOUTH OVER THE PAST TWO DECADES TO PROVIDE ACADEMIC SUPPORT AND MENTORING TO MINORITIES AND WOMEN STUDENTS. THE STEPS PROGRAM FOCUSES ON DEMONSTRATING A CONNECTED LEARNING APPROACH TO STEM ACADEMICS. STUDENTS PARTICIPATE IN MENTORING THROUGH THE STEM PIPELINE OF COURSE CHOICES, EXTRA-CURRICULAR ACTIVITIES, AND EXPOSURE TO STEM PRACTITIONERS. STUDENTS LEARN TO OVERCOME THE CHALLENGES THAT PREVENT SUCCESSFUL MATRICULATION INTO STEM FIELDS. MINORITY AND WOMEN STUDENTS IN ELEMENTARY

THROUGH COLLEGE IN THE BOSTON AND GREATER BOSTON AREAS LEARN HOW TO NAVIGATE FROM A DESIRE FOR A STEM CAREER TO ACHIEVING ONE. <https://doi.org/10.37626/GA9783959871129.0.86> PILGRIM, MARY E.; DICK, THOMAS P.: ACTIVELY ENGAGING IN CALCULUS TO SUPPORT ALL STUDENTS. pp 462 – 466 RESEARCH FINDINGS SUPPORT THE USE OF ACTIVE ENGAGEMENT IN THE MATHEMATICS CLASSROOM. ACTIVE LEARNING NOT ONLY HAS THE POTENTIAL TO POSITIVELY IMPACT STUDENT LEARNING, IT ALSO HELPS TO ADDRESS EQUITY ISSUES IN THE MATHEMATICS CLASSROOM. HOWEVER, WITH LIMITED EXPERIENCES IN STUDENT-CENTERED INSTRUCTION AND LITTLE TO NO PEDAGOGICAL TRAINING, MATHEMATICS FACULTY ARE OFTEN UNDERPREPARED TO MEET THE NEEDS TO TODAY'S STEM MAJORS. IN ADDITION, CONTENT-SPECIFIC PROFESSIONAL DEVELOPMENT IS TYPICALLY NOT READILY AVAILABLE TO FACULTY ON THEIR CAMPUSES. WITH A FOCUS ON CALCULUS, THIS WORKSHOP AIMS TO FILL THIS PROFESSIONAL DEVELOPMENT GAP BY PROVIDING PARTICIPANTS WITH THE OPPORTUNITY TO ENGAGE IN STUDENT-CENTERED ACTIVITIES AS WELL AS REFLECT AND DISCUSS THE IMPLICATIONS FOR THEIR OWN MATHEMATICS CLASSROOMS.

<https://doi.org/10.37626/GA9783959871129.0.87> POMUCZNŹ NAGY, ILDIKŹ -ANNA: HOW AND WHERE CAN A MATHEMATICS TEACHER UTILIZE HIS 33 YEARS OF TEACHING EXPERIENCE? A MATH TEACHER ABOUT TEACHING MATHEMATICS- EXCERPT FROM 33 YEARS OF TEACHING EXPERIENCE. pp 467 – 472 THIS PAPER SHOWS HOW A MATHEMATICS TEACHER CAN UTILIZE HIS TEACHING EXPERIENCE. I HAVE BEEN WORKING AS A MATHEMATICS AND PHYSICS TEACHER IN HUNGARY FOR 33 YEARS. I HAVE TAUGHT AT VARIOUS LEVELS OF THE EDUCATION SYSTEM: AT ELEMENTARY SCHOOL, HIGH SCHOOL, TEACHER TRAINING COLLEGE, AND IN TEACHER TRAINING TOO, BUT AT MOST TIME OF MY JOB I TAUGHT AT HIGH SCHOOL. I AM CURRENTLY WORKING ON THE SERIES OF A NEW MATHEMATICS TEXTBOOK FOR 10 TO 14-YEAR-OLD STUDENTS. IT IS BASED ON THE TRADITIONS OF THE HUNGARIAN MATHEMATICS EDUCATION, BUT USING THE OPPORTUNITIES OFFERED BY THE 21ST CENTURY, IT ALSO INCLUDES MODERN SAMPLE TASKS THAT FIT INTO THE CURRICULUM, FOR EXAMPLE GEOGEBRA FILES, WRITTEN BY ME. I WOULD LIKE TO SHARE HOW I USE MY TEACHING EXPERIENCE IN TEXTBOOK WRITING AND HOW I FOCUS PRIMARILY ON THE DIDACTIC ASPECTS OF TEACHING MATHEMATICS. I PURSUE MY PHD RESEARCH IN THE TOPIC OF PROBLEM-SOLVING THINKING, SO I STUDY THE MATHEMATICAL THINKING OF MY STUDENTS STUDYING IN DIFFERENT SCHOOL TYPES. IN MY LECTURE, I ANALYSE DIFFERENT TASKS BY FOCUSING ON MATHEMATICAL METHODOLOGICAL ASPECTS. FOR EXAMPLE I WILL TELL THAT I BELIEVE IT IS ADVANTAGEOUS TO INTRODUCE MATHEMATICAL DEFINITIONS WITH EXAMPLES WHICH ARE ASTONISHING FOR STUDENTS IN ORDER TO DRAW ATTENTION TO MATHS AS MUCH AS POSSIBLE. I WILL GIVE EXAMPLES OF HOW I BUILD MY EXPERIENCE INTO THE TEXTBOOK IN ORDER TO MAKE THE SYSTEM OF MATHEMATICAL CONCEPTS OPTIMAL FOR PUPILS. I WOULD LIKE IT IF GIVE YOU AN INSIGHT INTO A SEGMENT THE CURRENT HUNGARIAN MATHEMATICS EDUCATION, THE CURRENT TEACHING OF PROBLEM-SOLVING THINKING AND THE DIFFERENT WAYS OF STUDENTS' THINKING. <https://doi.org/10.37626/GA9783959871129.0.88>

POVEY, HILARY: MORAL AND POLITICAL DILEMMAS IN WORKING WITH THE CONCEPT OF CITIZENSHIP WITHIN MATHEMATICS TEACHING IN SCHOOLS: A PERSONAL PERSPECTIVE. pp 473 – 478 THIS PAPER SPRINGS OUT OF MY ENGAGEMENT WITH A CURRICULUM DEVELOPMENT PROJECT FRAMED IN RESPONSE TO A EUROPEAN UNION CALL FOR ACTION ON GLOBAL CITIZENSHIP. BUT CITIZENSHIP IS A COMPLEX AND ELUSIVE CONCEPT – SLIPPERY, DANGEROUS AND CONTESTED. INEVITABLY, TENSIONS ARISE AS WE SEEK TO FIND A WAY OF ACTING IN THE WORLD AND TRYING TO FIND, HOWEVER LIMITED AND PARTIAL, AN ANSWER TO THE QUESTION: „WHAT IS TO BE DONE?“. IN THIS PAPER, I IDENTIFY AND OFFER A PERSONAL RESPONSE TO SOME OF MORAL AND POLITICAL DILEMMAS WE HAVE IDENTIFIED DURING THE DESIGN AND IMPLEMENTATION OF THE PROJECT. <https://doi.org/10.37626/GA9783959871129.0.89> PRENDERGAST, MARK; ET AL: INCENTIVISING THE STUDY OF HIGHER LEVEL MATHEMATICS. pp 479 – 484 IN IRELAND, MATHEMATICS HAS BEEN ASSIGNED A SPECIAL STATUS WITHIN THE POSTPRIMARY SCHOOL CURRICULUM WITH THE INTRODUCTION OF A BONUS POINTS INITIATIVE (BPI) IN 2012. STUDENTS ARE NOW AWARDED AN EXTRA 25 POINTS IN THEIR UPPER POST-PRIMARY SCHOOL STATE EXAMINATION RESULTS IF THEY ACHIEVE A PASSING GRADE AT HIGHER LEVEL (HL) MATHEMATICS. THE CULMINATION OF POINTS THAT STUDENT ACHIEVE IN SIX DIFFERENT SUBJECTS ACTS AS A GATEKEEPER TO TERTIARY LEVEL EDUCATION. MATHEMATICS IS THE ONLY SUBJECT IN WHICH THERE ARE EXTRA POINTS AWARDED. THE INITIATIVE WAS INTRODUCED TO ENCOURAGE MORE STUDENTS TO STUDY THE SUBJECT AT AN ADVANCED LEVEL. ANECDOTALLY THERE HAVE BEEN MANY MIXED REVIEWS ABOUT THE SUCCESS OF THE BPI. WHILE THE NUMBERS TAKING HL MATHEMATICS HAVE STEADILY INCREASED, THERE HAVE BEEN CONCERNS EXPRESSED THAT MANY STUDENTS WHO ARE NOT MATHEMATICALLY CAPABLE OF PERFORMING UP TO THE STANDARD REQUIRED ARE NOW OPTING FOR THE HL PAPER AND THAT THE DIFFICULTY OF THIS EXAMINATION AND THE MARKING SCHEMES HAVE BEEN ADJUSTED ACCORDINGLY. THIS PAPER INVESTIGATES THE ADVANTAGES AND DISADVANTAGES ASSOCIATED WITH THE BPI FROM THE PERSPECTIVE OF MATHEMATICS TEACHERS (n=266).

<https://doi.org/10.37626/GA9783959871129.0.90> RAJA, SHAGUFTA; ET AL: USING GIS TO DEVELOP SPATIAL REASONING AND ANALYSIS OF DATA. pp 485 – 490 THE GEOGRAPHIC INFORMATION SYSTEM (GIS) IS A SPATIAL ANALYSIS TOOL THAT ALLOWS USERS TO CAPTURE, STORE, ANALYZE, AND VISUALIZE DATA RELATED TO REAL-WORLD PROBLEMS. GIS IS USED DAILY IN MULTIPLE STEM FIELDS TO SOLVE COMPLEX PROBLEMS. EDUCATORS FIND GIS USEFUL FOR STUDENTS TO BE ABLE TO INTERPRET DATA IN A SPATIAL CONTEXT. STUDENTS DEVELOP QUANTITATIVE AND SPATIAL ANALYSIS REASONING USING GIS TO UNDERSTAND AND DEVELOP SOLUTIONS FOR MANY CURRENT SCIENTIFIC CONCERNS. THIS PAPER PRESENTS TWO CASES HIGHLIGHTING MIDDLE GRADE STUDENTS' USE OF GIS. THE CASES ILLUSTRATE HOW GIS PROMOTES STUDENTS' DEVELOPMENT OF SPATIAL REASONING AS THEY THINK ABOUT PATTERNS AND RELATIONSHIPS MADE EVIDENT THROUGH DATA VISUALIZATION. THE CASES DEMONSTRATE HOW STUDENTS ENGAGE IN FINDING RELATIVE AND ABSOLUTE MAPPED FEATURES, GEOGRAPHIC PATTERNS, AND

CHANGES OVER TIME AS THEY MAKE DECISIONS USING GEOGRAPHIC INQUIRY, SPATIAL THINKING AND PROBLEM SOLVING. <https://doi.org/10.37626/GA9783959871129.0.91> RAMSAY, JOHN R.: MENTORED TEAMS OF UNDERGRADUATES IN REAL WORLD CONSULTING. PP 491 – 496 ONE OF THE DIFFICULTIES IN MATHEMATICS EDUCATION IS PROVIDING A GOOD ANSWER TO THE “WHAT CAN I DO WITH MATHEMATICS?” QUESTION. APPLIED EXAMPLES AND PROJECTS WITHIN EXISTING MATHEMATICS COURSES CAN HELP ANSWER THIS BUT OFTEN AREN’T CLOSE ENOUGH TO REAL WORLD APPLICATIONS AND THEY CAN CONSUME CONSIDERABLE COURSE TIME. WE HAVE ADDRESSED THIS DIFFICULTY WITH A SUMMER PROGRAM THAT EMPLOYS STUDENTS TO SOLVE ACTUAL APPLIED PROBLEMS. THE COLLEGE OF WOOSTER APPLIED METHODS & RESEARCH EXPERIENCE IS A SUMMER PROGRAM THAT PUTS TEAMS OF STUDENTS TO WORK AS CONSULTANTS IN THE LOCAL COMMUNITY. STUDENT TEAMS ARE USUALLY COMPOSED OF THREE STUDENTS WITH A MATHEMATICS OR COMPUTER SCIENCE FACULTY MEMBER ACTING AS MENTOR. CLIENTS OF THE PROGRAM COME FROM BUSINESS, INDUSTRY, GOVERNMENT AGENCIES, AND SERVICE ORGANIZATIONS. THE PROGRAM ALSO INCLUDES A SIGNIFICANT PROFESSIONAL DEVELOPMENT COMPONENT IN ORDER TO INCREASE THE EDUCATIONAL BENEFIT TO THE PARTICIPANTS. <https://doi.org/10.37626/GA9783959871129.0.92> RUGELJ, MARINA: COUNTING WITH 10 FINGERS AS A MAN, WITH 8 FINGERS AS A HEN OR WITH 2 SWITCHES AS A COMPUTER. PP 497 – 502 IN THE HIGH SCHOOL CURRICULUM OF MATHEMATICS IN SLOVENIA ONE OF THE GOALS IS “STUDENTS CAN CONVERT FROM DECIMAL TO BINARY NUMBER”. IN MOST HIGH SCHOOLS, AN ALGORITHM FOR CONVERSION IS PRESENTED, WHICH THE STUDENTS LEARN BY HEART LIKE A COOKING RECIPE, WITHOUT PROPER UNDERSTANDING. A DIFFERENT METHOD WILL BE PRESENTED, WHERE PUPILS PLAY, EXPLORE AND FIND CERTAIN CONCLUSIONS ON THEIR OWN. THIS HELPS STUDENTS TO UNDERSTAND AND LEARN THE NEW CONCEPT MUCH MORE EFFICIENTLY, COMPARING TO WHEN THEY ONLY LISTEN TO THE INSTRUCTION. HENCE, THE KNOWLEDGE GAINED THIS WAY IS HOPEFULLY MORE SOLID AND LASTING. <https://doi.org/10.37626/GA9783959871129.0.93> SACK, JACQUELINE; QUANDER, JUDITH: SECONDARY MATH TEACHER CANDIDATES’ PERSPECTIVES ON A CO-TAUGHT BLENDED CONTENT & METHODS GEOMETRY COURSE. PP 503 – 508 TWO FACULTY, FROM THE MATHEMATICS AND EDUCATION DEPARTMENTS IN AN URBAN UNIVERSITY, CO-TEACH A BLENDED METHODS AND CONTENT GEOMETRY COURSE FOR PRESERVICE SECONDARY TEACHERS WHO ARE ALSO MATH MAJORS. THE COURSE IS ENTIRELY INQUIRY-BASED, A DEPARTURE FROM TRADITIONAL INSTRUCTOR-CENTERED MATHS COURSES, AND UTILIZES DESIGN-BASED TRAJECTORIES DEVELOPED BY ONE OF THE AUTHORS OVER 12 YEARS. WE CONDUCTED TWO INDIVIDUAL CLINICAL INTERVIEWS AND ONE FOCUS-GROUP INTERVIEW WITH 6 VOLUNTEER STUDENTS, TO ASCERTAIN THEIR PERSPECTIVES ON HOW THEY BEST LEARN MATHEMATICS; TO GAUGE HOW THEY PERCEIVED THE INQUIRY-BASED EXPERIENCES FROM THIS COURSE; AND, THEIR REFLECTIONS ON INQUIRY-BASED INSTRUCTION IN MATHEMATICS AS THEY MOVE FORWARD IN THEIR GOALS TO BECOME TEACHERS. WE USED NARRATIVE INQUIRY AS A RESEARCH METHOD TO STUDY THE EXPERIENCES OF THESE STUDENTS INDIVIDUALLY AND COLLECTIVELY. <https://doi.org/10.37626/GA9783959871129.0.94> S[?] ENZ-LUDLOW, ADALIRA; JIM[?] NEZ, ALEXANDRA JIM[?] NEZ: LINKAGES BETWEEN A TEACHER’S PREPARATION AND THE POTENTIAL FOR STUDENTS’ LEARNING. PP 509 – 514 FROM THE PEIRCEAN PERSPECTIVE OF DIAGRAMMATIC REASONING, THE PAPER PRESENTS A TEACHER’S ANALYSIS OF A TASK WITH A SQUARE ARRAY OF DOTS. SHE CONCEPTUALIZES DIFFERENT PARTITIONS OF THE ARRAY AND TRANSFORMS IT INTO DIFFERENT TASKS OF SEQUENCES OF SQUARES TO FACILITATE HER INDUCTIVE THINKING AND THE EMERGENCE OF DIFFERENT GENERALIZATIONS PERTAINING SQUARE NUMBERS. <https://doi.org/10.37626/GA9783959871129.0.95> SANTHANAM, S. R.: WELCOME 2019 – A WORKSHOP ON FRAMING NON-ROUTINE PROBLEMS IN MATHEMATICS FOR ALL LEVELS. PP 515 – 516 THE MAIN ASPECT OF MATHEMATICS IS PROBLEM SOLVING. A NON-ROUTINE PROBLEM IS ANY COMPLEX PROBLEM THAT REQUIRES SOME DEGREE OF CREATIVITY TO SOLVE. THERE ARE NO STANDARDISED METHODS TO SOLVE A NON-ROUTINE PROBLEM, IF THERE IS ONE THEN IT BECOMES A ROUTINE PROBLEM. WHAT ABOUT FRAMING A NON-ROUTINE PROBLEM? IT IS ALL THE MORE DIFFICULT. IN THIS WORKSHOP THE AUTHOR ATTEMPTS TO MAKE THE AUDIENCE TO UNDERSTAND NON-ROUTINE PROBLEMS AND THEIR SOLUTIONS AND FURTHER TO FRAME PROBLEMS OF THIS NATURE. <https://doi.org/10.37626/GA9783959871129.0.96> SHAMASH, JOSEPHINE: FROM EQUATIONS TO STRUCTURES: LINKING ABSTRACT ALGEBRA AND HIGH-SCHOOL ALGEBRA FOR SECONDARY SCHOOL TEACHERS. PP 517 – 522 THE HIGH-SCHOOL CURRICULUM IN ALGEBRA DEALS MAINLY WITH THE SOLUTION OF DIFFERENT TYPES OF EQUATIONS. MODERN ALGEBRA HAS A COMPLETELY DIFFERENT VIEWPOINT AND IS CONCERNED WITH ALGEBRAIC STRUCTURES AND OPERATIONS. THE COURSE ALGEBRA: FROM EQUATIONS TO STRUCTURES IS PART OF AN M.SC. PROGRAMME FOR ISRAELI SECONDARY SCHOOL MATHEMATICS TEACHERS. IT PROVIDES AN INTRODUCTION TO ALGEBRAIC STRUCTURES AND MODERN ABSTRACT ALGEBRA, AND LINKS ABSTRACT ALGEBRA TO THE HIGH-SCHOOL CURRICULUM IN ALGEBRA. IT FOLLOWS THE HISTORICAL ATTEMPTS OF MATHEMATICIANS TO SOLVE POLYNOMIAL EQUATIONS OF HIGHER DEGREES, ATTEMPTS WHICH RESULTED IN THE DEVELOPMENT OF GROUP THEORY AND FIELD THEORY BY GALOIS AND ABEL. THIS APPROACH LEADS NATURALLY TO EXAMINING TOPICS AND FUNDAMENTAL THEOREMS IN BOTH GROUP THEORY AND FIELD THEORY. ALONG THE HISTORICAL “JOURNEY”, MANY OTHER MAJOR RESULTS IN ALGEBRA IN THE PAST 150 YEARS ARE INTRODUCED, AND CURRENT RESEARCH IN ALGEBRA IS HIGHLIGHTED. WE EXAMINE THE RELEVANCE OF THE COURSE TO THE TEACHERS’ WORK. <https://doi.org/10.37626/GA9783959871129.0.97> SHOWERS, DENNIS: REAL-WORLD MATHS: PREPARING TEACHERS TO USE REAL-LIFE CONTEXTS FOR TEACHING MATHS. PP 523 – 525 COMMON CORE MATHEMATICS IN THE US PROMOTES EIGHT STANDARDS FOR MATHEMATICAL PRACTICE TO GUIDE INSTRUCTIONAL REFORM. STANDARD 2 INCLUDES THE PRACTICE OF “DECONTEXTUALIZING” OR ABSTRACTING A GIVEN SITUATION AND REPRESENTING IT SYMBOLICALLY TO SOLVE REAL-WORLD PROBLEMS. PREPARING TEACHERS TO EMPLOY THIS PRACTICE IN CLASSROOMS REQUIRES KNOWLEDGE AND SKILL TO APPLY

TECHNOLOGY TO BRING THE REAL WORLD INTO THE CLASSROOM AND THE ABILITY TO DISCUSS PERSONAL EXPERIENCES IN A MATHEMATICAL WAY. PROFESSIONAL DEVELOPMENT WITH NEW YORK TEACHER CANDIDATES AND IN-SERVICE TEACHERS IN NICARAGUA, CHINA, AND THE US INDICATES THE NEED FOR FURTHER DISSEMINATION WITH A RESEARCH PROGRAM TO EVALUATE ITS EFFICACY. <https://doi.org/10.37626/GA9783959871129.0.98> SHRIKI, ATARA; LAVY, ILANA: SHEDDING NEW LIGHT ON COMMON ALGORITHMS: WHAT CAN WE LEARN FROM VEDIC MATHEMATICS? pp 526 – 528 In SANSKRIT, THE ANCIENT HINDUISM LANGUAGE, ‘VEDAS’ MEANS ‘KNOWLEDGE’. THE VEDAS ARE A CORPUS OF MORE THAN 1,000,000 ANCIENT PHILOSOPHICAL WRITINGS DIVIDED INTO SUTRAS, SOME OF WHICH DEAL WITH MATHEMATICS. THESE MATHEMATICS SUTRAS, TERMED ‘VEDIC MATHEMATICS’, CONCERN VARIOUS FIELDS OF MATHEMATICS. THE VEDIC METHODS ARE COHERENT, LOGICAL AND SIMPLE, AND STUDENTS ENJOY PRACTICING THEM. BESIDES ‘SPICING UP’ THE REGULAR MATHEMATICS LESSONS BY INTEGRATING SOME OF THE VEDIC ALGORITHMS, ENGAGING STUDENTS IN PROVING THEM SUPPORTS THE DEVELOPMENT OF THEIR INSIGHTS REGARDING THE RATIONALE UNDERLYING THE FORMAL RULES AND ALGORITHMS INCLUDED IN THE CURRICULUM. IN THIS WORKSHOP, WE PRESENT SOME OF THE BASIC VEDIC ARITHMETIC AND ALGEBRAIC ALGORITHMS, INVOLVE THE PARTICIPANTS IN PROVING THEM AND DISCUSS THE ADVANTAGES AND DISADVANTAGES OF INTEGRATING VEDIC MATHEMATICS INTO CLASSES AT DIFFERENT AGE GROUPS AND STUDY LEVELS. <https://doi.org/10.37626/GA9783959871129.0.99> SIBBALD, TIMOTHY: THE CONFLUENCE OF NUMERACY WITH INTERDISCIPLINARY MATHEMATICS. pp 529 – 534 INTERDISCIPLINARY MATHEMATICS, SUCH AS STEM, BUT NOT LIMITED TO IT, HAS RECEIVED CONSIDERABLE ATTENTION IN RECENT YEARS. ITS ROLE IN MATHEMATICS IS THE PROVISION OF PRACTICAL CIRCUMSTANCES THAT SUPPORT LEARNING MATHEMATICAL CONCEPTS. THE VALIDATION OF CONCEPTS THROUGH THE ADOPTION TO INTERDISCIPLINARY PURPOSES HAS A BROAD BASE OF EXAMPLES. FURTHERMORE, AMONG THE CONCEPTS BRIDGING MATHEMATICS AND ANOTHER DISCIPLINE IS A GROUP OF CONCEPTS THAT TRANSCEND A VARIETY OF OTHER DISCIPLINES AND, WITHIN THAT SCOPE, NUMERACY EMERGES. SINCE THIS IS NOT A TRADITIONAL DEFINITION OF NUMERACY IT IS RECONCILED WITH OTHER DEFINITIONS OF NUMERACY AND THE IMPLICATIONS OF THAT RECONCILIATION WITH INTERDISCIPLINARY INSTRUCTIONAL APPROACHES IS EXAMINED. <https://doi.org/10.37626/GA9783959871129.0.100> SIEMON, DIANNE: CONNECTING RESEARCH AND PRACTICE – THE CASE OF MULTIPLICATIVE THINKING. pp 535 – 540 THERE IS VERY LITTLE OF ANY SUBSTANCE THAT CAN BE ACHIEVED IN SCHOOL MATHEMATICS, AND BEYOND WITHOUT THE CAPACITY TO RECOGNISE, REPRESENT AND REASON ABOUT RELATIONSHIPS BETWEEN QUANTITIES, THAT IS, TO THINK MULTIPLICATIVELY. HOWEVER, RESEARCH HAS CONSISTENTLY FOUND THAT WHILE MOST STUDENTS IN THE MIDDLE YEARS OF SCHOOLING (I.E., YEARS 5 TO 9) ARE ABLE TO SOLVE SIMPLE MULTIPLICATION AND DIVISION PROBLEMS INVOLVING SMALL WHOLE NUMBERS, THEY RELY ON ADDITIVE STRATEGIES TO SOLVE MORE COMPLEX PROBLEMS INVOLVING LARGER NUMBERS, FRACTIONS, DECIMALS, AND/OR PROPORTION. THIS PAPER DESCRIBES HOW THIS SITUATION CAN BE ADDRESSED THROUGH THE USE OF EVIDENCE-BASED FORMATIVE ASSESSMENT TOOLS AND TEACHING ADVICE SPECIFICALLY DESIGNED TO SUPPORT THE DEVELOPMENT OF MULTIPLICATIVE THINKING. <https://doi.org/10.37626/GA9783959871129.0.101> SMITH, RAYMOND; ET AL: INSIGHTS GAINED FROM IMPLEMENTING TEACHING TOOLKITS: A CASE OF ACTIVATING PRIOR KNOWLEDGE. pp 541 – 546 IN DESIGNING TEACHING TOOLKITS FOR TEACHERS THE EFFECTIVENESS OF SUCH A RESOURCE DEPENDS ON MUTUAL ENACTMENT AND ENGAGEMENT BY THE DESIGNER, THE TEACHER AND THE LEARNERS. IT IS A RECURSIVE PROCESS AND ILLUMINATES THE TENSIONS BETWEEN THE INTENDED OUTCOMES ENVISAGED BY THE DESIGNER AND THE REALISED OUTCOMES IN THE CLASSROOM. IN THE QUALITATIVE RESEARCH TRADITION, THE EXPLORATORY INVESTIGATION CAPTURED IN THIS PAPER EMPLOYED A DESCRIPTIVE PHENOMENOLOGICAL APPROACH. WITH THIS ORIENTATION, AND ALONG THE THEORETICAL TRAJECTORY LED BY TODRES (2005:107), THIS STUDY SOUGHT TO COLLECT DETAILED DESCRIPTIVE ACCOUNTS OF PERSONAL EXPERIENCE. DATA WERE GATHERED BY COLLECTING SAMPLES OF LEARNERS’ WORK, TEACHER INTERVIEWS AND CLASSROOM OBSERVATIONS. THIS PAPER DRAWS ATTENTION TO THE PRACTICAL DISJUNCTURE BETWEEN ASSESSING AND ACTIVATING PRIOR KNOWLEDGE. INSIGHTS ACQUIRED MAY CONTRIBUTE BOTH TO THE DESIGN APPROACH AND TO TEACHING PRACTICE. <https://doi.org/10.37626/GA9783959871129.0.102> SPOONER, KERRI: AUTHENTIC MATHEMATICAL MODELLING BEHAVIOURS FOR SECONDARY SCHOOL STUDENTS. pp 547 – 551 MATHEMATICAL MODELLING IS PART OF MANY CURRICULA AROUND THE WORLD. SOME OF THESE CURRICULUM STATEMENTS ARE VAGUE AND GENERAL. THERE IS A NEED FOR STATEMENTS TO BE MORE SPECIFIC WITH SUPPORTING EXAMPLES FOR IMPLEMENTATION OF CURRICULUMS. THERE IS ALSO A NEED FOR FURTHER DEVELOPMENT OF ACTIVITIES FOCUSED ON AUTHENTIC MATHEMATICAL MODELLING BEHAVIOUR. TO ADDRESS THIS PROBLEM, AN ETHNOGRAPHIC STUDY IN NEW ZEALAND WAS CARRIED OUT TO IDENTIFY THE BEHAVIOURS OF A REAL WORLD MATHEMATICAL MODELLING TEAM. THESE BEHAVIOURS WERE THEN EXPLORED TO DETERMINE WHAT THEY COULD LOOK LIKE FOR A SIXTEEN-YEAR-OLD STUDENT. THIS PAPER WILL PRESENT THE MODELLING BEHAVIOURS OF THE REAL WORLD MODELLING TEAM AND THE POTENTIAL AUTHENTIC MATHEMATICAL MODELLING BEHAVIOURS OF A SECONDARY SCHOOL STUDENT. <https://doi.org/10.37626/GA9783959871129.0.103> STEPHENS, MAX: DEVELOPING ALGORITHMIC THINKING IN MATHEMATICS IN THE PRIMARY AND JUNIOR SECONDARY YEARS. pp 552 – 557 THE FOURTH INDUSTRIAL REVOLUTION IS ALREADY CHANGING WHAT WE MEAN BY MATHEMATICAL REASONING IN ITS DIFFERENT FORMS, SUCH AS ALGEBRAIC, SPATIAL AND GEOMETRIC, AND STATISTICAL. ALGORITHMIC THINKING IS ONE PARTICULAR FORM OF MATHEMATICAL REASONING, EMPHASIZING DECOMPOSITION (BREAKING A COMPLEX PROBLEM DOWN INTO COMPONENT SUB-PROBLEMS AND SUB-TASKS), PATTERN RECOGNITION, GENERALIZATION AND ABSTRACTION. WITH A GROWING GLOBAL EMPHASIS ON USING ALGORITHMIC THINKING IN CODING AND COMPUTING PROGRAMS IN

SCHOOLS, IT IS NECESSARY TO EXAMINE HOW ALGORITHMIC THINKING SHOULD BE INCLUDED MORE EXPLICITLY IN THE TEACHING AND LEARNING OF MATHEMATICS. <https://doi.org/10.37626/GA9783959871129.0.104> TAKAHASHI, TADASHI: PROVING IN MATHEMATICS EDUCATION – ON THE PROOF USING ATP. pp 558 – 563 THE AIM OF THE MATHEMATICS EDUCATION IS THE ACQUISITION OF “KNOWLEDGE/SKILL OF THE MATHEMATICS” AND “THE MATHEMATICAL THINKING”. PROVING IS A CHAIN OF THE LOGIC IN MATHEMATICS AND IS “MATHEMATICAL THINKING” ITSELF. So, PROVING IS THE DOMAIN THAT IS IMPORTANT FROM A POINT OF VIEW THAT CAN EVALUATE THE ACQUISITION OF ENOUGH “MATHEMATICAL THINKING”. THERE IS A VARIETY OF SENSE OF VALUES IN THE PRESENT SITUATION OF THE PROOF USING THE ATP (AUTOMATED THEOREM PROVING). WE SHOULD ESTABLISH A CLEAR VISION AS MATHEMATICS EDUCATION IN THIS SITUATION. THAT IS, IN MATHEMATICS EDUCATION, WE SHOULD BUILD SENSE OF VALUES FOR PROOF USING THE ATP NEWLY. TO THAT END, WE FIX CONTENTS OF THE MATHEMATICS, AND IT IS NECESSARY TO PROVE THEM BY USING ATP. WE WOULD LIKE TO ASSUME THE AIM THE THEOREMS OF EUCLID’S ELEMENTS. BECAUSE THE CONTENTS ARE THE BASICS OF THE MATHEMATICAL THINKING. THE PROVING IS AN IMPORTANT AIM IN THE MATHEMATICS EDUCATION, IT IS NECESSARY TO CLARIFY NEW VALUE BY USING THE ATP AS MATHEMATICS EDUCATION.

<https://doi.org/10.37626/GA9783959871129.0.105> TANNOR, DAVID: EFFECTIVE MATHEMATICS INSTRUCTION: TWO-YEAR COLLEGE MATHEMATICS INSTRUCTORS’ KNOWLEDGE AND SELF-EFFICACY. pp 564 – 569 IN THIS ARTICLE ARE FINDINGS FROM A 2017 MIXED METHODS STUDY ON TWO-YEAR COLLEGE MATHEMATICS INSTRUCTORS’ KNOWLEDGE AND SELF-EFFICACY ON EFFECTIVE PEDAGOGY. <https://doi.org/10.37626/GA9783959871129.0.106> TEMPLE, BARBARA ANN; ET AL: DESIGNING A TRANSDISCIPLINARY APPROACH TO ELEMENTARY MATH LITERACY LEARNING THROUGH SCIENCE & THE ARTS. pp 570 – 574 ENGAGING WITH SUBJECT MATTER IN ISOLATION STYMIES CREATIVITY, PROMOTES ROTE LEARNING, AND LIMITS DEVELOPMENT OF DIVERGENT THINKING SKILLS. CONVERSELY, A TRANSDISCIPLINARY APPROACH TO MATH DEVELOPS CRITICAL AND CREATIVE THINKING SKILLS, STRENGTHENS PROBLEM SOLVING CAPACITY, AND PROMOTES METACOGNITION. IN THIS PILOT STUDY, THE DESIGN-BASED RESEARCH PROCESS BEGAN WITH SHARING INITIAL INTERVENTION IDEAS FOR ELEMENTARY MATH LESSONS WITH PARTICIPANTS AT AN INTERNATIONAL ELEMENTARY MATH CONFERENCE. UTILIZING PARTICIPANT FEEDBACK AS PART OF THE ITERATIVE PROCESS, THREE SPECIFIC INTERVENTIONS FOR SECOND-GRADE MATH CONCEPTS WERE DESIGNED WITH INTENTIONAL INFUSION OF SCIENCE AND THE ARTS. THE ULTIMATE GOAL FOR THIS RESEARCH IS THE DESIGN OF AN EFFECTIVE ELEMENTARY MATH CURRICULUM OFFERING AUTHENTIC, REAL-WORLD LEARNING THROUGH A TRANSDISCIPLINARY APPROACH.

<https://doi.org/10.37626/GA9783959871129.0.107> THOMAS, JEFFREY: LEARNING THROUGH SELF-ASSESSMENT TOWARDS UNDERSTANDING THE NEW B.ED. CURRICULUM IN SOUTH AFRICA: EXPERIENCES FROM THE NEW B.ED. PROGRAMME AT SOL PLAATJE UNIVERSITY. pp 575 – 580 THE MISMATCH BETWEEN INSTRUCTION AND LEARNING COULD POSE A SERIOUS BARRIER TO EFFECTIVE TEACHING AND LEARNING. EFFECTIVE TEACHING SHOULD BE A DYNAMIC ALIGNMENT AND REALIGNMENT OF TEACHING AND LEARNING STYLES TO OPTIMISE ACHIEVEMENT. WHEN TEACHING AND LEARNING STYLES DO NOT COMPLEMENT EACH OTHER STUDENTS MAY BECOME ANXIOUS, FRUSTRATED AND DISENGAGED WHICH MAY HAVE NEGATIVE EFFECTS ON THEIR PERFORMANCE. THE FOCUS OF THE STUDY IS TO GATHER EVIDENCE ON HOW STUDENTS PERCEIVE THEIR OWN LEARNING IN ORDER TO ADAPT THE TEACHING APPROACH WHICH WILL ACCOMMODATE THE STUDENTS’ PREFERRED WAY OF LEARNING. THE MAIN FINDINGS IN THIS STUDY SHOWED THAT STUDENTS PREFER TO WORK INDEPENDENTLY AND THAT ELEMENTS OF METACOGNITION ARE PRESENT DURING THEIR EFFORTS TO LEARN. THIS STUDY THEREFORE SUGGESTS THAT SELF-ASSESSMENT ACTIVITIES SHOULD BECOME AN INTEGRAL PART OF THE TEACHING AND LEARNING PROCESS. THUS, STUDENTS ARE AFFORDED THE OPPORTUNITY TO ADVANCE PERSONAL LEARNING THROUGH THE DEVELOPMENT OF METACOGNITION AS SELF-MONITORING AND CORRECTIVE ACTIONS. KEY WORDS: SELF-ASSESSMENT, METACOGNITION, SELF-REGULATED LEARNING <https://doi.org/10.37626/GA9783959871129.0.108>

108 TORO-CLARKE, JOSÉ A.: A PARTICIPATIVE AND INDIVIDUALIZED LABORATORY: A STRATEGY FOR INCREASING STUDENT SUCCESS IN COLLEGE-LEVEL MATH COURSES. pp 581 – 586 THIS RESEARCH WAS CARRIED OUT WITHIN A QUALITATIVE RESEARCH PARADIGM. THE OBJECTIVE WAS TO OBSERVE, ANALYZE AND ENRICH PEDAGOGICAL PRACTICE THROUGH THE USE OF PEDAGOGICAL LEARNING STRATEGIES. THE LEARNING STRATEGY WAS A PARTICIPATIVE AND INDIVIDUALIZED LABORATORY CARRIED OUT DURING A RESEARCH PROJECT IN A NON-TRADITIONAL LABORATORY (LNT, ABBREVIATED IN SPANISH FORM). THE PRIMARY AIM OF THIS RESEARCH WAS TO OBSERVE IF THE LNT ASSISTS THE STUDENTS AND IN THIS WAY MAXIMIZES SUCCESS AND KNOWLEDGE IN THE INTRODUCTORY MATH COURSE (MATE3001) ON THE UNIVERSITY OF PUERTO RICO CAMPUS. THE LNT CONTRIBUTED TO: (1) STUDENTS IMPROVED THEIR STUDY HABITS; (2) THE STUDENTS HAD GREATER PARTICIPATION IN THE SOLUTION OF MATH PROBLEMS, THEIR PRACTICE AND DISCUSSION; (3) THEY ACCEPTED THAT THE RESEARCH PROFESSOR SUPERVISE THEIR WORK AS IT WAS CARRIED OUT AND UNDERSTOOD THAT THE PRESENCE WAS FOR THEIR BENEFIT. <https://doi.org/10.37626/GA9783959871129.0.109> VACARETU, ARIANA-STANCA: DEVELOPING HIGH-SCHOOL STUDENTS’ COMPETENCES THROUGH MATH RESEARCH WORKSHOPS – THE M&L PROJECT. pp 587 – 592 MATHEMATICS IS OR IT SHOULD BE ABOUT PROBLEM SOLVING AND MATH THINKING. HOWEVER, WHAT MATHEMATICS STUDENTS LEARN IN SCHOOLS IS MORE ABOUT PROCEDURES FOR SOLVING DIFFERENT TYPES OF MATH EXERCISES AND PROBLEMS. IN MANY CASES, STUDENTS LEARN BY HEART ALGORITHMS AND WORDS (MATH CONCEPTS) AND USE THEM FOR SOLVING DIFFERENT MATH TASKS. SCHOOL MATH IS VERY FAR FROM WHAT MATHEMATICIANS DO AND, IN MANY CASES, DOESN’T MOTIVATE STUDENTS FOR LEARNING MATH. THIS PAPER PRESENTS THE WAY WE ORGANIZED THE ASSESSMENT OF THE STUDENTS’ SKILLS DEVELOPED THROUGH MATH RESEARCH WORKSHOPS AND SOME OF THE ASSESSMENT RESULTS. EVEN THOUGH WE DIDN’T ASSESS ALL THE COMPETENCES THE

STUDENTS DEVELOP THROUGH THE MATH RESEARCH WORKSHOP, THE FINDINGS SHOW THAT THE STUDENTS CERTAINLY DEVELOP THEIR PROBLEM-SOLVING SKILLS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.110](https://doi.org/10.37626/GA9783959871129.0.110) WALSH JR., THOMAS: EXPLORING COMPUTER SCIENCE WITH MICROWORLDS EX TO LEARN GEOMETRY AND LOGO PROGRAMMING CODE. PP 593 – 598 FUTURE EMPLOYMENT OF COMPUTER-PROGRAMMING JOBS WILL BE BEST FOR APPLICANTS WITH EXPERIENCE IN DIFFERENT LANGUAGES AND CODING TOOLS (BUREAU OF LABOR STATISTICS, 2018). EMPIRICAL AND META-ANALYSIS RESEARCH STUDIES SUPPORT OF TEACHING LOGO PROGRAMMING IN DEVELOPING STUDENT COGNITIVE PROBLEM-SOLVING SKILLS HAS BEEN DOCUMENTED. USING GUIDED INSTRUCTION WITH TEACHER-MEDIATED SCAFFOLDING EXPLORING COMPUTER SCIENCE WITH MICROWORLDS EX (WALSH, 2013-2017) HAS BEEN FOUND AS AN EFFECTIVE METHOD IN PREPARING STUDENTS USING THE LOGO CODE PROGRAMMING LANGUAGE TO CREATE GEOMETRIC GRAPHIC, ANIMATION, AND GAMING PROJECTS. MORE RESEARCH IS NEEDED TO STUDY TEACHER SCAFFOLDING AND MEDIATION SKILLS TO SUPPORT LEARNING LOGO CODING AND TRANSFER TO OTHER DOMAINS INCLUDING OTHER PROGRAMMING ENVIRONMENTS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.111](https://doi.org/10.37626/GA9783959871129.0.111) WALSH JR., THOMAS: THE SURVEY TOOLKIT CURRICULUM METHODOLOGY FOR RESEARCHING INFORMATION, SURVEY QUESTIONING, AND ANALYZING DATA WITH TINKERPLOTS. PP 599 – 604 IN AN ERA WHERE SOCIAL MEDIA TRAFFICS FAKE NEWS WEBSITES THAT PUBLISHES MISINFORMATION IT IS IMPERATIVE TO PROVIDE STUDENTS' EXPERIENCES IN THE SURVEY TOOLKIT AND TINKERPLOTS CURRICULUM TEACHING SOUND RESEARCH PRINCIPLES AND INFORMATION GATHERING TECHNIQUES. THE FIELD-TESTED PROGRAM WAS FOUND EFFECTIVE IN GUIDING STUDENTS CHOOSING RESEARCH QUESTIONS, WRITING A RESEARCH REPORT USING A PARAGRAPH CLUSTER INFORMATION STRATEGY, DEVELOPING UNBIASED SURVEY QUESTIONS USING RELIABLE SAMPLING, ANALYZING SURVEY DATA WITH TINKERPLOTS, AND SHARING RESULTS. THE PAPER WILL PRESENT SUPPORT FOR TEACHING THE CURRICULUM, DEVELOPMENT BASED ON RESEARCH DIRECTION, IMPLEMENTATION CONSIDERATIONS, AND USE OF THE CURRICULUM WITH ELEMENTARY TO MIDDLE SCHOOL STUDENTS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.112](https://doi.org/10.37626/GA9783959871129.0.112) WARREN, LYNÆ; WOHLHUTER, KAY: MERGING THEORY AND PRACTICE IN STATISTICS IN COMMUNITIES OF MATHEMATICAL INQUIRY. PP 605 – 606 THIS WORKSHOP WILL ENGAGE PARTICIPANTS IN STATISTICAL PROBLEM SOLVING WITH REALLIFE DATA, USING TECHNOLOGY. PARTICIPANTS WILL WORK IN A COMMUNITY OF INQUIRY, (COI, GARRISON, 2016) WITH OTHER PARTICIPANTS TO FORMULATE QUESTIONS THAT WILL BE ANSWERED IN THEIR COMMUNITY. THE PARTICIPANTS WILL ENGAGE IN PROBLEM SOLVING USING 2018 DATA ABOUT WORLD POPULATIONS, TO DETERMINE HOW BEST TO ANSWER THEIR QUESTIONS AND HOW THEIR ANSWERS MAY BECOME PART OF A LARGER EXPLORATION. THE FACILITATORS WILL SHARE EXAMPLES FROM THEIR WORK WITH DEVELOPMENTAL MATHEMATICS STUDENTS AND MATHEMATICS TEACHER CANDIDATES REGARDING HOW THEY USE THE COI MODEL TO MERGE THEORY AND PRACTICE IN THE AREAS OF: TEACHING & LEARNING, EDUCATIONAL TECHNOLOGY, CURRICULUM DEVELOPMENT, TEACHERS' PREPARATION AND DEVELOPMENT, AND ISSUES OF EQUITY. PARTICIPANTS WILL NEED ACCESS TO A COMPUTER OR TABLET WITH WEB ACCESS AND SPREADSHEET SOFTWARE. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.113](https://doi.org/10.37626/GA9783959871129.0.113) WATSON, STEVEN: BRIDGING THEORY AND PRACTICE: A POSTHUMAN PERSPECTIVE ON MATHEMATICS TEACHER EDUCATION. PP 607 – 612 THIS PAPER CONSIDERS POSTHUMANISM IN THE CONTEXT OF MATHEMATICS TEACHER PROFESSIONAL LEARNING. POSTHUMANISM PRESENTS A CHALLENGE TO ENLIGHTENMENT RATIONALITY AND THE PRIVILEGED POSITION AND POTENTIAL CAPABILITY OF THE HUMAN MIND. POSTHUMAN PERSPECTIVES PRESENT KNOWLEDGE AND KNOWING AS AN EMBODIED AND EXPERIENTIAL PROCESS. LEARNING, THEN, IS NOT SIMPLY ABOUT THE ACQUISITION OF KNOWLEDGE AND SKILLS, IT IS AN EMBODIED EXPERIENCE IN WHICH THE LEARNER ACTS WITHIN AN ENVIRONMENT AND COMES TO MAKE SENSE OF THIS EXPERIENCE THROUGH A REFLECTIVE PROCESS. AS WELL AS PRESENTING A THEORETICAL ACCOUNT OF MATHEMATICS PROFESSIONAL LEARNING AND THE IMPLICATIONS OF THE POSTHUMAN TO THIS FIELD, I ILLUSTRATE THIS WITH MY OWN RESEARCH IN MATHEMATICS TEACHERS' PRESERVICE EDUCATION AND THE PROFESSIONAL DEVELOPMENT OF PRACTISING TEACHERS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.114](https://doi.org/10.37626/GA9783959871129.0.114) WEBB, LYN; ET AL: ENABLING GRADE 3 TEACHERS TO TRANSFORM AN INTENDED CURRICULUM INTO AN ENACTED CURRICULUM IN MATHEMATICS CLASSROOMS. PP 613 – 617 THE INTRODUCTION OF A NEW MATHEMATICS CURRICULUM IS USUALLY HERALDED BY THE PRODUCTION OF A PLETHORA OF LEARNER WORKBOOKS AND TEACHER AIDS. IN SOUTH AFRICA THIS STUDY RESEARCHES THE EFFECT OF CURRICULUM CHANGE ON GRADE 3 MATHEMATICS TEACHERS IN AN ENDEAVOUR TO UNDERSTAND WHAT ELEMENTS ENABLE THE TRANSITION FROM AN INTENDED CURRICULUM TO AN ENACTED CURRICULUM. THE THEORETICAL FRAMING FOR THIS PAPER IS FULLAN'S (2006) CHANGE THEORY THAT FOCUSES ON NEW MATERIALS, NEW PRACTICES AND NEW BELIEFS. THE RESEARCH IDENTIFIES THAT CURRENT SOUTH AFRICAN CURRICULUM DOCUMENTS AND WORKBOOKS FOCUS ON MATHEMATICAL CONTENT ALMOST EXCLUSIVELY, AND GIVE MINIMAL GUIDANCE CONCERNING PEDAGOGICAL CONTENT KNOWLEDGE AND TEACHER AGENCY. A TRI-LEVEL SYSTEM IS SUGGESTED TO NARROW THE GAP BETWEEN POLICY AND PRAXIS. [HTTPS://DOI.ORG/10.37626/GA9783959871129.0.115](https://doi.org/10.37626/GA9783959871129.0.115) WEBB, PAUL: TOWARDS UNIFYING LOGIC FOR THE PEDAGOGY OF MATHEMATICS IN SOUTH AFRICA. PP 618 – 622 SOUTH AFRICA'S PERFORMANCE IN MATHEMATICS AT SCHOOL LEVEL IS NOT IMPRESSIVE, EVEN WHEN MEASURED AGAINST COUNTRIES WITH FEWER RESOURCES. AS A COUNTRY, IT IS ONE OF THE LOWEST PERFORMERS IN THE WORLD WITH A WIDE RANGE OF ACHIEVEMENT BETWEEN SCHOOLS, WITH HISTORICALLY WHITE SCHOOLS ACHIEVING RESULTS MUCH CLOSER TO THE INTERNATIONAL AVERAGE COMPARED TO HISTORICALLY-BLACK AFRICAN SCHOOLS. THE SOUTH AFRICAN NATIONAL PLANNING COMMISSION HAS IDENTIFIED MATHEMATICS EDUCATION AS A KEY AREA OF CONCERN, PARTICULARLY AMONGST POOR CHILDREN. IN RESPONSE, THE MAPUNGBWE INSTITUTE FOR STRATEGIC REFLECTION (MISTRA) INITIATED A RESEARCH PROJECT TO EXPLORE THE POSSIBILITY OF A 'UNIFYING PEDAGOGY' THAT COULD HELP

IMPROVE MATHEMATICS TEACHING ACROSS THE RANGE OF SCHOOLS IN THE COUNTRY. THIS PAPER PRESENTS A SUMMARY OF THE 'CUMULATIVE RESONANCES' OF 'SAGACIOUS' MEMBERS OF THE MATHEMATICS EDUCATION COMMUNITY IN SOUTH AFRICA AND ABROAD. THE DATA GENERATED BY THESE 'SAGACIOUS' SOURCES' IN ACADEMIA AND GOVERNMENTAL AND NON-GOVERNMENTAL ORGANISATIONS WERE ANALYSED THEMATICALLY IN ORDER TO EXPLORE THE POSSIBILITY OF FRAMING A UNIFYING PEDAGOGY OF MATHEMATICS FOR SOUTH AFRICAN CONDITIONS. <https://doi.org/10.37626/GA9783959871129.0.116> WICKLIFF, GREGORY A.; ET AL: COMMUNICATING MATHEMATICS AND SCIENCE: TEACHING AND TUTORING WRITING IN A SUMMER PROGRAM FOR HIGH SCHOOL STUDENTS. PP 623 – 628 SUPPLEMENTAL INSTRUCTION AND TUTORING IN WRITING, GENRE, AND DOCUMENT DESIGN AND ILLUSTRATION, CAN IMPROVE THE QUALITY OF FORMAL MATHEMATICS AND SCIENCE PAPERS AND PRESENTATIONS COMPOSED BY RISING HIGH SCHOOL JUNIOR AND SENIOR STUDENTS IN A FOUR-WEEK SUMMER PROGRAM. THIS PAPER DISCUSSES THE PROGRAM HISTORY AND GOALS, ITS STRUCTURE, THE METHODS OF INSTRUCTION AND TUTORING, AND THE PROFESSIONAL AND STUDENT WRITING SAMPLES DELIVERED THROUGH THE UNIVERSITY OF NORTH CAROLINA AT CHARLOTTE'S SUMMER VENTURES IN SCIENCE AND MATHEMATICS PROGRAM. THE PROGRAM IS A NO-COST, STATE-FUNDED PROGRAM FOR ACADEMICALLY TALENTED STUDENTS WHO ASPIRE TO CAREERS IN SCIENCE, TECHNOLOGY, ENGINEERING, AND MATHEMATICS. PARTICIPANTS RESIDE ON THE UNIVERSITY CAMPUS FOR FOUR WEEKS AND CONDUCT RESEARCH AROUND TOPICS OF THEIR OWN INTEREST INDIVIDUALLY OR IN COLLABORATION WITH LIKE-MINDED PEERS. PARTICIPANTS ENGAGE IN RESEARCH UNDER THE SUPERVISION OF UNIVERSITY FACULTY. <https://doi.org/10.37626/GA9783959871129.0.117> WILLSON, IAN: FORMATIVE ASSESSMENT AND MIDDLE-SCHOOL CLASSROOM TASKS WITH THE WOLFRAM LANGUAGE. PP 629 – 630 MIDDLE-SCHOOL CLASSROOM TASKS WITH THE WOLFRAM LANGUAGE CAN PLAY A VERY SIGNIFICANT ROLE IN THE GROWTH AND DEVELOPMENT OF MATHEMATICAL COMPETENCE. THIS CAN OCCUR AT THE INTERSECTION OF CHALLENGING MATHEMATICAL TASKS, CODING SKILLS, EXPLORATION, DISCOVERY, COLLABORATION AND FORMATIVE ASSESSMENT. THIS WORKSHOP WILL REFERENCE ALL OF THESE ELEMENTS AS THEY INFORMED AND UNDERPINNED CLASSROOM ACTIVITIES CONDUCTED AT SEVERAL DIFFERENT SECONDARY SCHOOLS IN MELBOURNE AUSTRALIA. <https://doi.org/10.37626/GA9783959871129.0.118> WOODCOCK, STEPHEN: NOT ALL EQUALS ARE EQUAL: DECOUPLING THINKING PROCESSES AND RESULTS IN MATHEMATICAL ASSESSMENTS. PP 631 – 636 ONE OF THE GREATEST CHALLENGES IN MATHEMATICS EDUCATION IS IN FOSTERING AN UNDERSTANDING OF WHAT MATHEMATICIANS WOULD RECOGNISE AS "MATHEMATICAL THOUGHT." WE SEEK TO ENCOURAGE STUDENTS TO DEVELOP THE TRANSFERABLE SKILLS OF ABSTRACTION, PROBLEM GENERALIZATION AND SCALABILITY AS OPPOSED TO SIMPLY ANSWERING THE SPECIFIC QUESTION POSED. THIS DIFFERENCE IS PERHAPS BEST ILLUSTRATED BY THE FAMOUS – BUT LIKELY APOCRYPHAL – TALE OF GAUSS'S SCHOOL DAYS AND HIS APPROACH TO SUMMING ALL POSITIVE INTEGERS UP TO AND INCLUDING 100, RATHER THAN JUST SUMMING EACH SEQUENTIALLY. ESPECIALLY WITH THE RISE OF TECHNOLOGY-ENABLED MARKING AND RESULTS-FOCUSSED TUTORING SERVICES, THE ONUS IS ON THE EDUCATOR TO DEVELOP NEW TYPES OF QUESTION WHICH ENCOURAGE AND REWARD THE DEVELOPMENT OF MATHEMATICAL PROCESSES AND DEPRIORITISE RESULTS ALONE. SOME INITIAL WORK IN THIS AREA IS PRESENTED HERE. <https://doi.org/10.37626/GA9783959871129.0.119> ZELL, SIMON: WEEKLY 10-MINUTE-TASKS TO PROMOTE STUDENTS SOLVING EQUATIONS IN A CONTENT-ORIENTED MANNER. PP 637 – 642 WHEN SOLVING EQUATIONS IN SCHOOL, STUDENTS OFTEN RELY ON ROUTINES AND DO NOT CONSIDER ALTERNATIVE WAYS OF SOLVING. EVEN BASIC EQUATIONS WHICH COULD BE SOLVED QUITE FAST USING COMMON SENSE ARE REGULARLY SOLVED IN A COMPLICATED WAY. TO OVERCOME THIS RELIANCE ON ROUTINE, A STUDY WITH 17 CLASSES OF GRADE 10 STUDENTS WAS CARRIED OUT. WEEKLY 10-MINUTE-TASKS, WHICH CONTAINED APPROPRIATE SUBTASKS TO ENHANCE CONTENT-ORIENTED SOLVING, WERE SOLVED BY STUDENTS OVER THE COURSE OF ONE SCHOOL YEAR. THESE TASKS WERE DESIGNED WITH THE PURPOSE OF REDUCING THE DOMINANCE OF ROUTINES AND THE AIM OF USING INSIGHT IN THE SOLVING OF EQUATIONS. <https://doi.org/10.37626/GA9783959871129.0.120> ZOLLMAN, ALAN: COLLECTIVE PARTICIPATION: A STORY OF BUSINESS, COMMUNITY, SCHOOLS, AND UNIVERSITY PARTNERING IN STEM EDUCATION. PP 643 – 648 THE QUALITY OF THE PUBLIC SCHOOL TEACHER HAS THE GREATEST IN-SCHOOL IMPACT ON NURTURING COGNITIVE ABILITIES, DEVELOPING CONTENT KNOWLEDGE, AND INCREASING MOTIVATION OF STUDENTS (FERGUSON & LADD 1996; HAYCOCK 1998; RIVKIN, HANUSHEK, & KAIN 2005; RICE 2003; SANDERS & RIVERS, 1996; ZOLLMAN, TAHERNEZHADI, & BILLMAN, 2012). WE ALSO KNOW FROM EDUCATIONAL RESEARCH (JOHNSON & SONDERGELD, 2015) THAT TRADITIONAL PROFESSIONAL DEVELOPMENT FORMATS DO NOT RESULT IN IMPROVEMENT OF TEACHER PRACTICES NOR SUBSTANTIAL GAIN IN STUDENT ACHIEVEMENT. THIS PAPER REPORTS ON A SHIFT IN THE TRADITIONAL PROFESSIONAL DEVELOPMENT PROJECT – ONE TO ENHANCE THE QUALITY OF THE PUBLIC SCHOOL TEACHER IN STEM EDUCATION PROJECTS THROUGH A SYNERGY OF BUSINESS, COMMUNITY, AND SCHOOL DISTRICTS PARTNERS WITH EDUCATION AND SCIENCE UNIVERSITY FACULTY. <https://doi.org/10.37626/GA9783959871129.0.121> ZONNEFELD, RYAN G.; ZONNEFELD, VALORIE L.: INNOVATIVE PATHWAYS IN STEM TEACHER PREPARATION: BRIDGING THE GAP BETWEEN UNIVERSITY EXPECTATIONS & SECONDARY SCHOOL NEEDS. PP 649 – 651 INNOVATIVE TEACHER PREPARATION PROGRAMS FOR STEM EDUCATION ARE ESSENTIAL FOR MEETING THE GOAL OF ENSURING THAT SECONDARY SCHOOL STUDENTS RECEIVE INSTRUCTION FROM A CERTIFIED TEACHER. THIS EXPLORATORY WORKSHOP EXAMINES THE ROLE THAT INTERDISCIPLINARY STEM AND MATHEMATICS PROGRAMS CAN HAVE TO INCREASE THE NUMBER OF CERTIFIED TEACHERS PREPARED TO TEACH STEM CLASSES FROM AN INTERDISCIPLINARY APPROACH. <https://doi.org/10.37626/GA9783959871129.0.122>

*BUILDING POWERFUL NUMERACY FOR MIDDLE AND HIGH SCHOOL STUDENTS* PAMELA WEBER HARRIS 2011 "I CONTINUE TO BE AMAZED AT THE POWER WE CAN HARNESS IN OUR SECONDARY STUDENTS BY TEACHING OURSELVES AND OUR STUDENTS REAL NUMERACY." --PAMELA HARRIS AS SECONDARY MATH TEACHERS, WE'RE OFTEN FRUSTRATED BY THE LACK OF TRUE NUMBER SENSE IN OUR STUDENTS. SOLID RESEARCH AT THE ELEMENTARY LEVEL SHOWS HOW TO HELP ALL STUDENTS BECOME MATHEMATICALLY PROFICIENT BY REDEFINING WHAT IT MEANS TO COMPUTE WITH NUMBER SENSE. PAM HARRIS HAS SPENT THE PAST TEN YEARS SCRUTINIZING THE RESEARCH AND USING THE RESULTING REFORM MATERIALS WITH TEACHERS AND STUDENTS, SEEING WHAT WORKS AND WHAT DOESN'T WORK, ALWAYS WITH AN EYE TO SUCCESS IN HIGHER MATH. THIS BOOK BRINGS THESE INSIGHTS TO THE SECONDARY WORLD, WITH AN EMPHASIS ON ONE POWERFUL GOAL: BUILDING NUMERACY. DEVELOPING NUMERACY IN TODAY'S MIDDLE AND HIGH SCHOOL STUDENTS IS REFLECTIVE OF THE COMMON CORE STATE STANDARDS MISSION TO BUILD "THE SKILLS THAT OUR YOUNG PEOPLE NEED FOR SUCCESS IN COLLEGE AND CAREERS." (CCSS 2010) NUMERACY IS MORE THAN THE ABILITY TO DO BASIC ARITHMETIC. AT ITS HEART, NUMERACY IS THE ABILITY TO USE MATHEMATICAL RELATIONSHIPS TO REASON WITH NUMBERS AND NUMERICAL CONCEPTS, TO THINK THROUGH THE MATH LOGICALLY, TO HAVE A REPERTOIRE OF STRATEGIES TO SOLVE PROBLEMS, AND TO BE ABLE TO APPLY THE LOGIC OUTSIDE OF CLASSROOMS. HOW CAN WE BUILD POWERFUL NUMERACY IN MIDDLE AND SECONDARY STUDENTS? HARRIS'S APPROACH EMPHASIZES TWO BIG IDEAS: TEACH THE IMPORTANCE OF REPRESENTATION. THE REPRESENTATION OF STUDENT STRATEGIES ON MODELS SUCH AS THE OPEN NUMBER LINE, THE OPEN ARRAY, AND THE RATIO TABLE PROMOTE DISCUSSION ON RELATIONSHIPS RATHER THAN PROCEDURES TEACH WITH PROBLEM STRINGS. INTRODUCED BY CATHERINE TWOMEY FOSNOT AND HER COLLEAGUES IN THE YOUNG MATHEMATICIANS AT WORK SERIES, PROBLEM STRINGS ARE PURPOSEFULLY DESIGNED SEQUENCES OF RELATED PROBLEMS THAT HELP STUDENTS CONSTRUCT NUMERICAL RELATIONSHIPS. THEY ENCOURAGE STUDENTS TO LOOK TO THE NUMBERS FIRST BEFORE CHOOSING A STRATEGY, NUDGING THEM TOWARD EFFICIENT, SOPHISTICATED STRATEGIES FOR COMPUTATION. UNDERSTANDING NUMERICAL RELATIONSHIPS GIVES STUDENTS THE FREEDOM TO CHOOSE A STRATEGY, RATHER THAN BEING STUCK WITH ONLY ONE WAY TO SOLVE A PROBLEM. USING THE STRINGS AND ACTIVITIES IN THIS BOOK CAN EMPOWER YOUR STUDENTS TO REASON THROUGH PROBLEMS AND SEEK TO FIND CLEVER SOLUTIONS. THEY'LL BECOME MORE NATURALLY INCLINED TO USE THE STRATEGIES THAT MAKE SENSE TO THEM. STUDENTS BECOME ENGAGED, WILLING TO THINK, AND MORE CONFIDENT IN THEIR JUSTIFICATIONS. WHEN WE GIVE SECONDARY STUDENTS THIS NUMERICAL POWER, WE ALSO HELP THEM LEARN HIGHER MATHEMATICS WITH MORE CONFIDENCE AND MORE SUCCESS.

**INVESTIGATE MULTIPLICATION** CATHERINE TWOMEY FOSNOT 2010-10 "THE RICH, OPEN INVESTIGATIONS WE'VE DEVELOPED ALLOW CHILDREN TO ENGAGE IN MATHEMATIZING IN A VARIETY OF WAYS. WE HONOR CHILDREN'S INITIAL ATTEMPTS AT STRUCTURING AND MODELING THEIR WORLD MATHEMATICALLY, WHILE AT THE SAME TIME SUPPORTING AND CHALLENGING THEM TO ENSURE THAT IMPORTANT BIG IDEAS AND STRATEGIES ARE BEING DEVELOPED PROGRESSIVELY." -CATHERINE TWOMEY FOSNOT LEARN HOW TO ESTABLISH A VIBRANT, COLLABORATIVE MATH WORKSHOP FOR STUDENTS IN GRADES 3 THROUGH 5 AND HOW CATHERINE FOSNOT AND HER COLLEAGUES INTRODUCE EARLY MULTIPLICATION STRATEGIES AND SHOW STUDENTS HOW TO WORK WITH THE RATIO TABLE AND THE DISTRIBUTIVE PROPERTY. THROUGH 2 FOUNDATIONAL BOOKS-*INVESTIGATING MULTIPLICATION AND DIVISION: OVERVIEW* AND *THE BIG DINNER: MULTIPLICATION WITH THE RATIO TABLE* -AND NINE ONLINE VIDEO CLIPS, CATHY AND HER COLLEAGUES PROVIDE THE STRATEGIES, LESSON PLANS, AND TOOLS YOU'LL NEED TO TRANSFORM YOUR CLASSROOM INTO A COMMUNITY OF YOUNG MATHEMATICIANS. IN THE OVERVIEW BOOK CATHY PROVIDES THE PROFESSIONAL UNDERSTANDINGS NEEDED TO ESTABLISH A VIBRANT MATH WORKSHOP. AFTER CHRONICLING THE MOTIVATIONS AND IDEALS THAT INSPIRE HER WORK, CATHY DESCRIBES HOW TO HELP STUDENTS CONSTRUCT THE BIG IDEAS, STRATEGIES, AND MODELS THAT SHAPE THE LANDSCAPE OF LEARNING. ENSUING SECTIONS DESCRIBE THE ARCHITECTURE OF AN INVESTIGATION AND EXPLAIN HOW THE PREDICTABILITY OF THIS FRAMEWORK FOSTERS INDEPENDENCE AND COLLABORATION. IN ADDITION TO DESCRIBING THE MANAGEMENT SYSTEMS THAT MAKE THESE INVESTIGATIONS RIGOROUS AND RESPONSIVE, CATHY SUGGESTS WAYS TO SEQUENCE INSTRUCTION AND HIGHLIGHT HOW UNITS CAN BE USED TO ENHANCE YOUR EXISTING CURRICULUM. LIKE THE OTHER UNITS IN THE *CONTEXTS FOR LEARNING MATHEMATICS* SERIES, *THE BIG DINNER: MULTIPLICATION WITH THE RATIO TABLE* PROVIDES A TWO-WEEK SEQUENCE OF INVESTIGATIONS, MINILESSONS, GAMES, AND OTHER CONTEXTS FOR LEARNING. IN THIS UNIT THE PREPARATION OF A TURKEY DINNER INTRODUCES EARLY MULTIPLICATION STRATEGIES AND SUPPORTS AUTOMATIZING THE FACTS, USING THE RATIO TABLE, AND DEVELOPING THE DISTRIBUTIVE PROPERTY WITH LARGE NUMBERS. STRINGS OF PROBLEMS GUIDE LEARNERS TOWARD COMPUTATIONAL FLUENCY WITH WHOLE-NUMBER MULTIPLICATION AND BUILD AUTOMATICITY WITH MULTIPLICATION FACTS BY FOCUSING ON RELATIONSHIPS. THE NINE ACCOMPANYING VIDEO CLIPS INCLUDE LIVE FROM-THE-CLASSROOM VIDEO FOOTAGE OF THE UNIT IN ACTION AND NARRATED SLIDE SHOWS THAT DESCRIBE THE IDEALS THAT SHAPE THE MATH WORKSHOP AND THE THINKING BEHIND THE *CONTEXTS FOR LEARNING MATHEMATICS* SERIES. (VIDEO CLIPS ARE FREE FOR 6 MONTHS UPON REGISTRATION. YOU MUST REGISTER WITHIN 6 MONTHS OF PURCHASE.) LEARN MORE ABOUT THESE RESOURCES AND THE SERIES AT [WWW.CONTEXTSFORLEARNING.COM](http://WWW.CONTEXTSFORLEARNING.COM). THIS PACK IS PART OF FIRSTHAND'S GETTING STARTED SERIES. BRIDGING THE GAP BETWEEN EDUCATIONAL THEORY AND PRACTICE, FIRSTHAND CLASSROOM MATERIALS MODEL THE CAREFULLY CRAFTED TECHNIQUES AND LANGUAGE OF MASTER TEACHERS IN WAYS THAT HELP TEACHERS REFINE THEIR PRACTICE AND REINVENT THEIR OWN TEACHING. THE MOST COMPREHENSIVE OF THESE RESOURCES SPAN MORE THAN A YEAR OF INSTRUCTION. FIRSTHAND'S GETTING STARTED PACKS WERE CREATED FOR TEACHERS IN TRAINING AND

PROFESSIONAL BOOK STUDY GROUPS WHO WANT A COMPACT, AFFORDABLE WAY TO STUDY AND TRYOUT THESE TRANSFORMATIVE CLASSROOM MATERIALS. EACH GETTING STARTED PACK INCLUDES AN OVERVIEW BOOK, A COMPLETE UNIT OF STUDY, ONLINE VIDEO CLIPS PROVIDED FREE OF CHARGE FOR 6 MONTHS, AND AN ACCOMPANYING STUDY GUIDE. GETTING STARTED PACKS INCLUDE: LAUNCH A PRIMARY WRITING WORKSHOP, GRADES K-2; LAUNCH AN INTERMEDIATE WRITING WORKSHOP, GRADES 3-5; LAUNCH AN INTERMEDIATE READING WORKSHOP, GRADES 3-5; INTRODUCE THE QUALITIES OF WRITING, GRADES 3-6; MONITOR COMPREHENSION WITH PRIMARY STUDENTS, GRADES K-2; MONITOR COMPREHENSION WITH INTERMEDIATE STUDENTS, GRADES 3-6; INVESTIGATE THE NUMBER SYSTEM, GRADES K-3; INVESTIGATE MULTIPLICATION, GRADES 3-5; INVESTIGATE FRACTIONS, GRADES 4-6.

**MINILESSONS FOR EARLY MULTIPLICATION AND DIVISION** CATHERINE TWOMEY FOSNOT 2008-03 MINILESSONS FOR EARLY MULTIPLICATION AND DIVISION IS ONE OF TWO YEARLONG RESOURCE GUIDES IN CONTEXTS FOR LEARNING MATHEMATICS' INVESTIGATING MULTIPLICATION AND DIVISION (3-5) MINILESSONS FOR EARLY MULTIPLICATION AND DIVISION IS A RESOURCE OF 75 MINILESSONS THAT YOU CAN CHOOSE FROM THROUGHOUT THE YEAR. IN CONTRAST TO INVESTIGATIONS, WHICH CONSTITUTE THE HEART OF THE MATH WORKSHOP, THE MINILESSON IS MORE GUIDED AND MORE EXPLICIT, DESIGNED TO BE USED AT THE START OF MATH WORKSHOP AND TO LAST FOR TEN TO FIFTEEN MINUTES. EACH DAY, NO MATTER WHAT OTHER MATERIALS YOU ARE USING, YOU MIGHT CHOOSE A MINILESSON FROM THIS RESOURCE TO PROVIDE YOUR STUDENTS WITH EXPERIENCES TO DEVELOP EFFICIENT COMPUTATION. YOU CAN ALSO USE THEM WITH SMALL GROUPS OF STUDENTS AS YOU DIFFERENTIATE INSTRUCTION. THE MINILESSONS IN THIS GUIDE WERE DESIGNED TO BE USED IN GRADES 3-4. SOME OF THE MINILESSONS USE PICTURES OF REALISTIC SITUATIONS, CAREFULLY CRAFTED TO SUPPORT THE DEVELOPMENT OF SPECIFIC STRATEGIES THAT CAN BE HELPFUL IN AUTOMATIZING THE FACTS. OTHERS MAKE USE OF QUICK IMAGES WITH TEN-FRAMES AND ARRAYS. FLASHED FOR ONLY A FEW SECONDS, THE IMAGES ENCOURAGE CHILDREN TO GIVE UP TRYING TO COUNT EACH ITEM AND INSTEAD TO USE FIVE-TIMES AND TENTIMES AS HELPFUL PARTIAL PRODUCTS. OTHER MINILESSONS ARE CRAFTED AS A TIGHTLY STRUCTURED SERIES, OR "STRING," OF COMPUTATION PROBLEMS DESIGNED TO ENCOURAGE CHILDREN TO LOOK TO THE NUMBERS FIRST, BEFORE THEY DECIDE ON A COMPUTATION STRATEGY. THE STRINGS ARE LIKELY TO GENERATE DISCUSSION ON CERTAIN STRATEGIES OR BIG IDEAS UNDERLYING AN UNDERSTANDING OF EARLY MULTIPLICATION AND DIVISION. TO LEARN MORE VISIT [HTTP://WWW.CONTEXTSFORLEARNING.COM](http://www.contextsforlearning.com)

*TEACHING CHILDREN MATHEMATICS 2006*

*GUIDING CHILDREN'S LEARNING OF MATHEMATICS* ART JOHNSON 2016-12-05 THIS THOROUGH AND PRACTICAL GUIDE TO TEACHING MATHEMATICS FOR GRADES K-6 IS A PERFECT COMBINATION OF A MATH METHODS TEXT AND RESOURCE BOOK FOR PRE-SERVICE AND IN-SERVICE ELEMENTARY SCHOOL TEACHERS. THE TEXT'S ORGANIZATION USES THE COMMON CORE STATE STANDARDS AS ITS OVERARCHING FRAMEWORK. OVER 275 LESSON ACTIVITIES REINFORCE THE STANDARDS AND INCLUDE MANY EXAMPLES OF COOPERATIVE LEARNING STRATEGIES, TAKE-HOME ACTIVITIES, AND ACTIVITIES USING TECHNOLOGY SUCH AS APPS. CONTENT CHAPTERS FIRST DEVELOP A MATH TOPIC, AND THEN EXTEND THE SAME TOPIC, PROVIDING FOUNDATIONAL MATERIAL THAT CAN BE USED THROUGHOUT THE ELEMENTARY GRADES. OTHER USEFUL FEATURES HIGHLIGHT MISCONCEPTIONS OFTEN HELD ABOUT MATH OPERATIONS AND CONCEPTS, WAYS TO BE INCLUSIVE OF VARIOUS CULTURAL BACKGROUNDS, AND KEY TECHNOLOGY RESOURCES. IMPORTANT NOTICE: MEDIA CONTENT REFERENCED WITHIN THE PRODUCT DESCRIPTION OR THE PRODUCT TEXT MAY NOT BE AVAILABLE IN THE EBOOK VERSION.

CONTEXTS FOR LEARNING MATHEMATICS CATHERINE TWOMEY FOSNOT 2007-05 CONTEXTS FOR LEARNING CONSISTS OF: INVESTIGATIONS AND RESOURCE GUIDES - WORKSHOP STRUCTURE INVOLVES STUDENTS IN INQUIRING, INVESTIGATING, DISCUSSING, AND CONSTRUCTING MATHEMATICAL SOLUTIONS AND STRATEGIES - INVESTIGATIONS ENCOURAGE EMERGENT LEARNING AND HIGHLIGHT THE DEVELOPMENTAL LANDMARKS IN MATHEMATICAL THINKING - STRINGS OF RELATED PROBLEMS DEVELOP STUDENTS' DEEP NUMBER SENSE AND EXPAND THEIR STRATEGIES FOR MENTAL ARITHMETIC READ-ALoud BOOKS AND POSTERS - CREATE RICH, IMAGINABLE CONTEXTS--REALISTIC AND FICTIONAL--FOR MATHEMATICS INVESTIGATIONS - ARE CAREFULLY CRAFTED TO SUPPORT THE DEVELOPMENT OF THE BIG IDEAS, STRATEGIES, AND MODELS - ENCOURAGE CHILDREN TO EXPLORE AND GENERATE PATTERNS, GENERALIZE, AND DEVELOP THE ABILITY TO MATHEMATIZE THEIR WORLDS RESOURCES FOR CONTEXTS FOR LEARNING CD-ROM - AUTHOR VIDEOS DESCRIBE THE SERIES' PHILOSOPHY AND ORGANIZATION - VIDEO OVERVIEWS SHOW CLASSROOM FOOTAGE OF A MATH WORKSHOP, INCLUDING MINILESSONS, INVESTIGATIONS, AND A MATH CONGRESS - PRINT RESOURCES INCLUDE RESEARCH BASE, POSTERS, AND TEMPLATES

*FRACTIONAL DIFFERENTIAL EQUATIONS* IGOR PODLUBNY 1998-10-27 THIS BOOK IS A LANDMARK TITLE IN THE CONTINUOUS MOVE FROM INTEGER TO NON-INTEGER IN MATHEMATICS: FROM INTEGER NUMBERS TO REAL NUMBERS, FROM FACTORIALS TO THE GAMMA FUNCTION, FROM INTEGER-ORDER MODELS TO MODELS OF AN ARBITRARY ORDER. FOR HISTORICAL REASONS, THE WORD 'FRACTIONAL' IS USED INSTEAD OF THE WORD 'ARBITRARY'. THIS BOOK IS WRITTEN FOR READERS WHO ARE NEW TO THE FIELDS OF

FRACTIONAL DERIVATIVES AND FRACTIONAL-ORDER MATHEMATICAL MODELS, AND FEEL THAT THEY NEED THEM FOR DEVELOPING MORE ADEQUATE MATHEMATICAL MODELS. IN THIS BOOK, NOT ONLY APPLIED SCIENTISTS, BUT ALSO PURE MATHEMATICIANS WILL FIND FRESH MOTIVATION FOR DEVELOPING NEW METHODS AND APPROACHES IN THEIR FIELDS OF RESEARCH. A READER WILL FIND IN THIS BOOK EVERYTHING NECESSARY FOR THE INITIAL STUDY AND IMMEDIATE APPLICATION OF FRACTIONAL DERIVATIVES FRACTIONAL DIFFERENTIAL EQUATIONS, INCLUDING SEVERAL NECESSARY SPECIAL FUNCTIONS, BASIC THEORY OF FRACTIONAL DIFFERENTIATION, UNIQUENESS AND EXISTENCE THEOREMS, ANALYTICAL NUMERICAL METHODS OF SOLUTION OF FRACTIONAL DIFFERENTIAL EQUATIONS, AND MANY INSPIRING EXAMPLES OF APPLICATIONS. A UNIQUE SURVEY OF MANY APPLICATIONS OF FRACTIONAL CALCULUS PRESENTS BASIC THEORY INCLUDES A UNIFIED PRESENTATION OF SELECTED CLASSICAL RESULTS, WHICH ARE IMPORTANT FOR APPLICATIONS PROVIDES MANY EXAMPLES CONTAINS A SEPARATE CHAPTER OF FRACTIONAL ORDER CONTROL SYSTEMS, WHICH OPENS NEW PERSPECTIVES IN CONTROL THEORY THE FIRST SYSTEMATIC CONSIDERATION OF CAPUTO'S FRACTIONAL DERIVATIVE IN COMPARISON WITH OTHER SELECTED APPROACHES INCLUDES TABLES OF FRACTIONAL DERIVATIVES, WHICH CAN BE USED FOR EVALUATION OF ALL CONSIDERED TYPES OF FRACTIONAL DERIVATIVES

**CURRICULUM AND AIMS** DECKER F. WALKER 2004 THE REVISED FOURTH EDITION PROVIDES A BROAD PERSPECTIVE ON THE BASIC CURRICULUM QUESTIONS EDUCATORS FACE REGARDING THE PURPOSES, CONTENT, DESIGN, AND STRUCTURE OF EDUCATIONAL PROGRAMS. THE AUTHORS DEAL WITH FUNDAMENTAL CONTEMPORARY ISSUES OF CURRICULUM THEORY AND INSTRUCTIONAL PRACTICE.